

# Models of embryogenesis and biomineralization **II**

Jaap A. Kaandorp

Computational Science Lab

Faculty of Science

University of Amsterdam

Science Park 904, 1098 XH Amsterdam

The Netherlands

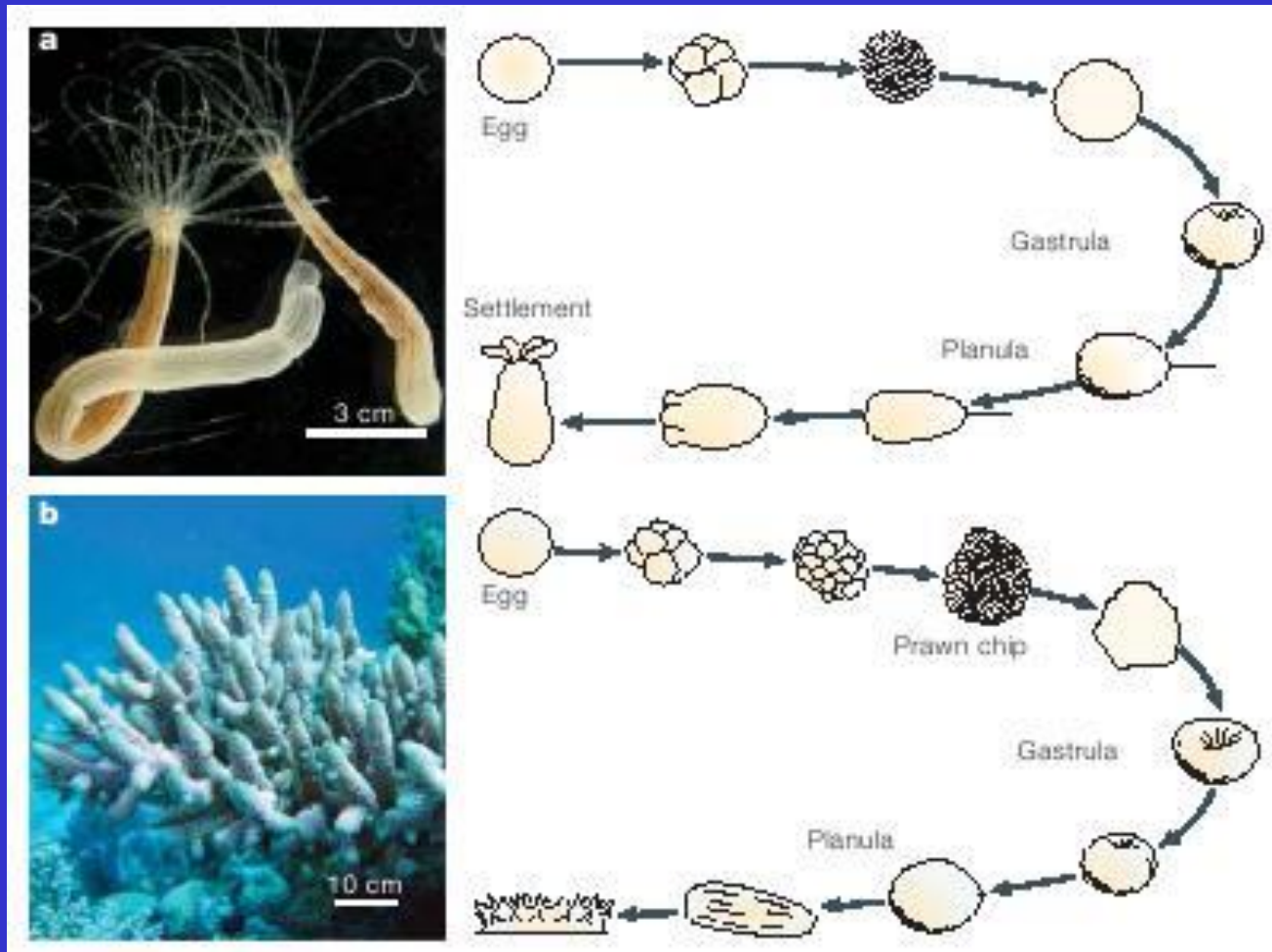
E-mail: [J.A.Kaandorp@uva.nl](mailto:J.A.Kaandorp@uva.nl)

<http://www.science.uva.nl/~jaapk>

# Overview

- Modelling gene regulation
- The sea anemone *Nematostella vectensis* case study modelling gene regulation
- Cell-based modelling of gastrulation in *Nematostella* and the hydrozoan *Clytia hemisphaerica*
- Biomineralization in the scleractinian coral *Acropora millepora*
- Modelling calcification physiology in corals
- Morphological plasticity and the physical environment in corals
- Modelling growth and form of corals (e.g. *Madracis* sp.) and the impact of the physical environment

*Nematostella vectensis* (top) / *Acropora millepora* (bottom) (Ball et al., Nature Reviews Genetics: 567, 2004)



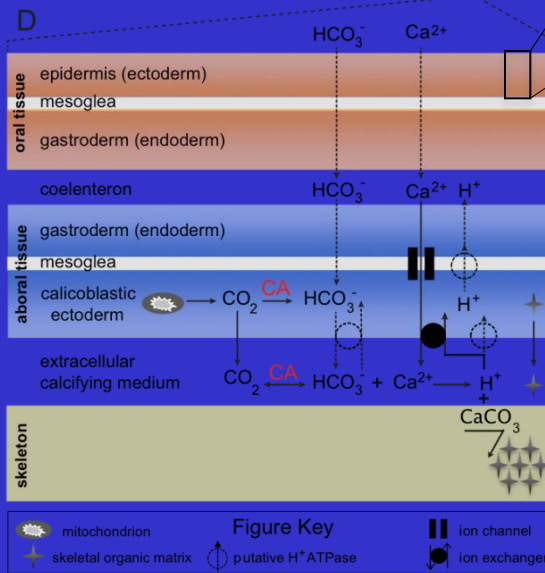
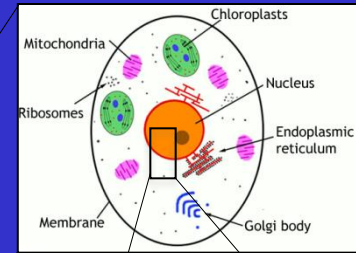
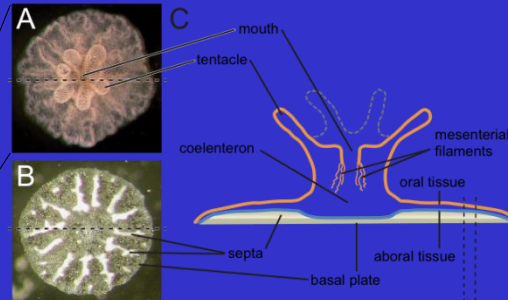
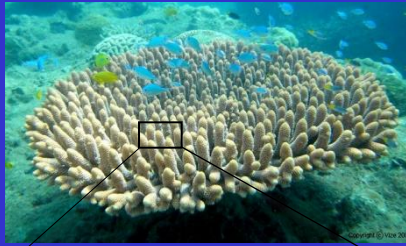
# Growth of corals: a multiscale problem

**Micromorphology**

$\mu\text{m} - \text{mm}$ ; days - weeks

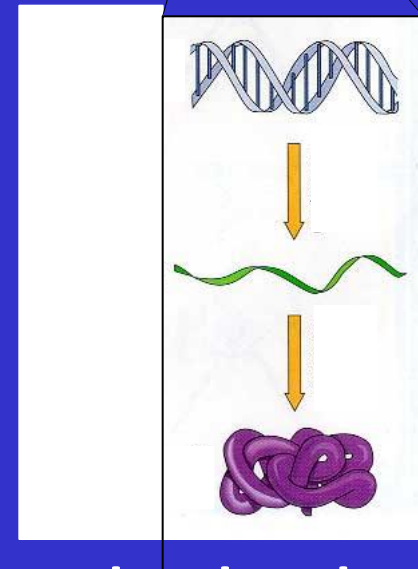
**cell physiology**

$1 - 10 \mu\text{m}$ ; ns - hours



**tissue physiology**

$1 - 100 \mu\text{m}$ ; ns -  $\mu\text{s}$



**molecular physiology**

$\text{\AA} - \text{nm}$ ; s - mins

**Macromorphology**

cm - m

months - years

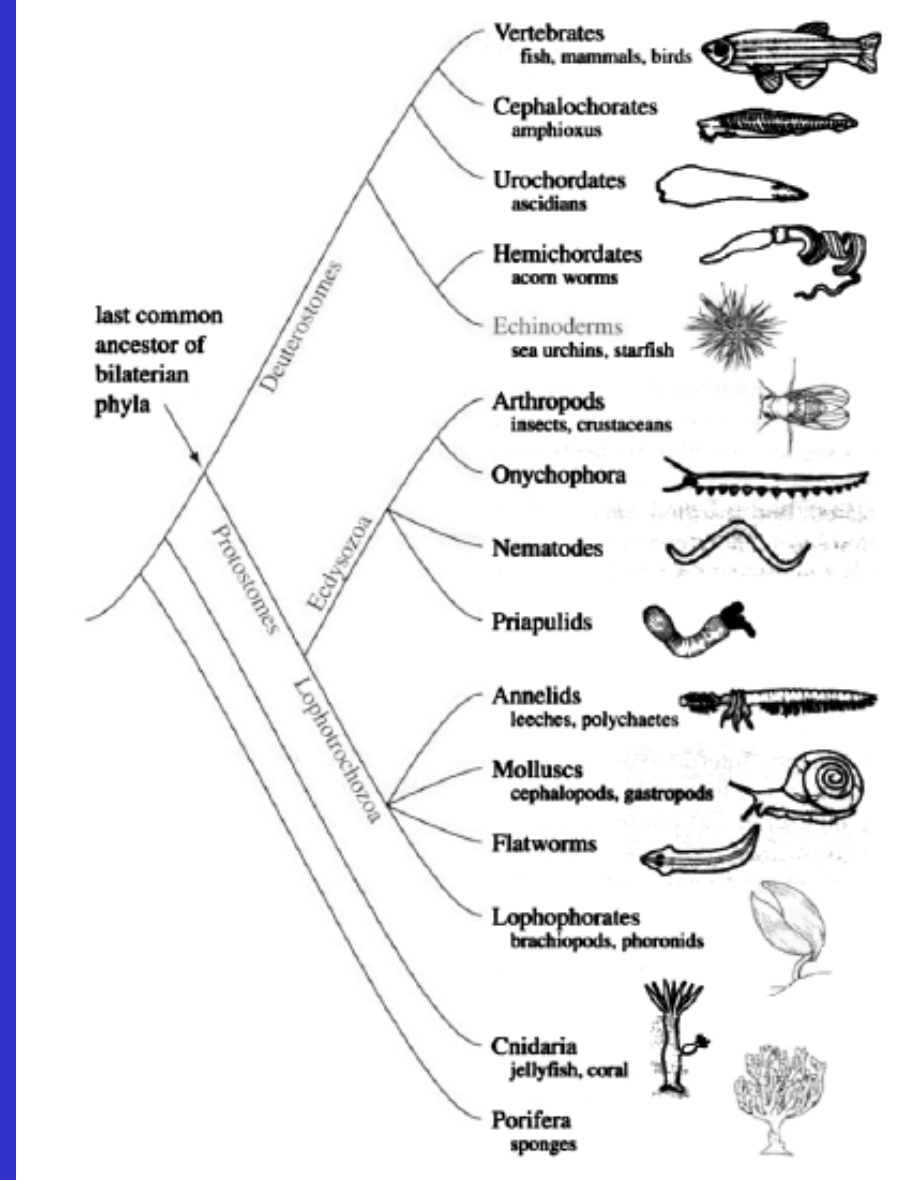
# Great Barrier Reef Australia I



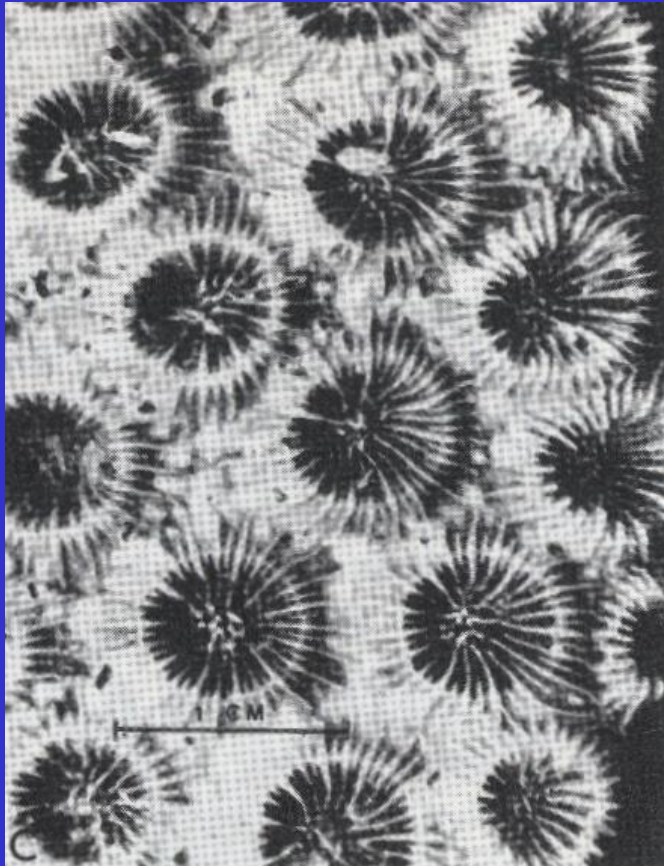
# Great Barrier Reef Australia II



# Scleractinian corals

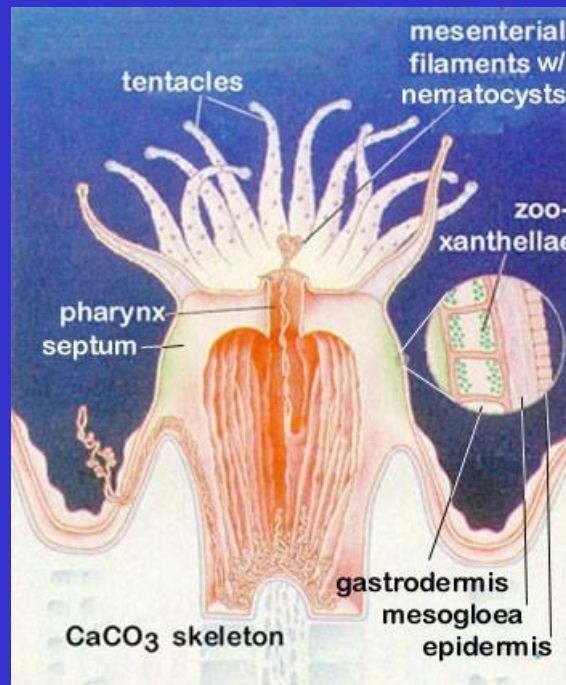


# Coral polyps

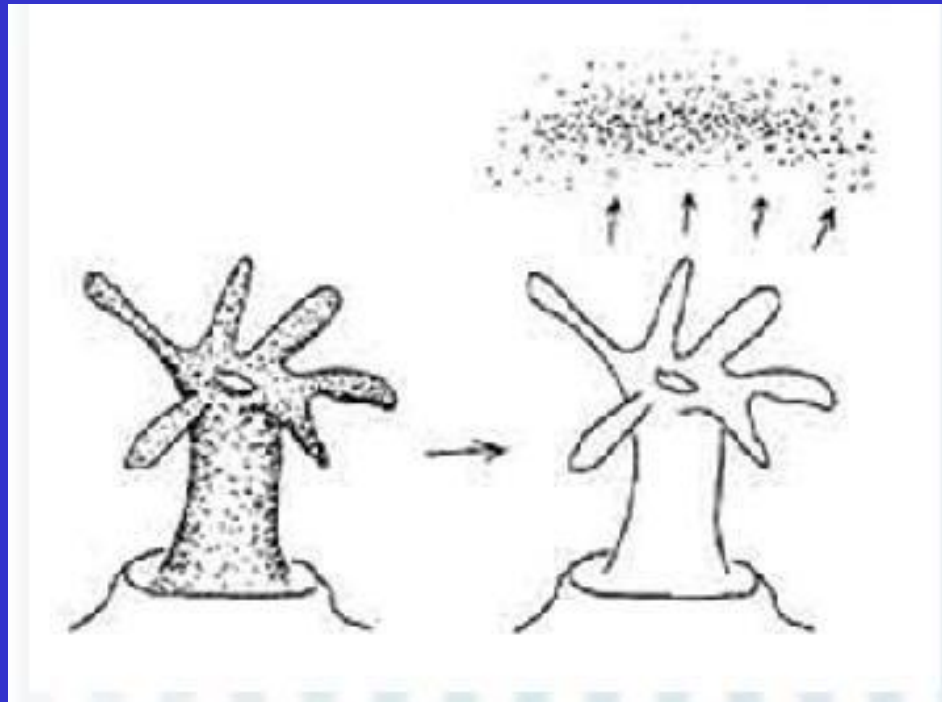




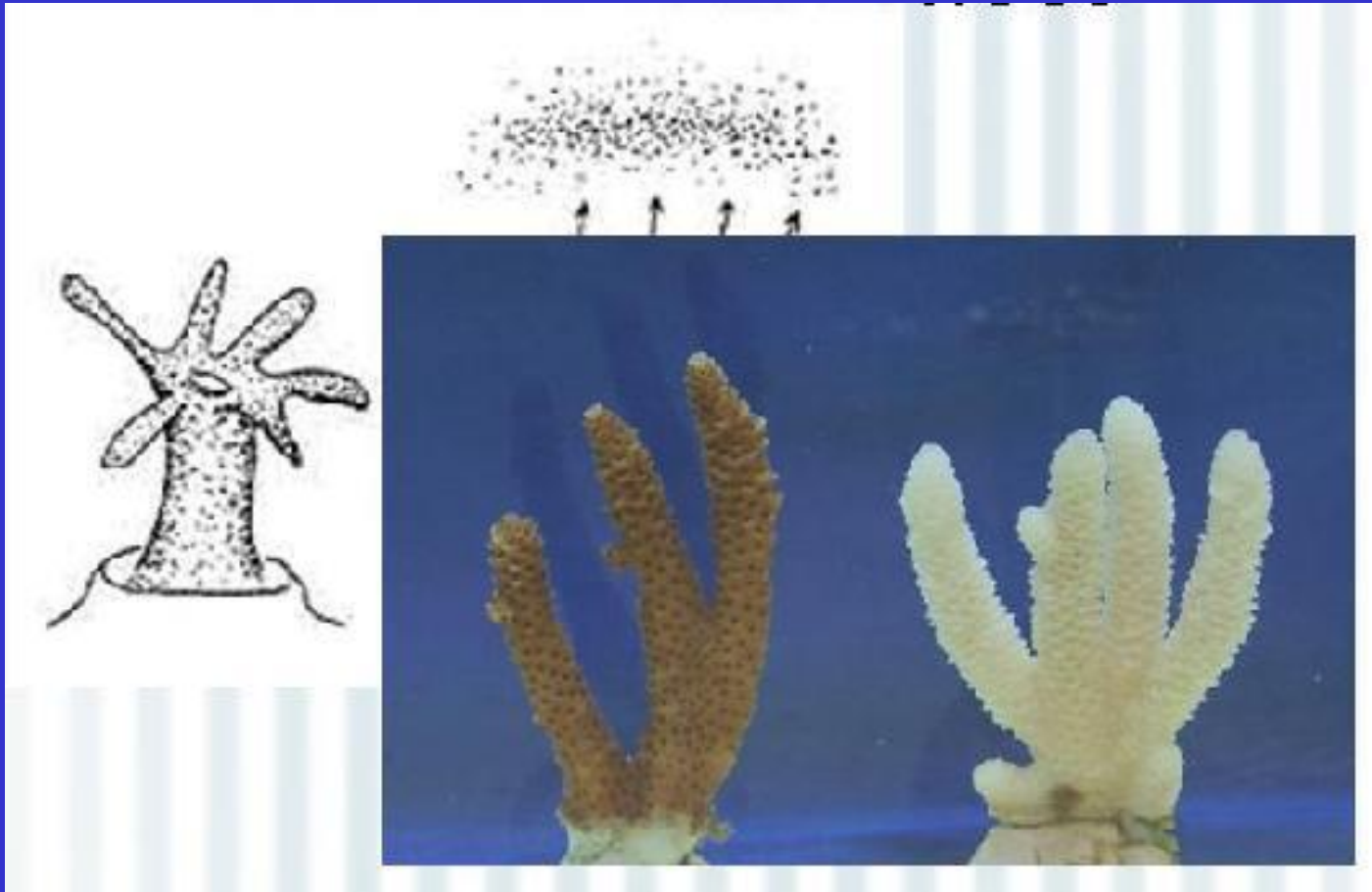
# Coral polyp with symbiotic algae (zooxanthellae)



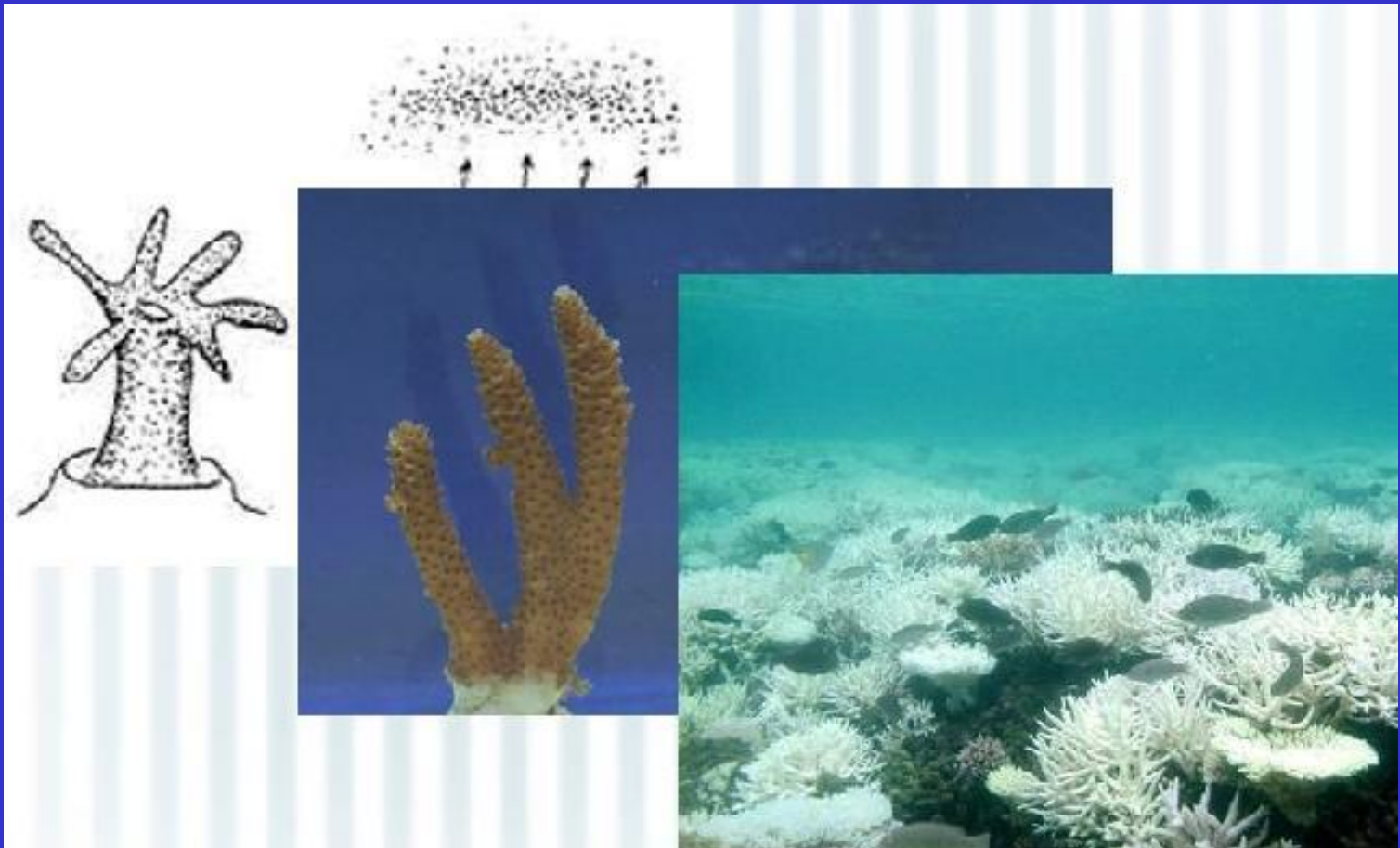
# Coral bleaching I (van Oppen, 2005)



# Coral bleaching II

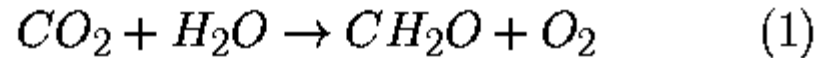


# Coral bleaching III

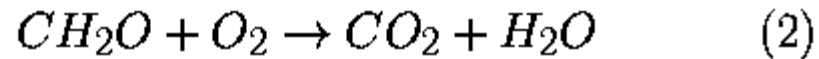


# Calcification and CO<sub>2</sub>

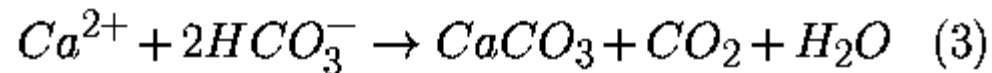
**photosynthesis**



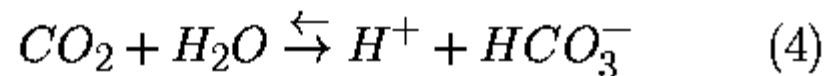
**respiration**



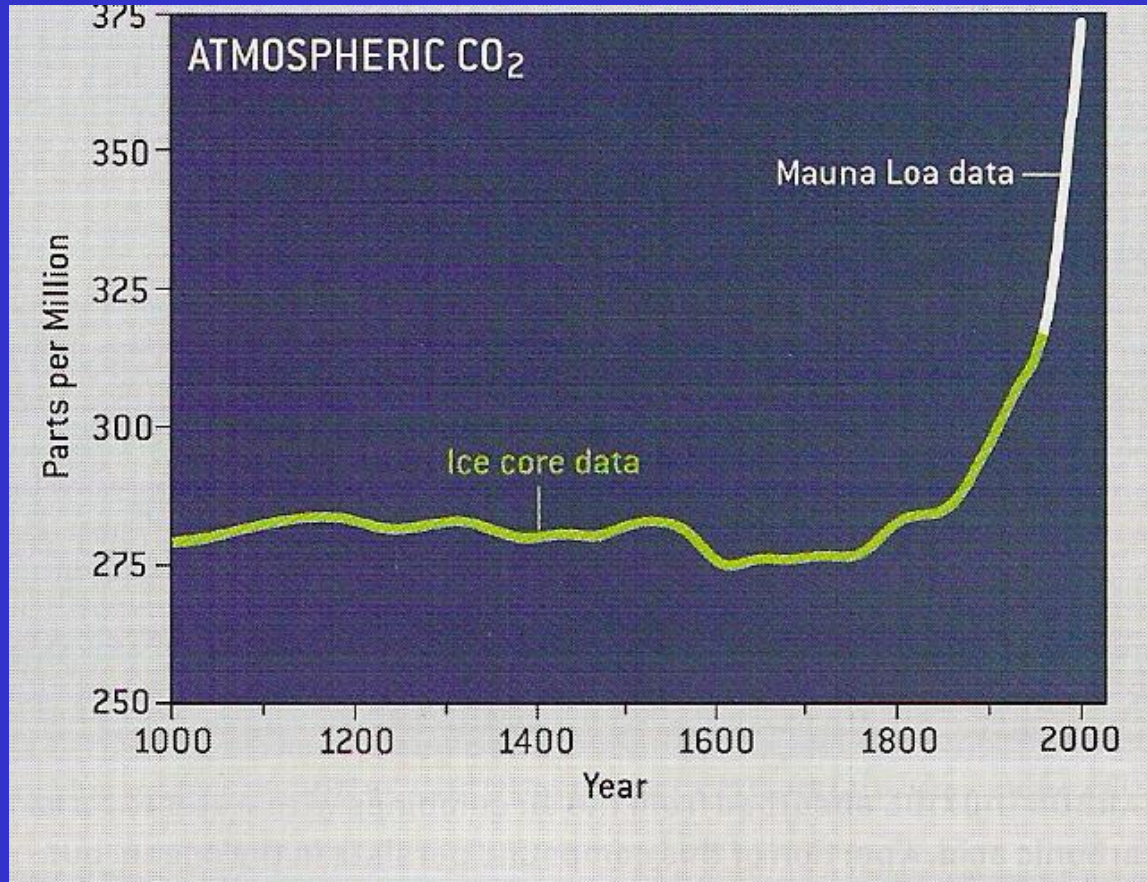
**calcification**



**equilibrium reaction**



# Acidification of oceans I



# On concretions, spicules, and specular skeletons (D.W Thompson, 1942)

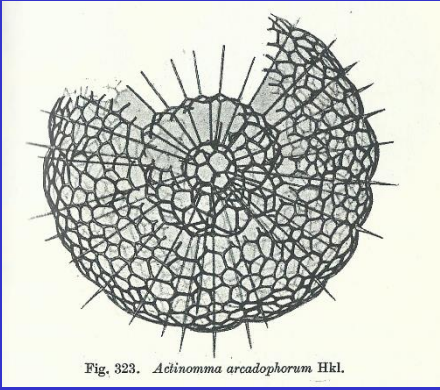


Fig. 323. *Acinomma arcadophorum* Hkl.

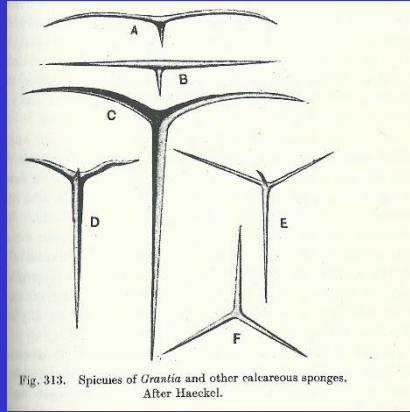


Fig. 313. Spicules of *Grantia* and other calcareous sponges. After Haeckel.

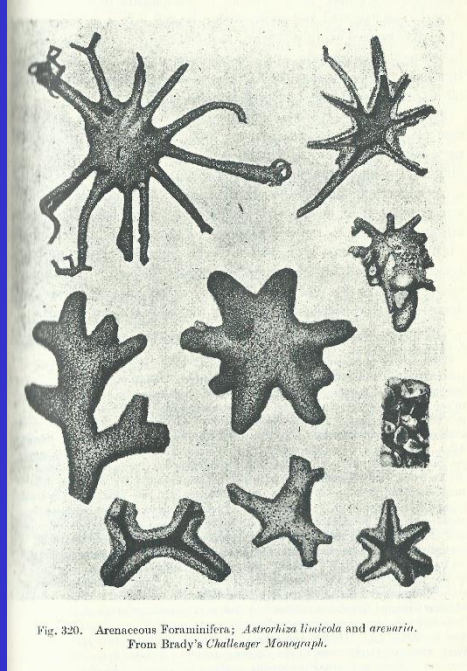


Fig. 320. Arenaceous Foraminifera: *Astorhiza limicola* and *arcuaris*. From Brady's Challenger Monograph.

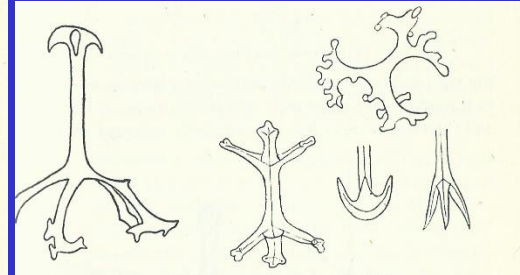


Fig. 315. Various holothurian spicules. After Théel.

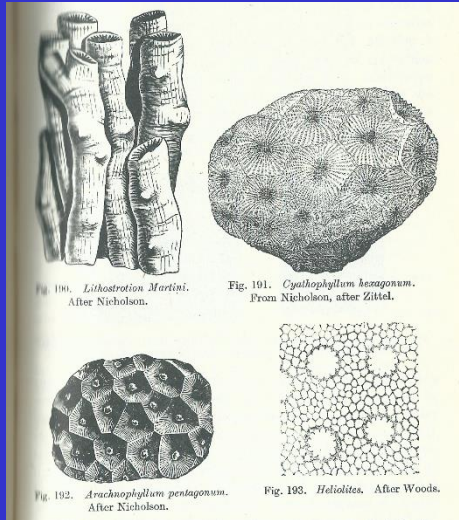


Fig. 190. *Lithostrogon Martini*. After Nicholson.

Fig. 191. *Cyathophylum hexagonum*. From Nicholson, after Zittel.

Fig. 192. *Arachnophylum pentagonum*. After Nicholson.

Fig. 193. *Heliolites*. After Woods.

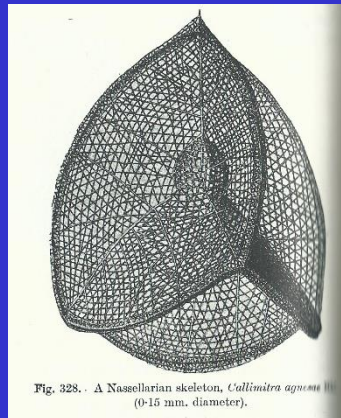


Fig. 328. A Nassellarian skeleton, *Callimitra agassa* (9-15 mm. diameter).

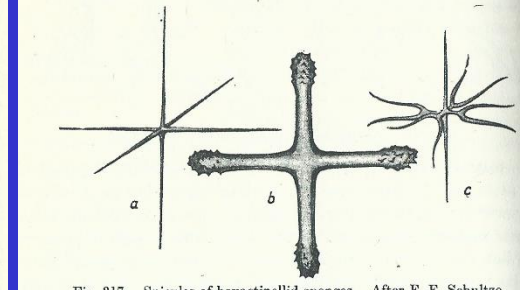


Fig. 317. Spicules of hexactinellid sponges. After F. E. Schultze.

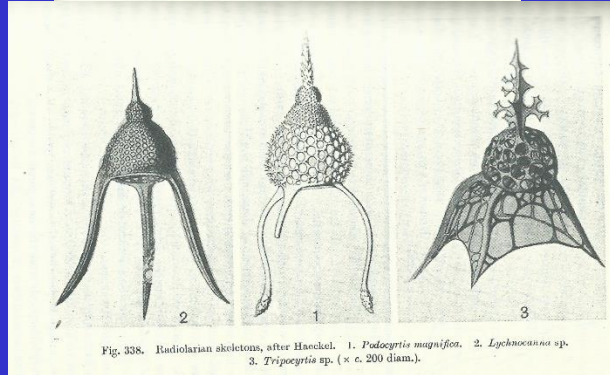


Fig. 338. Radiolarian skeletons, after Haeckel. 1. *Podocypis magnifica*. 2. *Lychnocanna* sp. 3. *Tripocypis* sp. (x c. 200 diam.).

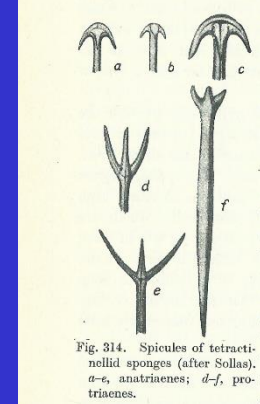
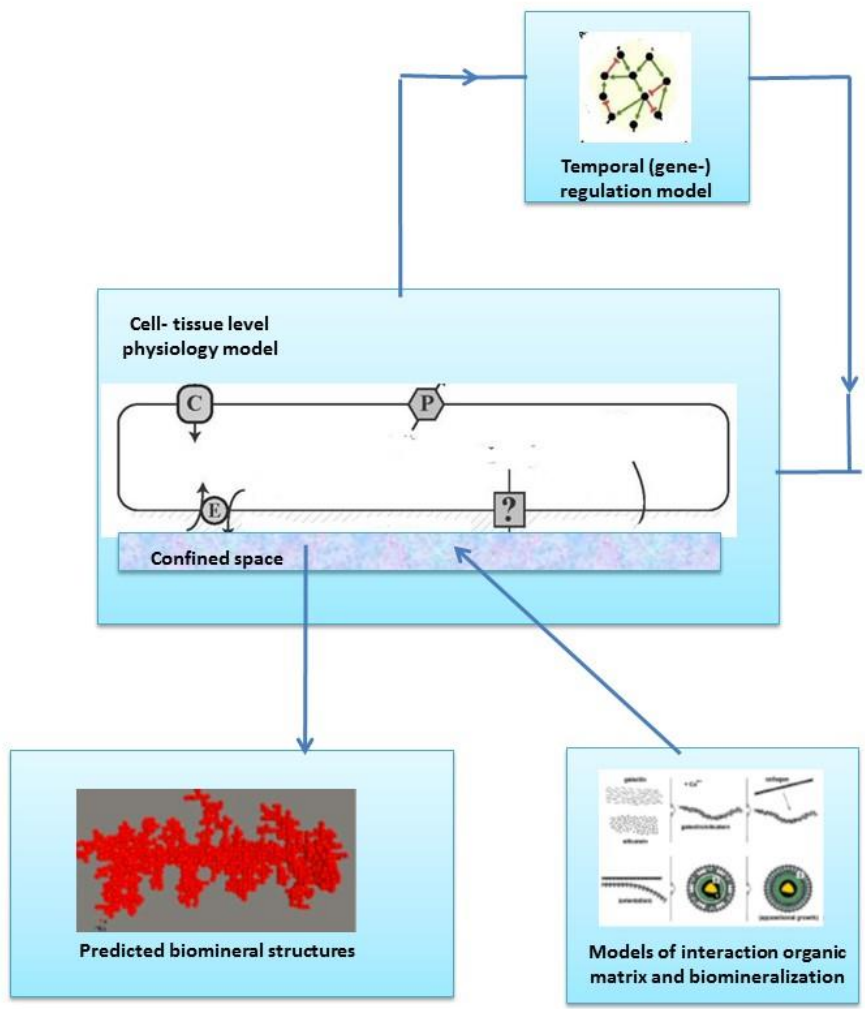


Fig. 314. Spicules of tetractinellid sponges (after Sollas). a-c, anatriaenes; d-f, protriaenes.

# Central concept of a model of biomineralization in a confined space

The cell physiology is controlling the concentrations of the inorganic components by channels, exchangers and pumps. Gene regulation controls the release of organic components in the system. The actual place of the biomineralization is confined (located in vesicles in unicellular organisms or outside the cell in multicellular organisms). In the confined space the biomineralization is controlled by the concentrations of inorganic agents and the interaction with the organic matrix

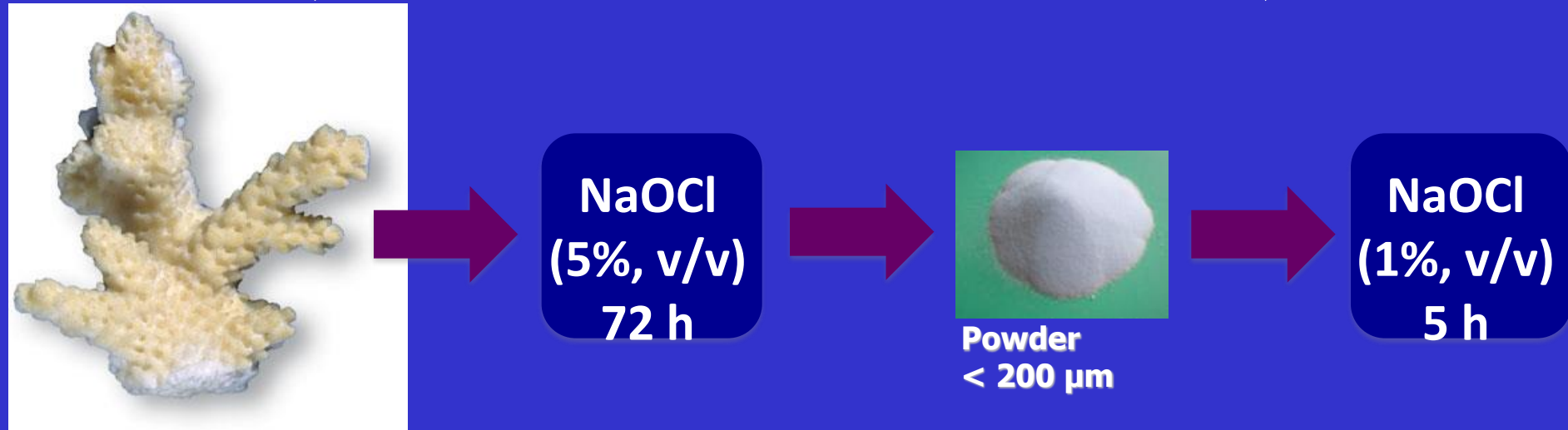




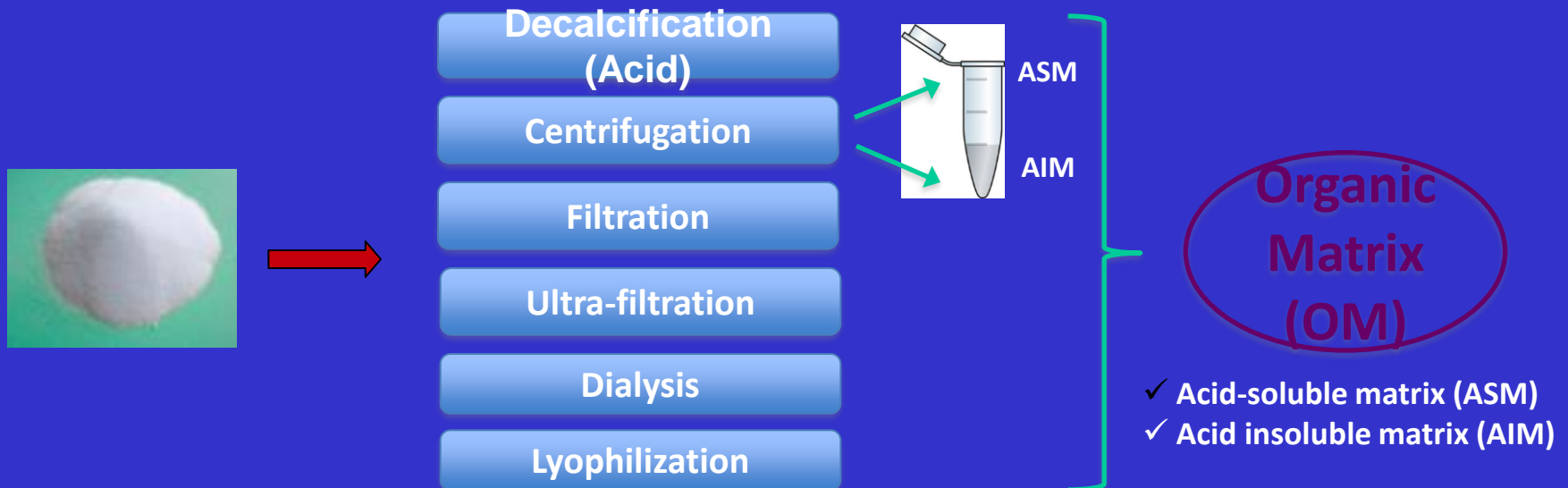
What do *Acropora* skeletal proteins tell us about coral biocalcification ?

- P. Ramos-Silva, F. Marin, J.A. Kaandorp, and B. Marie, PNAS, 3–5. 2013
- P. Ramos-Silva J.A, Kaandorp, L. Huisman, B. Marie, I. Zanella-Cléon, N. Guichard, D.J. Miller and F. Marin, Molecular Biology and Evolution, 2013

# Organic matrix extraction in the scleractinian coral *Acropora millepora* (Ramos-Silva et al., Molec. Biol. Evol., 2013)

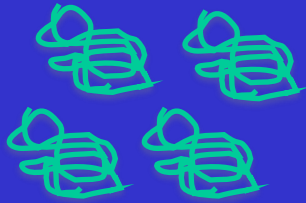


## The organic matrix extraction:

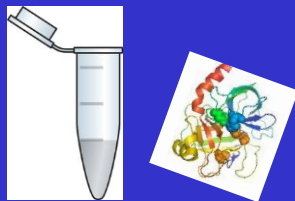


# Mass spectrometry analysis of the Organic matrix

Protein samples:  
ASM  
AIM



Proteins are denatured, reduced and alkylated



Trypsin digestion

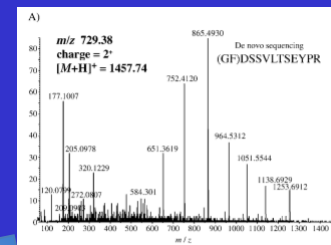


Peptides

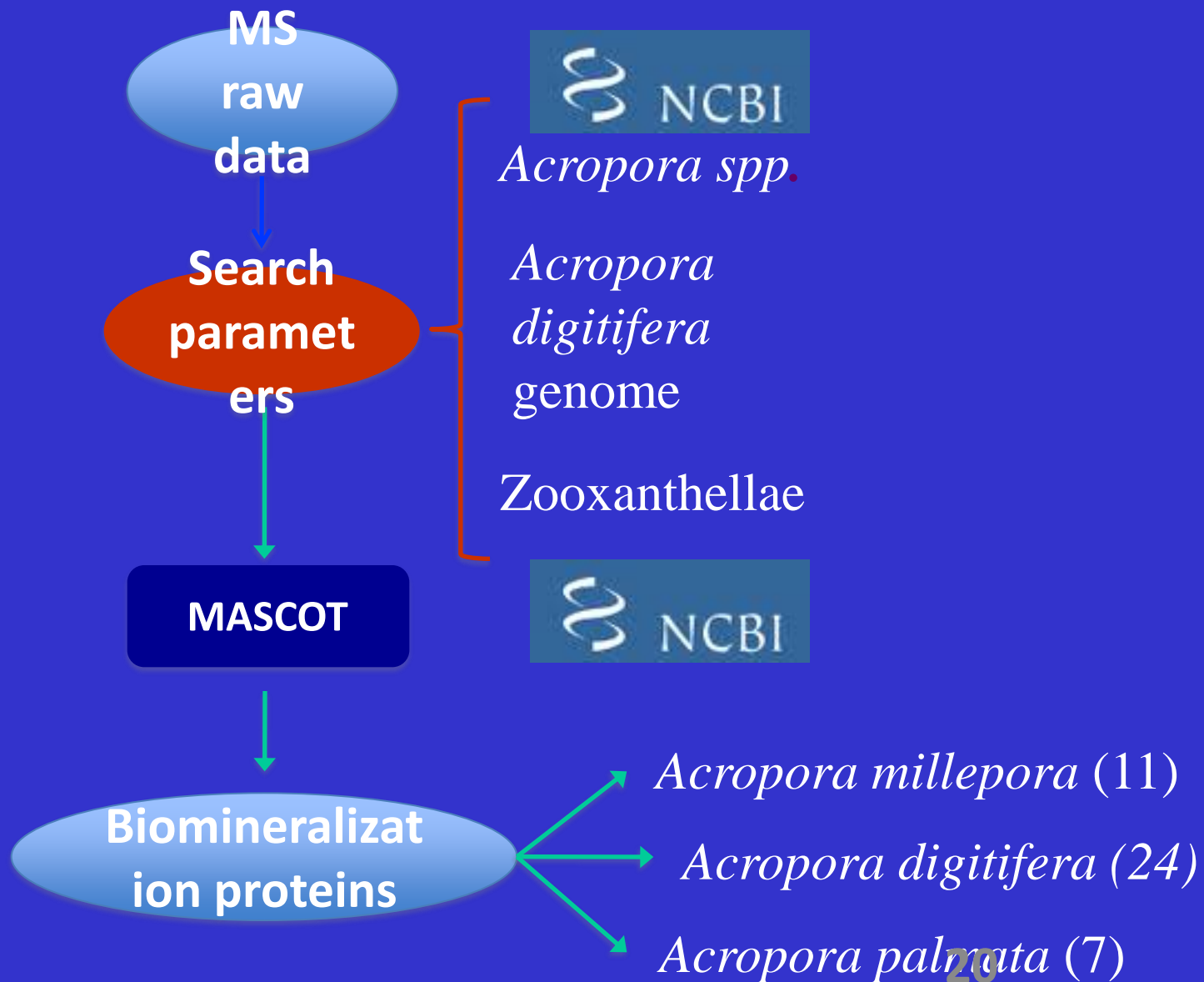


Mass Spectrometry

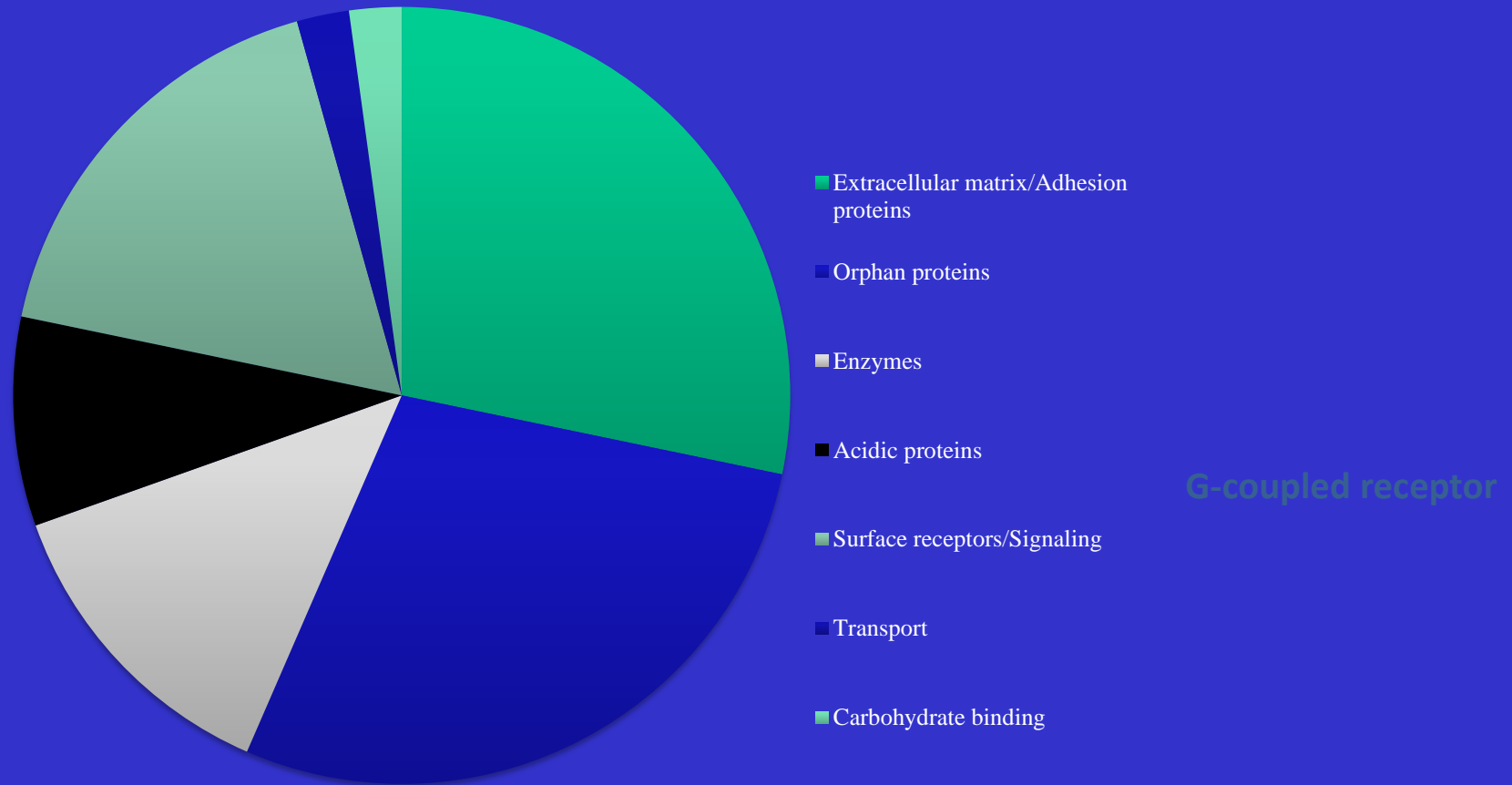
Protein identification

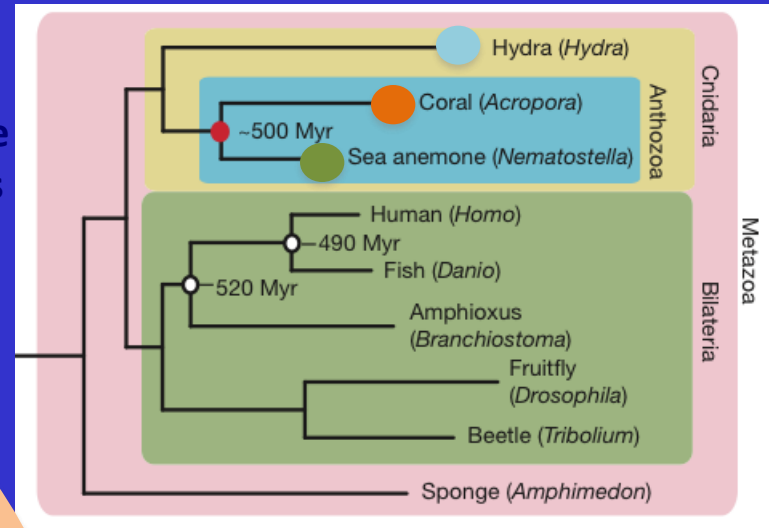
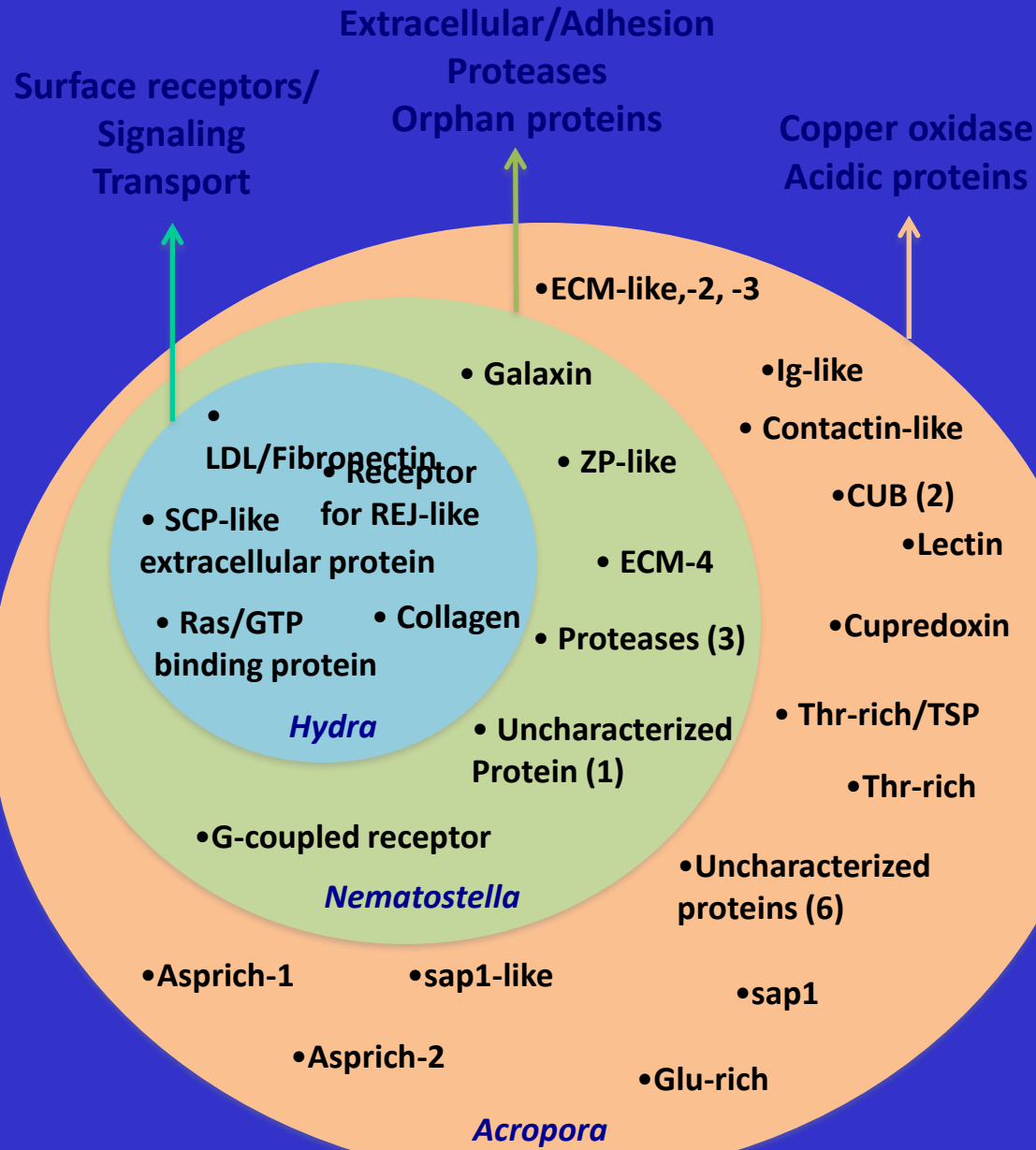


# Protein identification

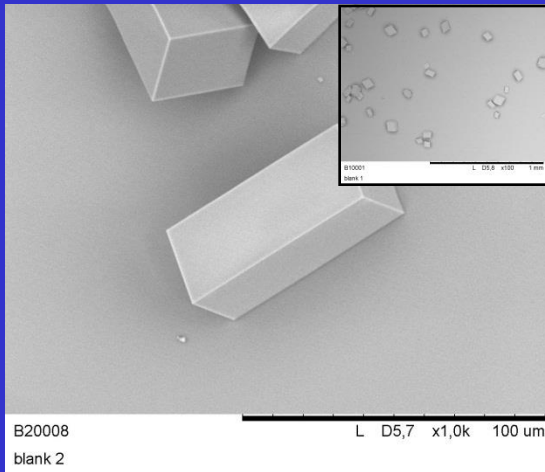


# Protein analysis: distribution of functions from proteins of the Acidic Soluble Matrix

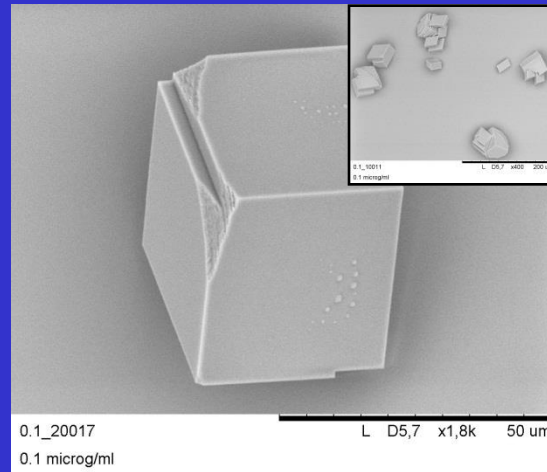




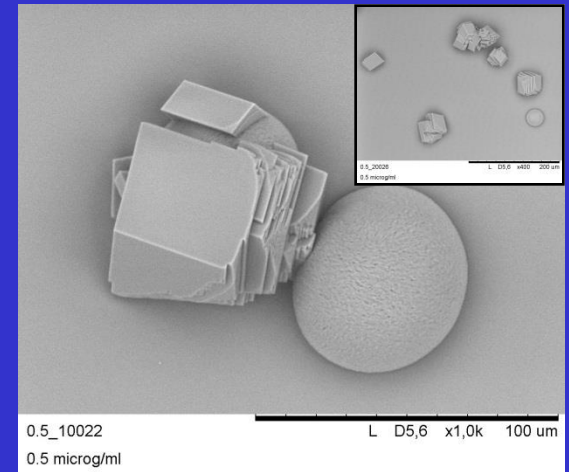
# *In vitro* interaction of Acid Soluble Matrix with $\text{CaCO}_3$ (Ramos-Silva et al., Molec. Biol. Evol., 2013)



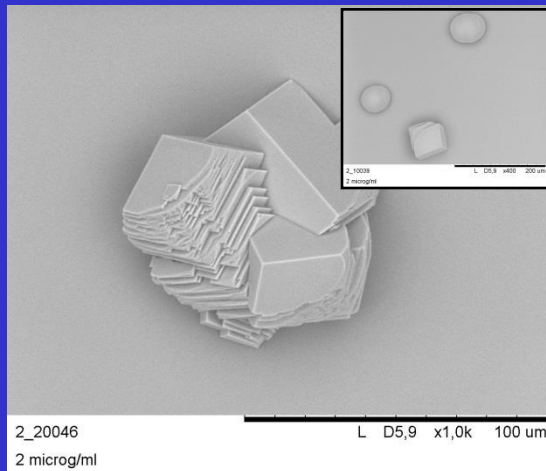
**blank**



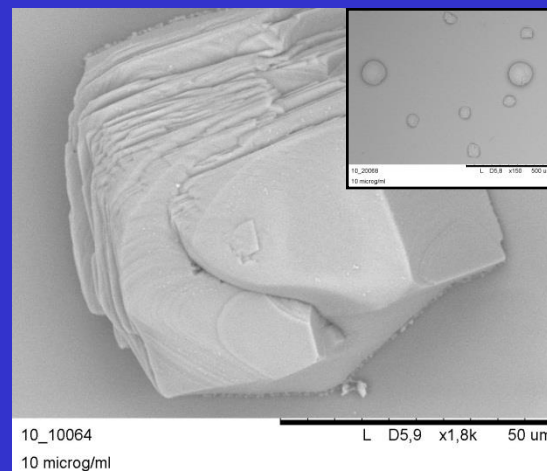
**0.1**



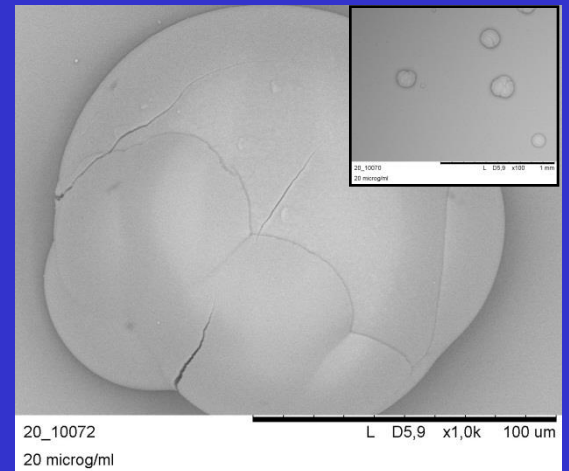
**0.5**



**2.0**



**10**



**20**

# Conclusions

- First attempt to fully characterize the organic matrix of a reef coral using proteomics together with the available genomic resources
- *In vitro* interaction of Acid Soluble Matrix with  $\text{CaCO}_3$  shows that the crystallization process is strongly influenced

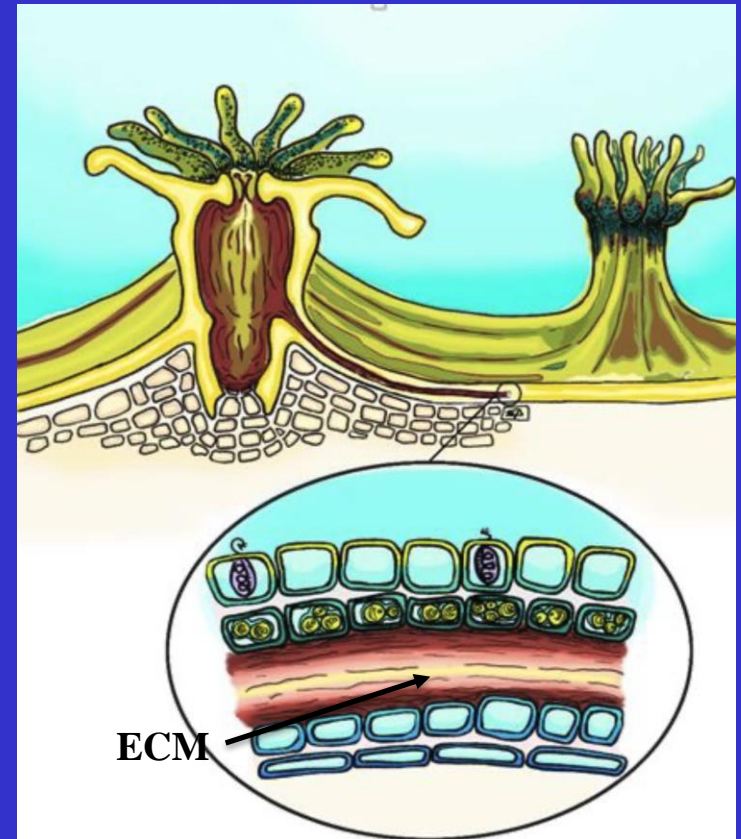


# Modelling calcification physiology in a confined space

- H.F. Willard, E.S. Deutekom, D. Allemand, S. Tambutté, J. A. Kaandorp, Testing hypotheses on the calcification in scleractinian corals using a spatio-temporal model that shows a high degree of robustness, Journal of Theoretical Biology, Volume 561, 21 March 2023

# Coral calcification

- Enhanced Calcifying Medium (ECM)
  - Located between tissue and skeleton
  - Biomineralization
  - Strong biological control
  - High calcification
  - Increased pH and  $\text{Ca}^{2+}$ -concentration
- Light-enhanced calcification (LEC)



# Many hypotheses!

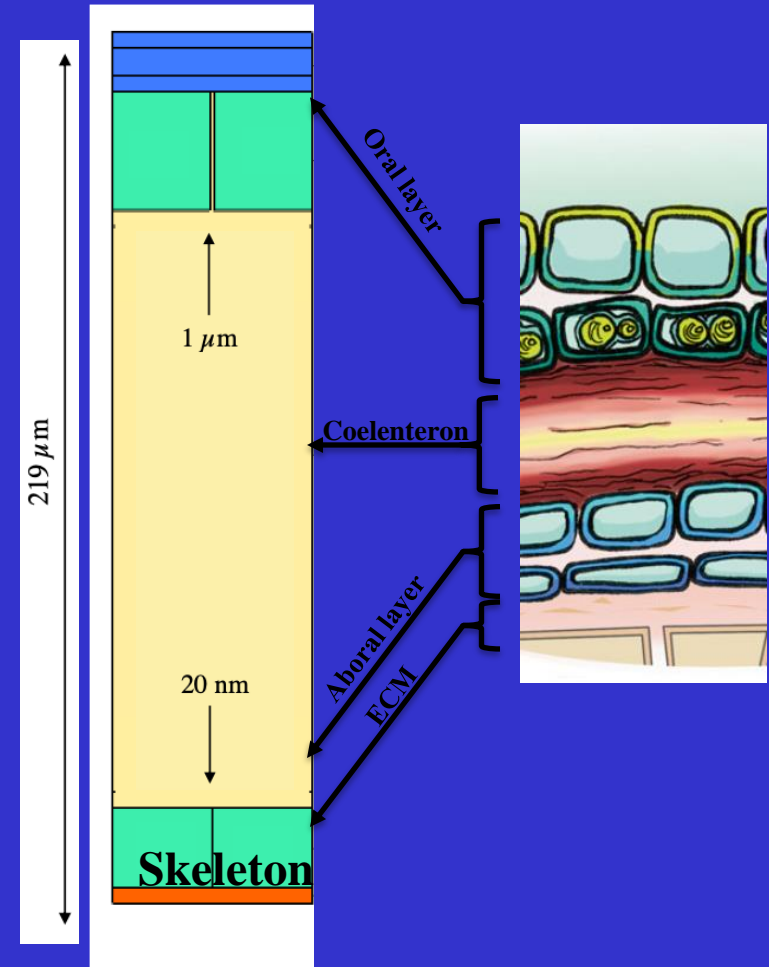
- Hypotheses ion-transport, reviewed by Allemand et al. (2011):
  - Only paracellular (passive) transport
  - Only transcellular (active) transport
  - Combination of paracellular and transcellular transport
- Hypotheses on Light-Enhanced Calcification
  - Modification of the CO<sub>2</sub> -chemistry within coral tissues caused by CO<sub>2</sub> uptake for photosynthesis (Goreau, 1959, McConnaughey and Whelan, 1997)
  - Increased available energy, simulating ion-transport. (Fukuda et al., 2003, Colombo-Pallotta et al., 2010)
  - Stimulation respiration by more available O<sub>2</sub> (Rinkevich and Loya, 1984)
  - Removal of inhibiting substances (Simkiss, 1964)
  - Synthesis by symbionts of organic matrix molecules or precursors (Muscatine and Cernichiari, 1969)
  - Stimulation Ca<sup>2+</sup>-ATPase in light conditions (Al-Horani et al., 2003, Taubner et al., 2019)

# Spatio-temporal modelling

- Modelling technique using both time and space
- Used to test and create hypotheses
- Spatio-temporal experimental data
  - Microscopy in combination with pH-sensitive dye (Venn et al. 2011)
  - Measurements with microsensors (Al-Horani et al. 2003)
  - More spatio-temporal data (e.g. Ca<sup>2+</sup> concentrations)

# Calcification model

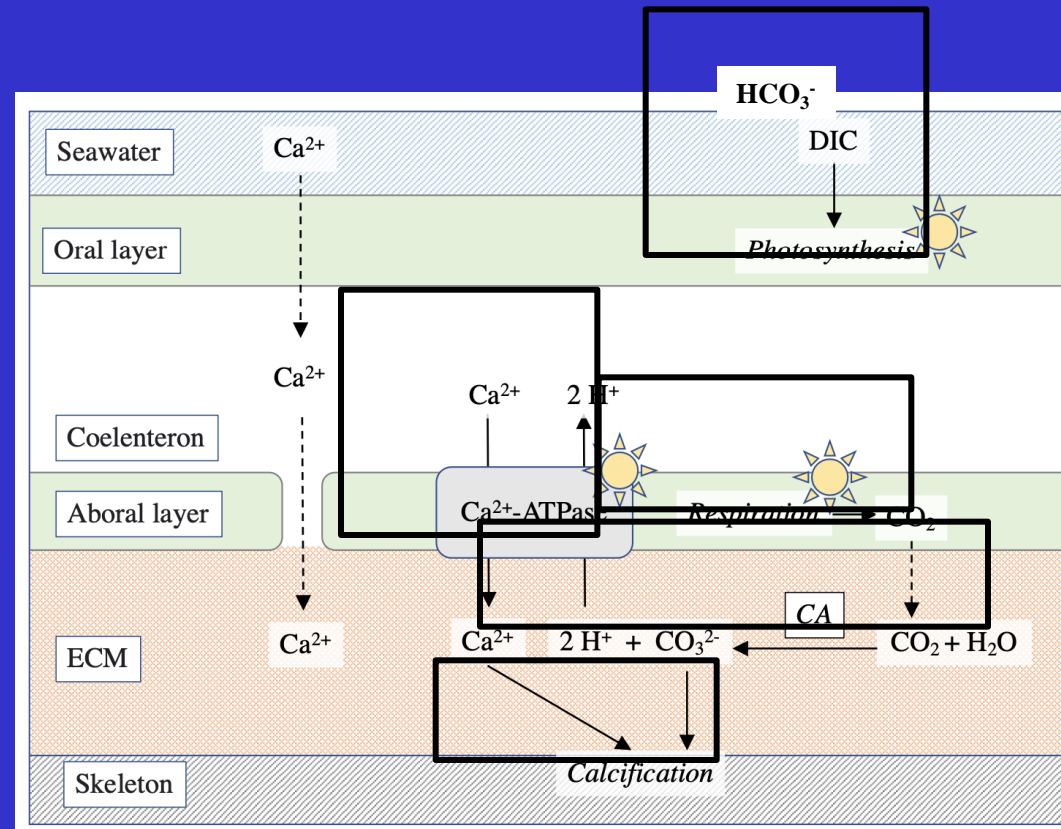
- Topology is as simple as possible!
  - Cell layers are combined
- Reaction-diffusion model:  
CO<sub>2</sub>-chemistry (Zeebe et al. 2001)
  - H<sup>+</sup>/OH<sup>-</sup>
  - CO<sub>2</sub>/HCO<sub>3</sub><sup>-</sup>/CO<sub>3</sub><sup>2-</sup>
  - B(OH)<sub>3</sub>/B(OH)<sub>4</sub><sup>-</sup>
- Only CO<sub>2</sub> diffuses over cell membrane



# Calcification model

- Photosynthesis
- Respiration
- Active ion-transport
- Carbonic Anhydrase (CA)
- Calcification

Light  
dependent  
processes

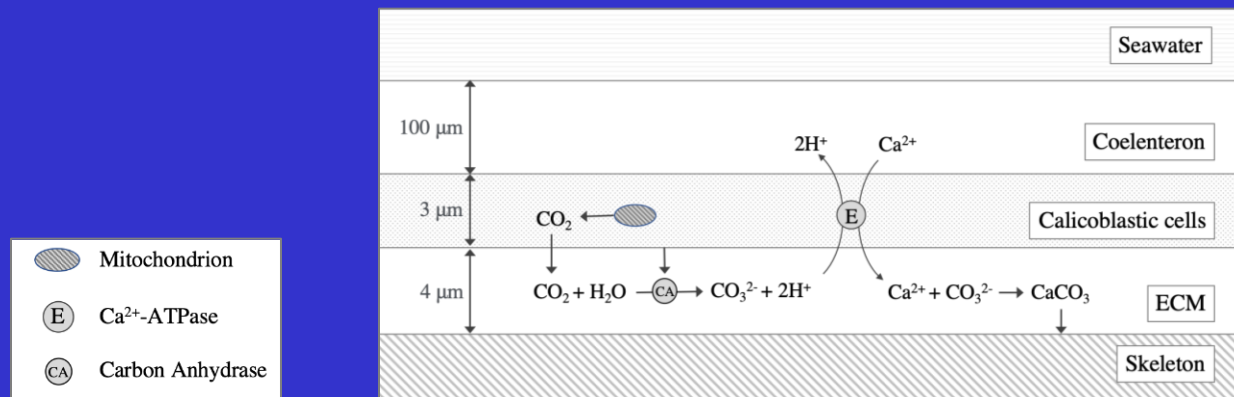


# Modelling approach I

- Spatial model considering chemical processes controlling the chemical composition of the ECM.
- Both diffusion (spatial information) and chemical reactions.
- Can we create a simple spatial model that reproduces data from in vivo measured data (e. g. Al Horani 2003) of the ECM in reef building corals?
- Can we, using this model, gain a better understanding on how the coral keeps the ECM's chemical composition favorable for calcification?
- Can we, using this model, reproduce the light-dark dynamics that are the effect of LEC?

# Modelling approach II

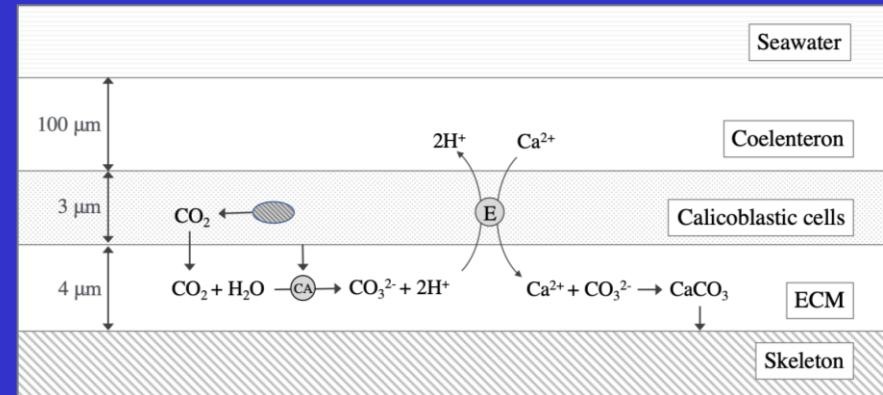
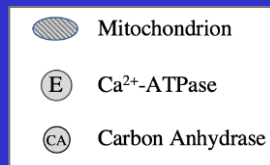
- Spatial Reaction-Diffusion model
  - Including  $\text{CO}_2$ -chemistry based on the system of Zeebe and Gladrow (2001)
- Simple topology
  - Cell membranes only permeable by  $\text{CO}_2$
  - Calcification at skeleton boundary
  - Seawater constant concentrations





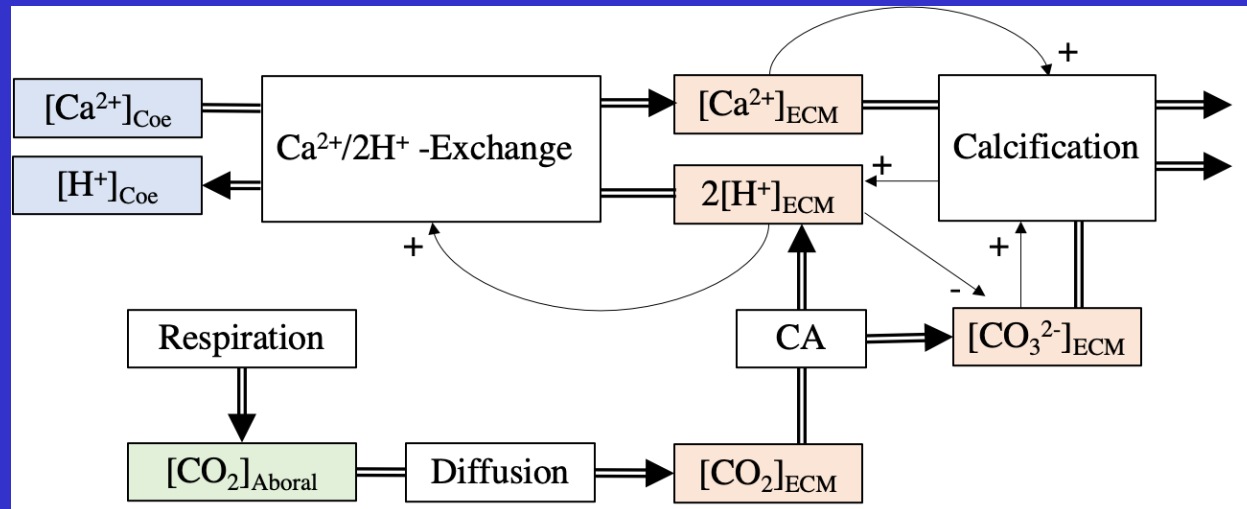
# Modelling approach III

- Chemical composition ECM is controlled by
  - Respiration in Calicoblastic cells
  - Ion transport of  $\text{Ca}^{2+}$ -ATPase
    - Modelled as flux over Calicoblastic cells
    - $$J_{\text{ex}} = J_{\text{ex}}^{\text{max}} \frac{[\text{H}^+]^2 [\text{Ca}^{2+}]_{\text{cell}}}{K_{\text{ex}} + [\text{H}^+]^2 [\text{Ca}^{2+}]_{\text{cell}}}$$
  - Carbonic Anhydrase
    - $$V_{\text{CA}} = E(\text{CA})_{\text{tot}} k_{\text{cat}} \frac{[\text{CO}_2]}{K_{\text{CA}} + [\text{CO}_2]}$$



# Modelling approach IV

- System reaches steady state
  - Flux of  $\text{Ca}^{2+}$ -ATPase equals calcification rate
  - $\text{CO}_2$  – diffusion equals calcification rate



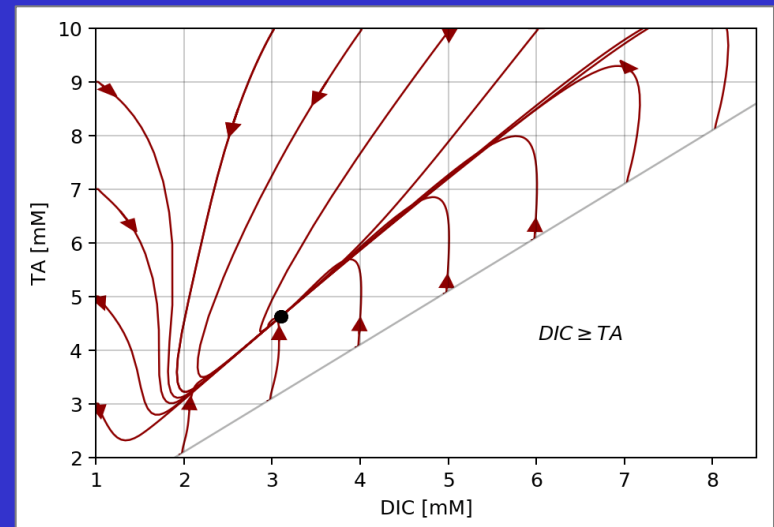
# Modelling approach V

- We assume that, for every biologically relevant set of parameters, there exists at least one *stable* equilibrium point for which the concentrations in the ECM are constant. The latter also for biologically relevant ranges.
- The *chemical concentrations* corresponding to this equilibrium point are assumed to be controlled by the Calicoblastic cells.
- By understanding how this stable point is controlled, we might be able to simulate *the light-dark dynamics* as observed by, among others, Al-Horani (2003).

# Steady state of the model

- System shows one stable point
  - $\{DIC^*, TA^*\} = \{3.1 \text{ mM}, 4.6 \text{ mM}\}$ 
    - These values correspond with literature<sub>10 14</sub>
  - $\Omega^* = 24.1$
- Stable points seems global
  - not formally proven
- Steady state is analyzed by changing
  - $J_{ex}^{max}$
  - $R_{resp}$
  - $E(CA)_{tot}$

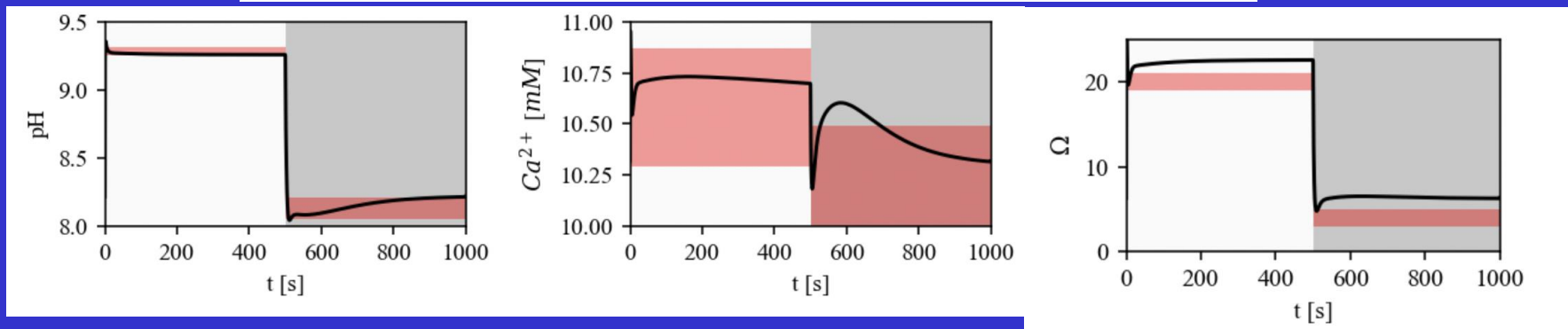
$$\begin{aligned} E(CA)_{tot} &= 0.05 \mu\text{mol} \\ J_{max}^{ex} &= 10 \mu\text{mol}(\text{m}^2 \cdot \text{s}) \\ R_{resp} &= 2 \text{ mM/s} \end{aligned}$$



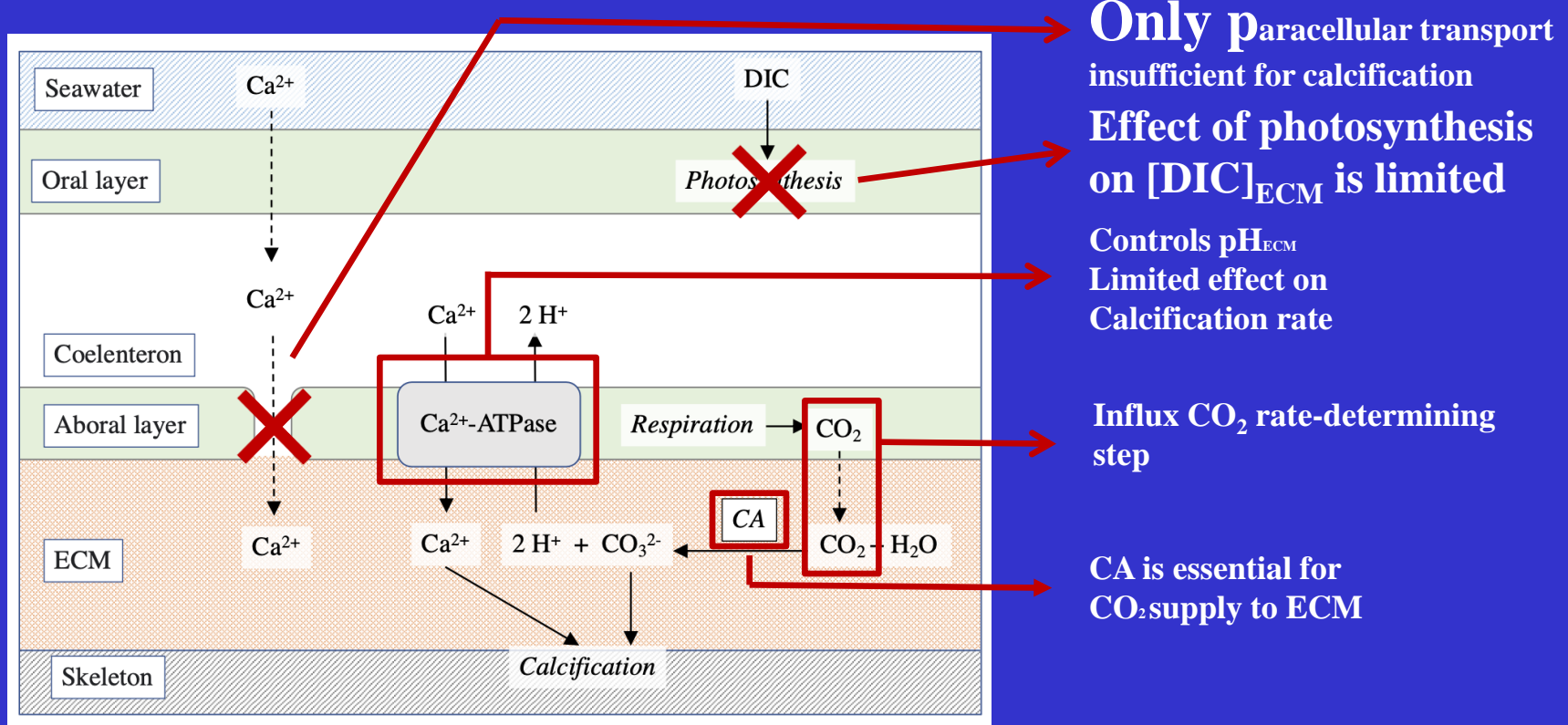
# Calcification model results

- Model (solid black line) can reproduce experimental data (red areas) (Al-Horani et al. 2003) for light and dark (grey shade) conditions
- Model is robust, essential for biological models (Kitano et al. 2002)

Variables in ECM



# Testing hypotheses using calcification model



# Conclusions

- The effect of paracellular transport was limited in the model. Only paracellular transport does not sufficiently supply ions to the ECM for calcification.
- Carbonic Anhydrase is essential for the CO<sub>2</sub>-supply into the model's ECM.
- Light-enhanced calcification was the result of two processes: more available respirational CO<sub>2</sub> and increased activity of Ca<sup>2+</sup>-ATPase.

# Morphological plasticity in scleractinian corals: examples



# The scleractinian coral *Montastrea annularis*

1m



22m



25m

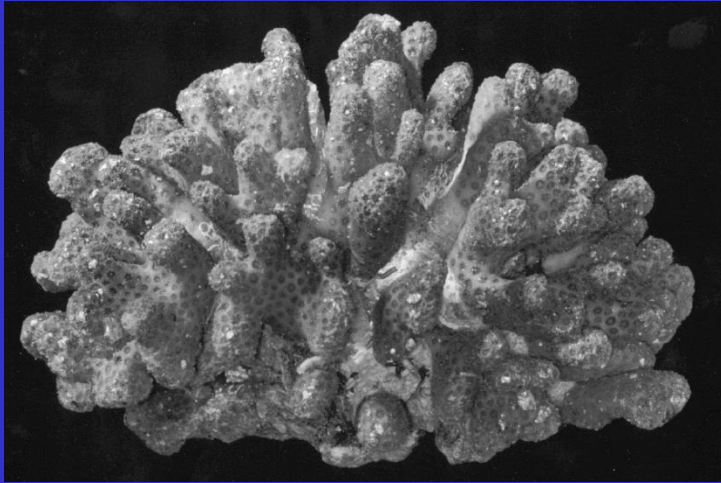


30m

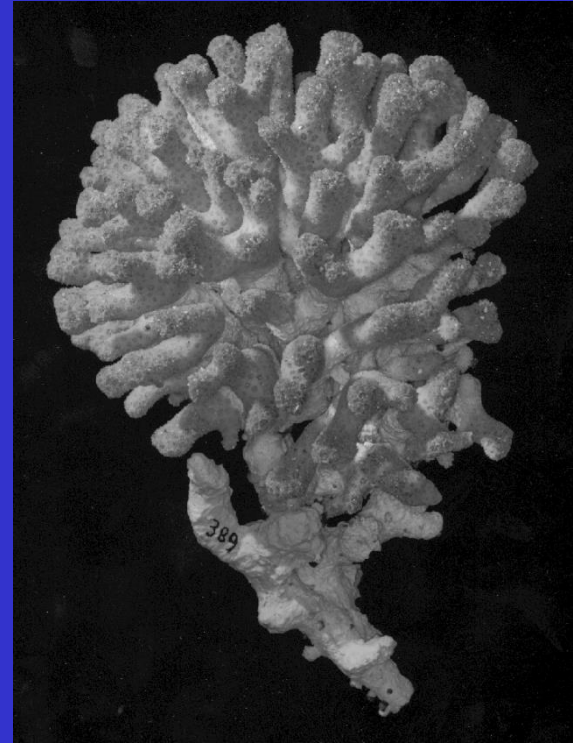


# The stony coral *Madracis mirabilis*

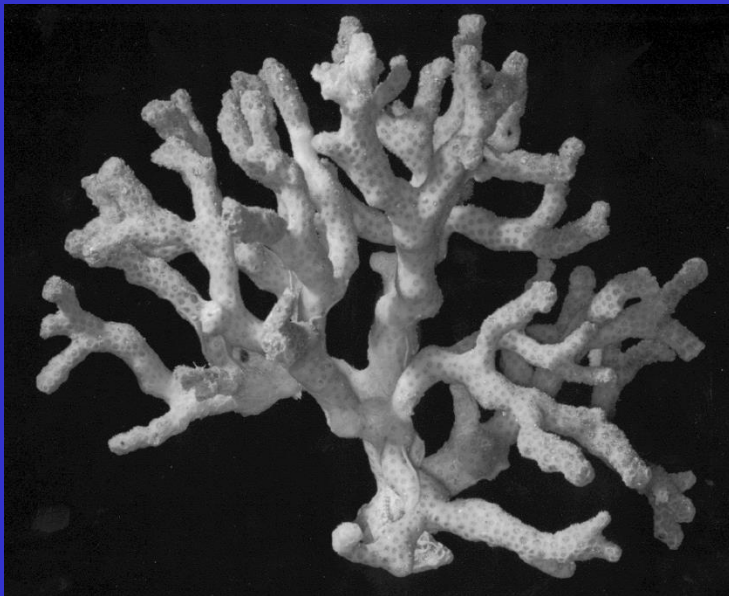
6m



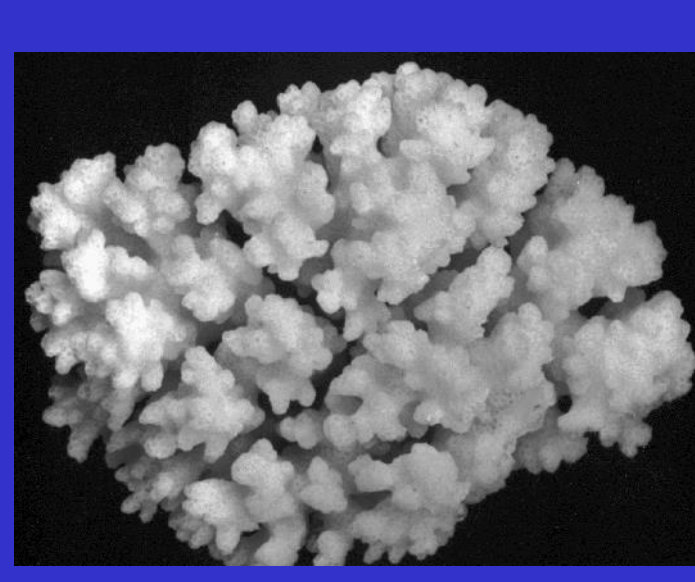
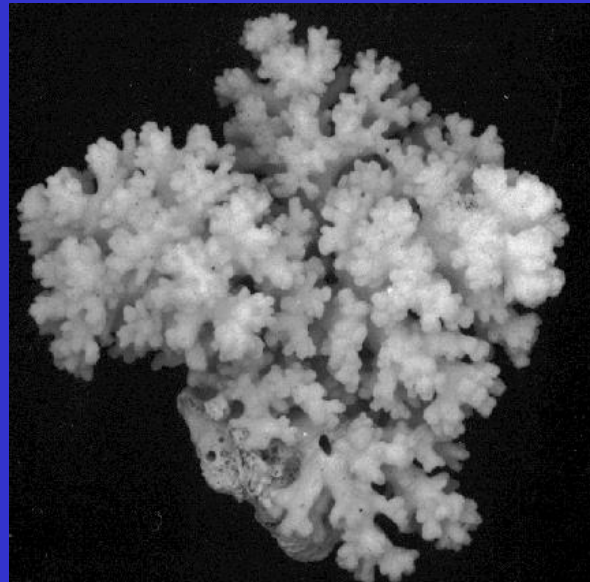
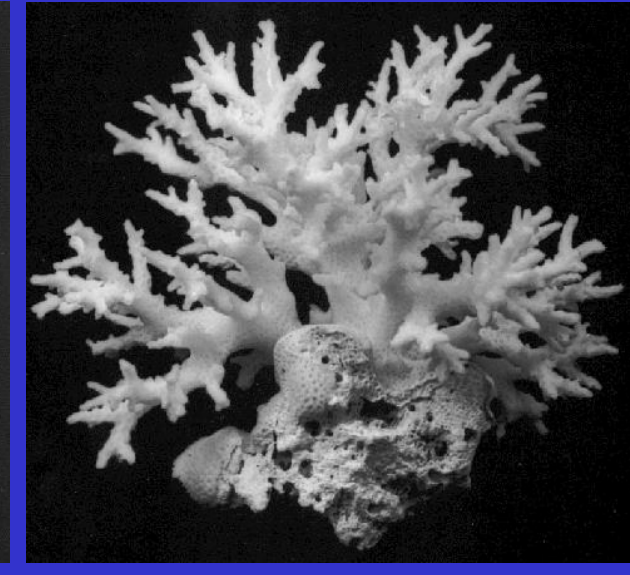
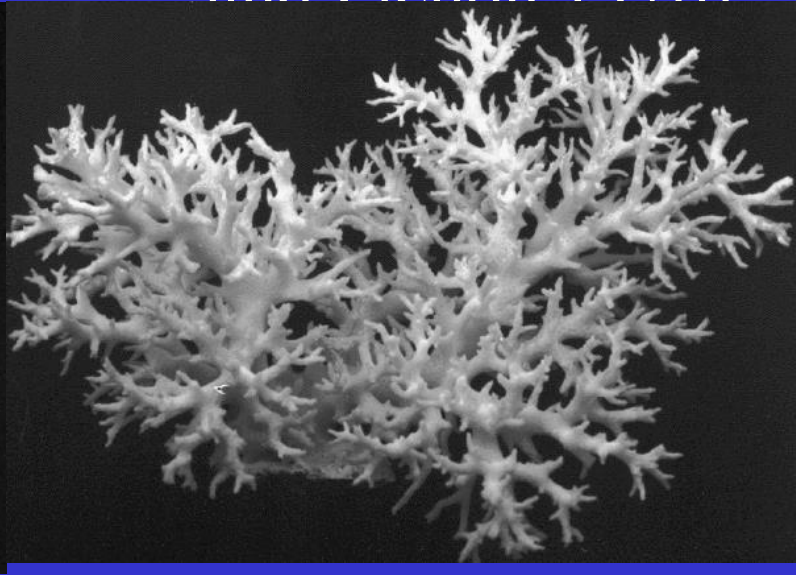
15m



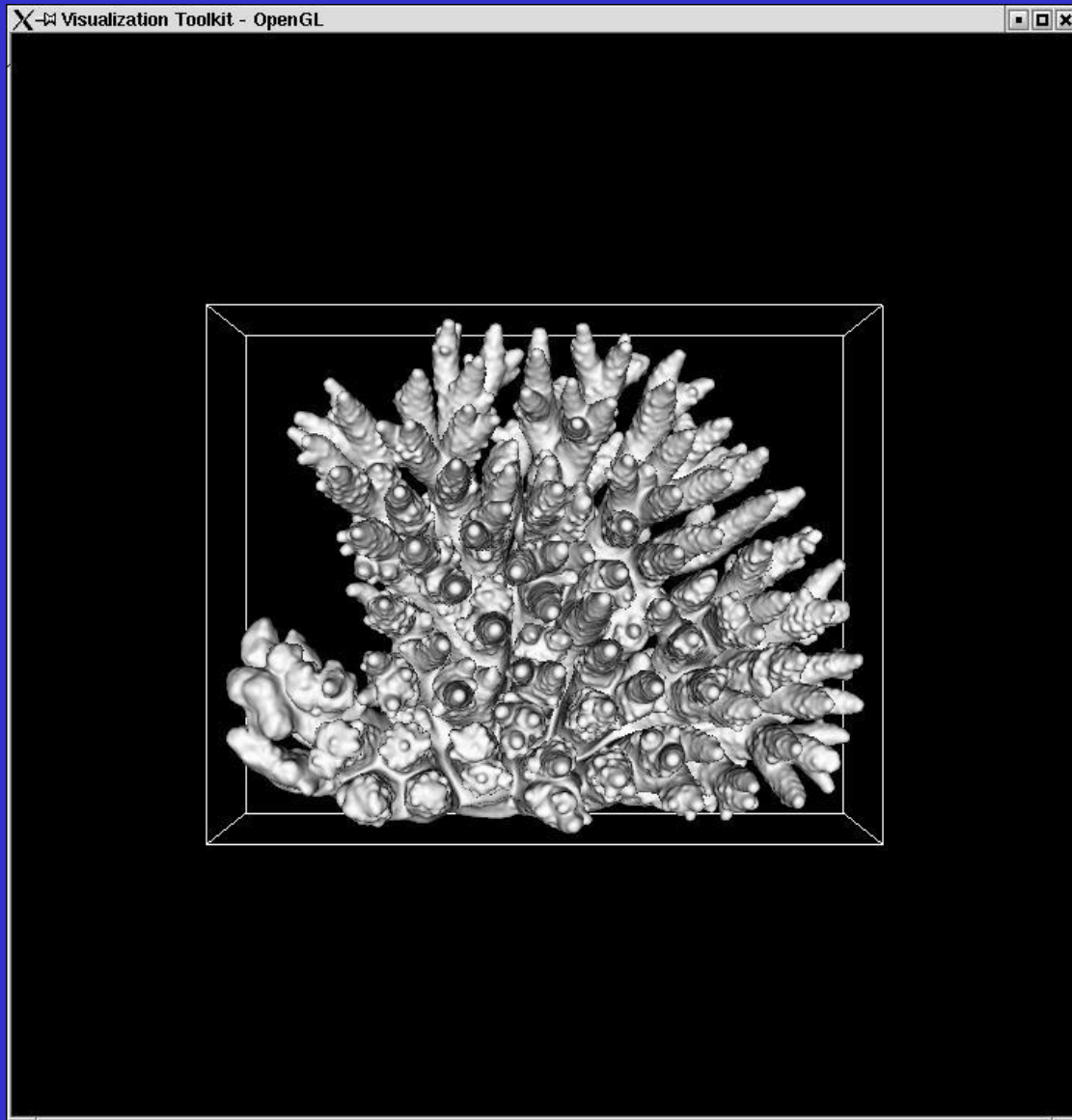
20m



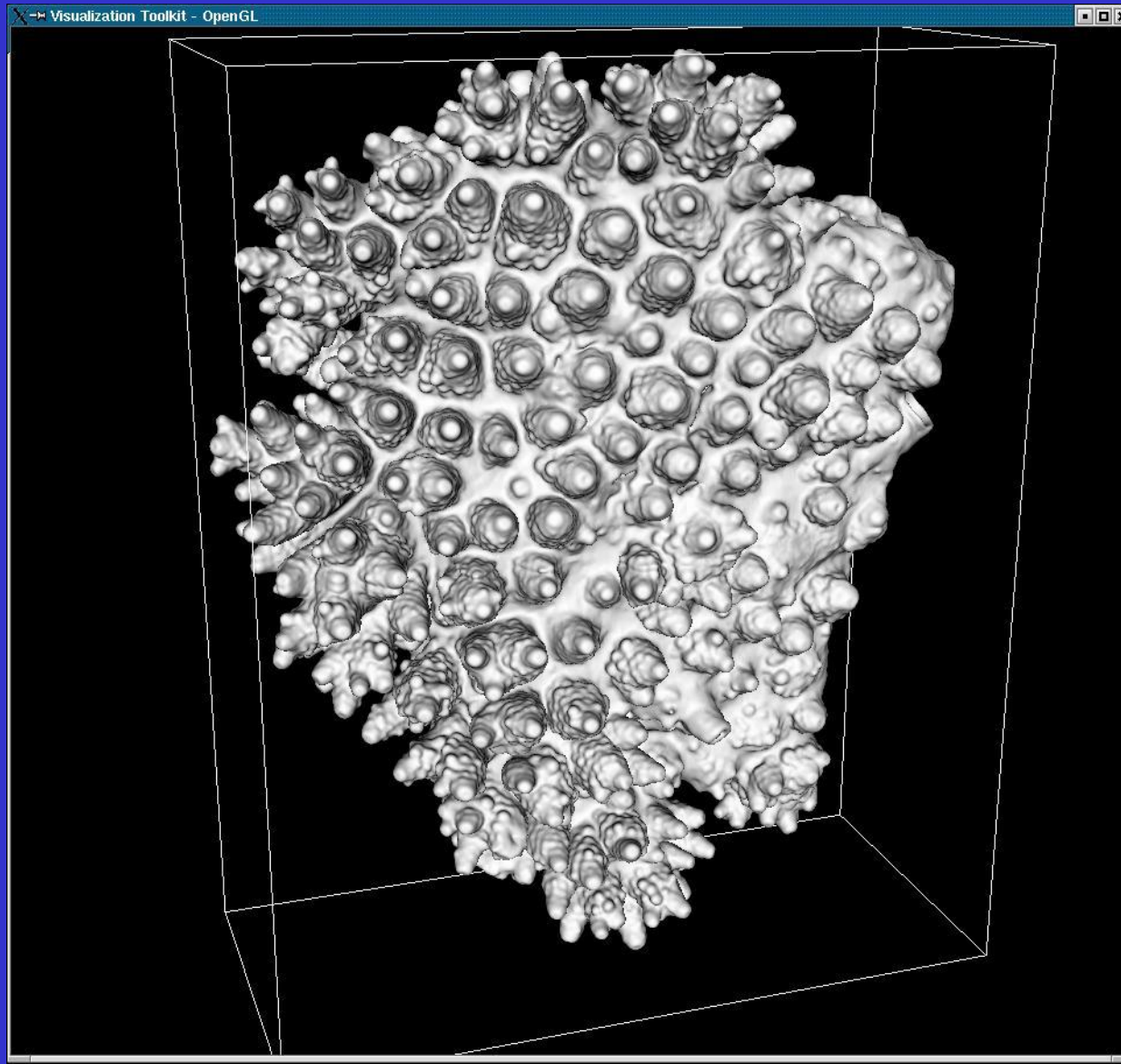
The stony coral *Pocillopora damicornis*; a range from very sheltered – very exposed (top left to right bottom) (after Veron and Pichon 1976)



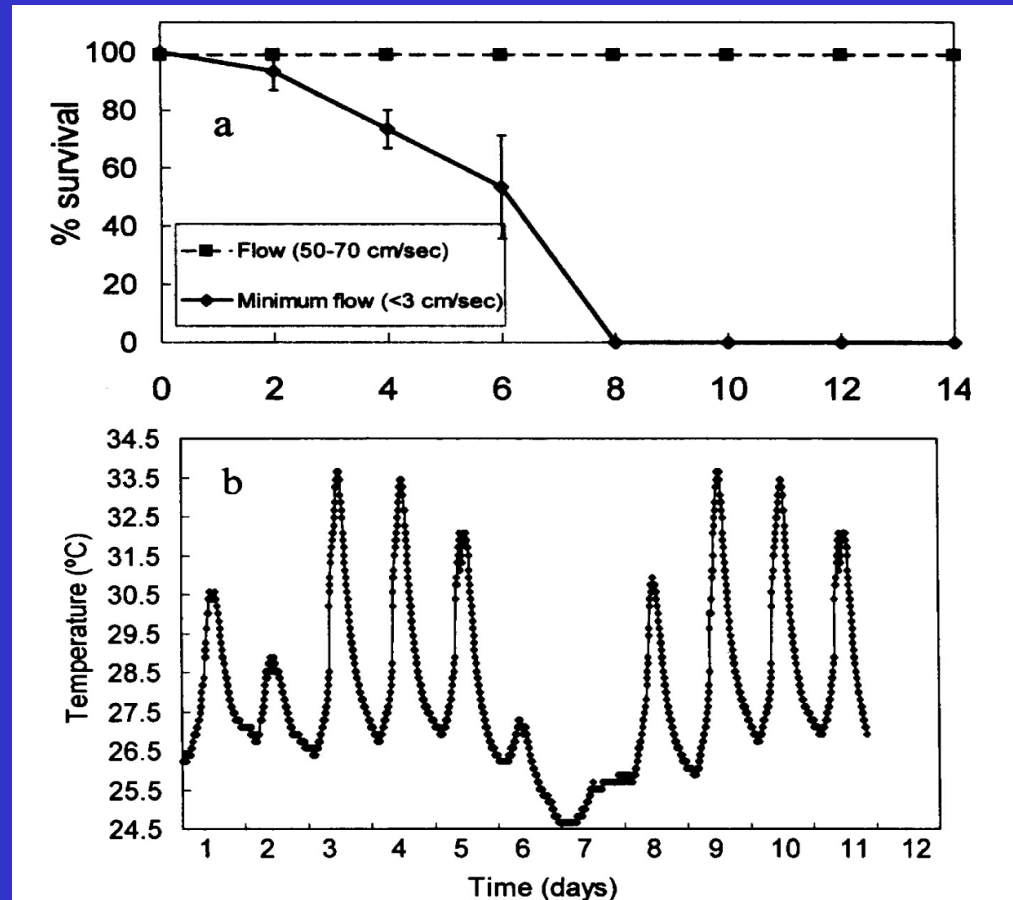
# *Acropora digitifera* low flow morphology



# *Acropora digitifera* high flow morphology



# Survival of *Acropora digitifera* for high and low flow velocities (Nakamura & van Woeseik, 2001)



**Figure 2.** Percent survival (a) of *Acropora digitifera* at elevated temperatures (b) while maintained under high (50-70 cm/sec) and low (<3 cm/sec) flow (Nakamura & Van Woeseik 2001).

Symmetry in the colony shape of  
the scleractinian coral  
*Pocillopora verrucosa*  
(experiment by Mass & Genin,  
2008)

# Symmetry of colony shape

- Is morphological plasticity in corals genetically controlled or influenced by external factors? Growth of the coral *Pocillopora verrucosa* under the influence of *uni-directional* current.

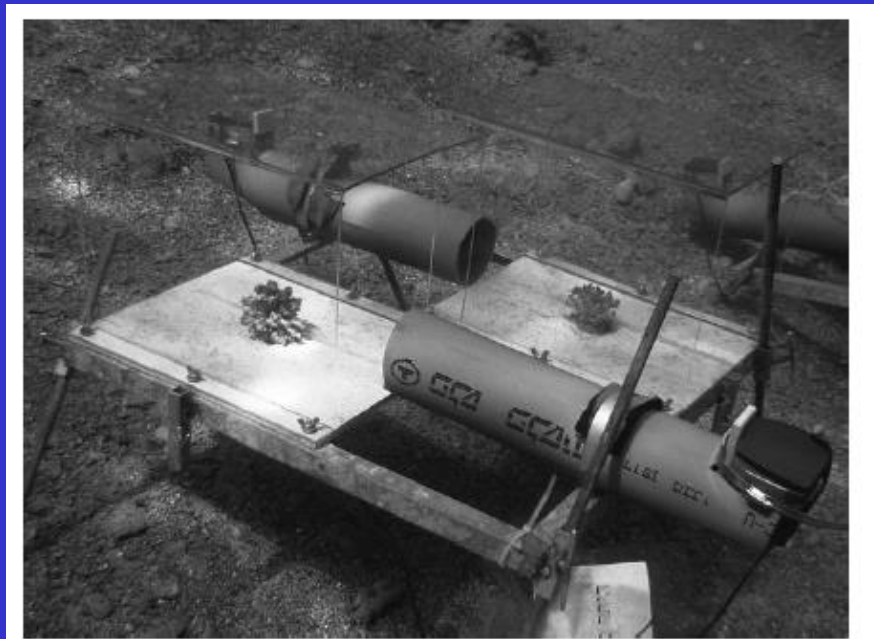


Fig. 1. Underwater setup of flow-manipulation experiment showing 2 units each consisting of a transparent, upside down U-shape box (40 × 40 × 30 cm) and a pump attached to a 50 cm long, 10.1 cm diameter pipe directed at the coral

Mass et al., 2010

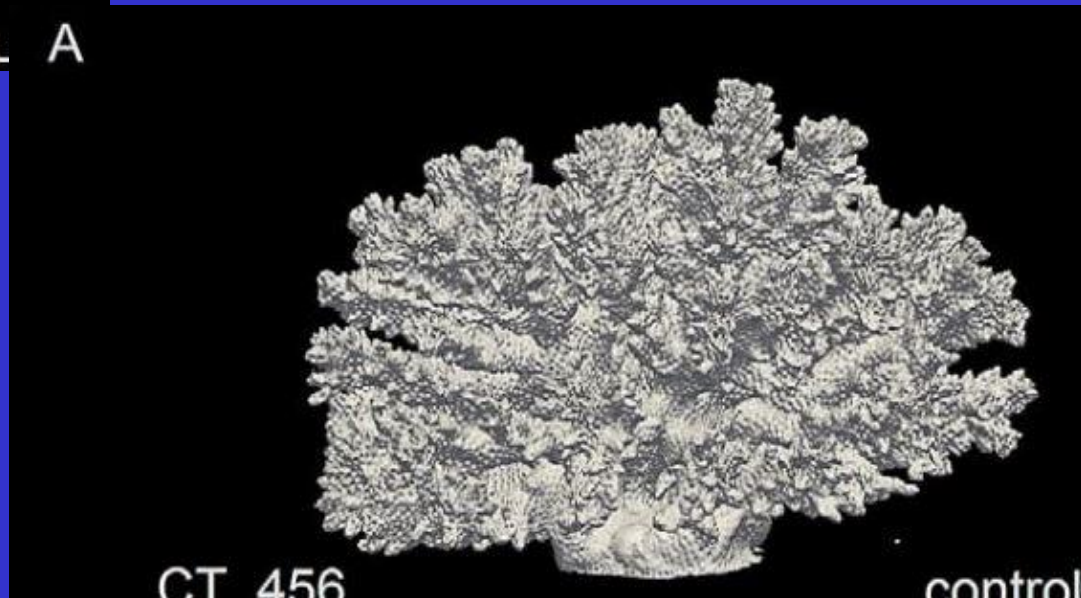


# Symmetry in *Pocillopora verrucosa* (experiment by Mass & Genin 2008)



A-symmetrical form (uni-directional flow)

Symmetrical form



# Research Questions

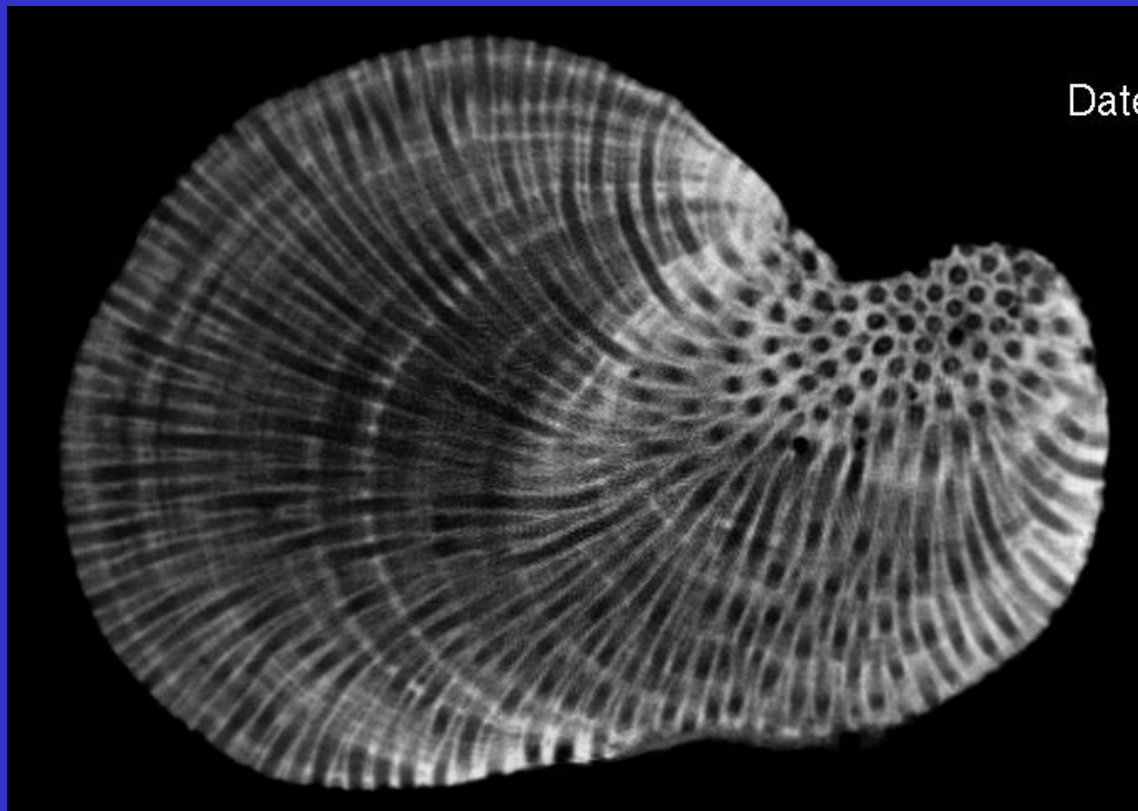
- ▶ **Research question 1:** Is the symmetry found in coral colony determined by symmetry in the flow rather than intrinsic control by the coral?
- ▶ **(Additional) Research question 2:** Is a local increase of O<sub>2</sub> concentrations produced by photosynthesis the cause of bleaching under low flow conditions?



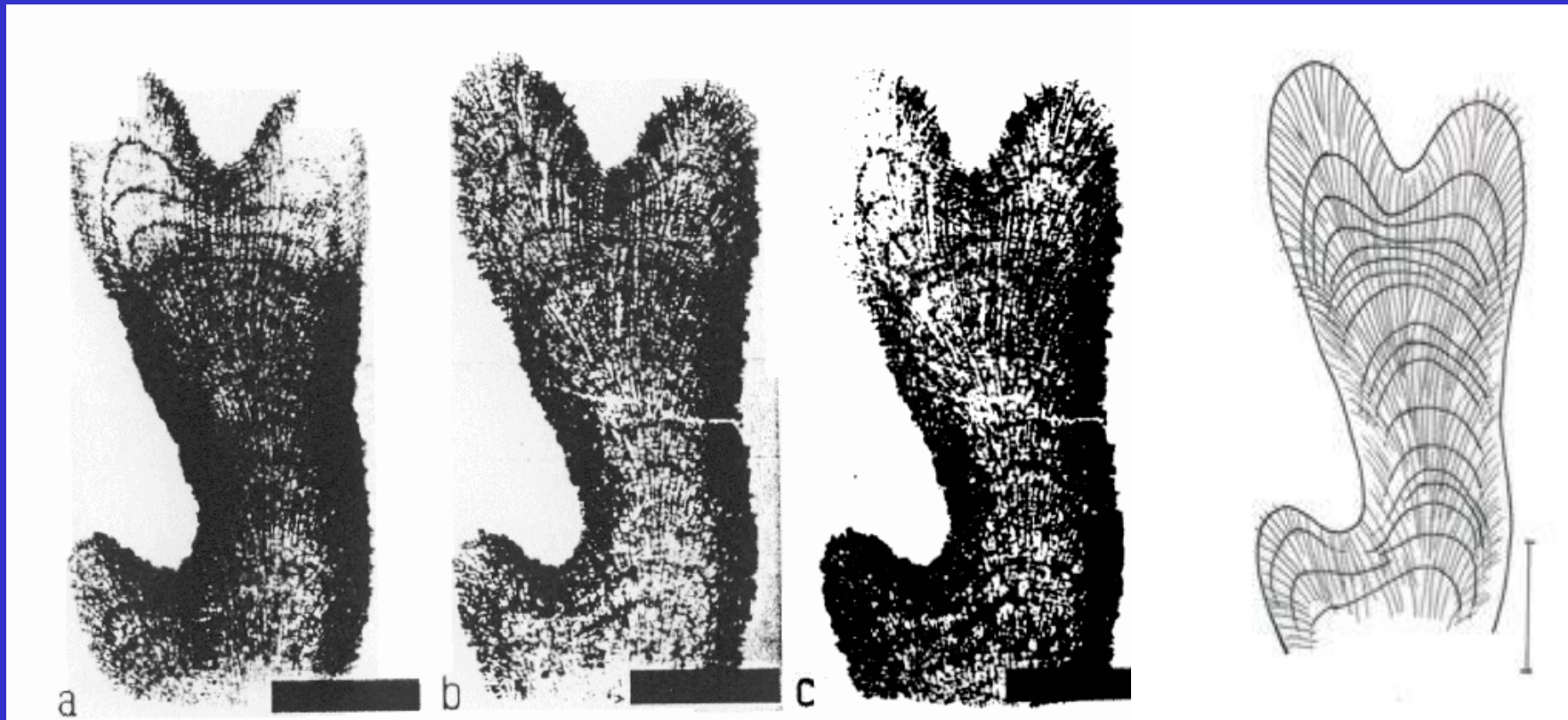
CT scan *Pocillopora verrucosa* (from experiment by Mass & Genin 2008)

Radiate accretive growth in  
scleractinian corals and sponges:  
growth layers and surface structure  
of a growth layer

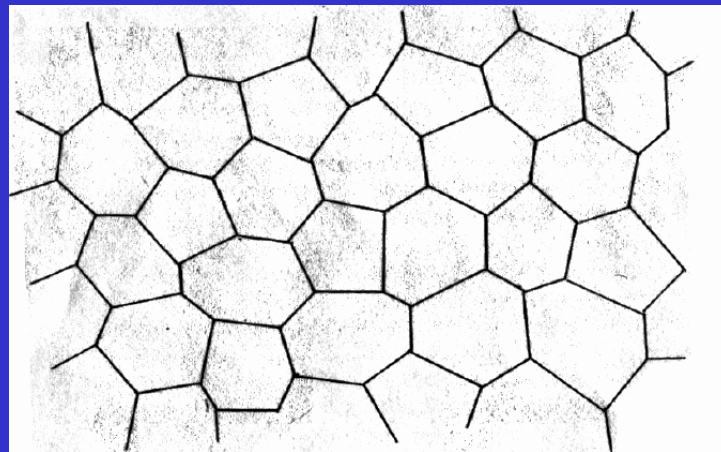
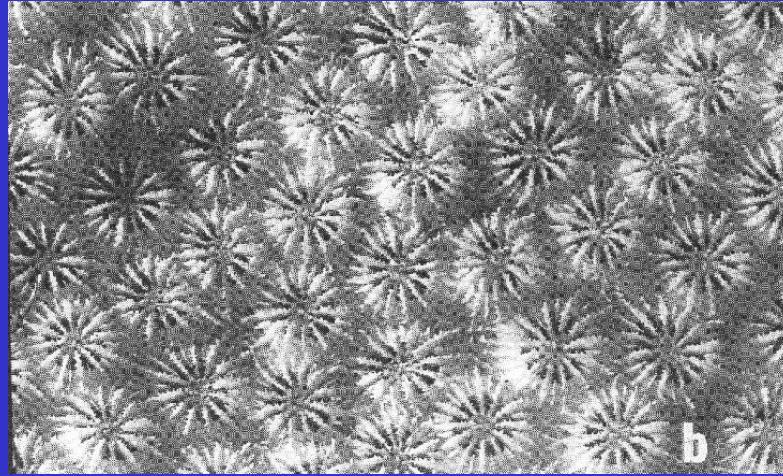
# Growth layers in 3D images of corals (*Montastrea annularis*)



# Radiographs of slices through the scleractinian *Porites porites* (after Tissier et al., 1994)



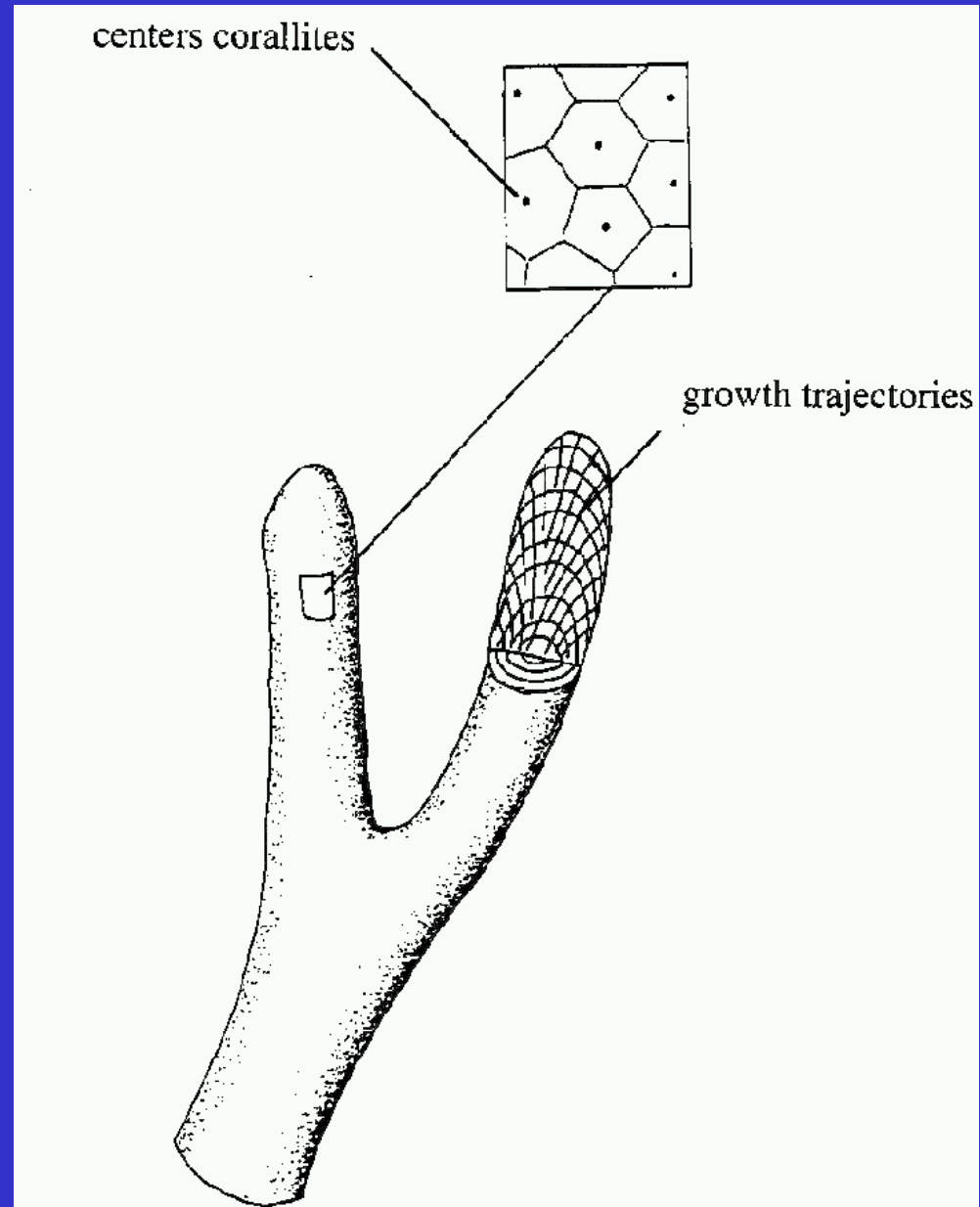
# Surface view of the scleractinian *Montastrea annularis*



Modelling the influence of the  
physical environment (diffusion,  
light, hydrodynamics) on  
calcification

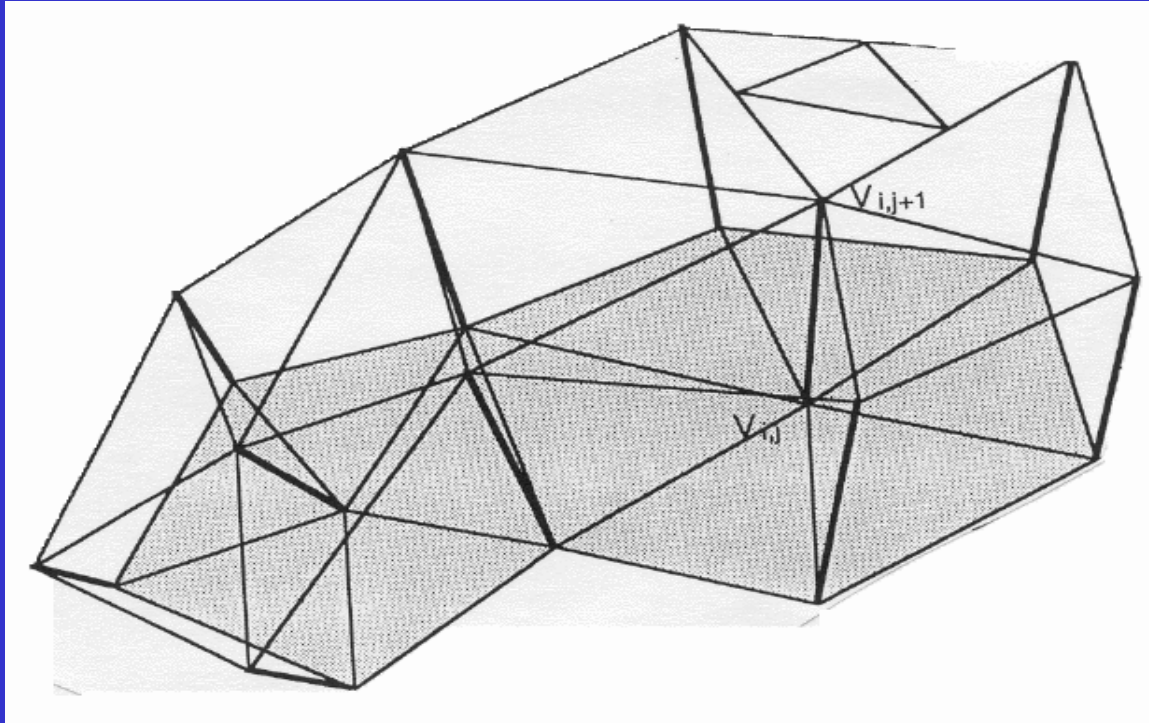
# Central concept of accretive growth

- Layers of material are deposited on top of the previous ones. The previous layers remain unchanged
- The local thickness of a new growth layer is determined by the local absorption of nutrients / local light intensity along the surface normal vector



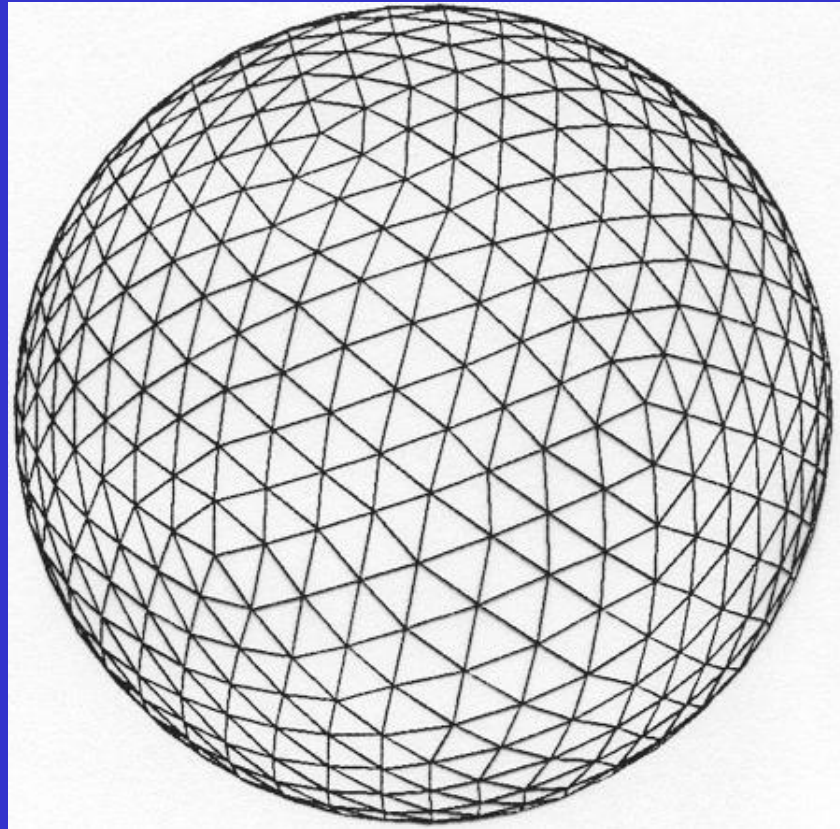


# Simulation of radiate accretive growth:



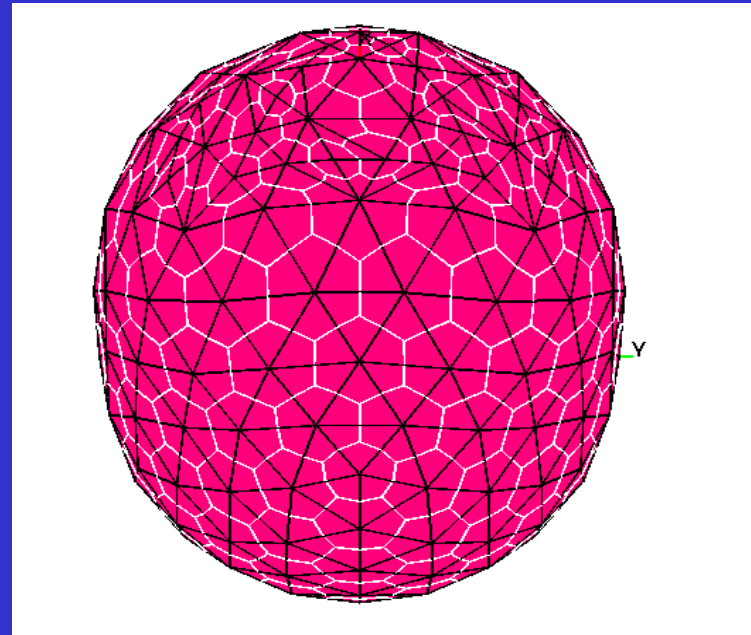
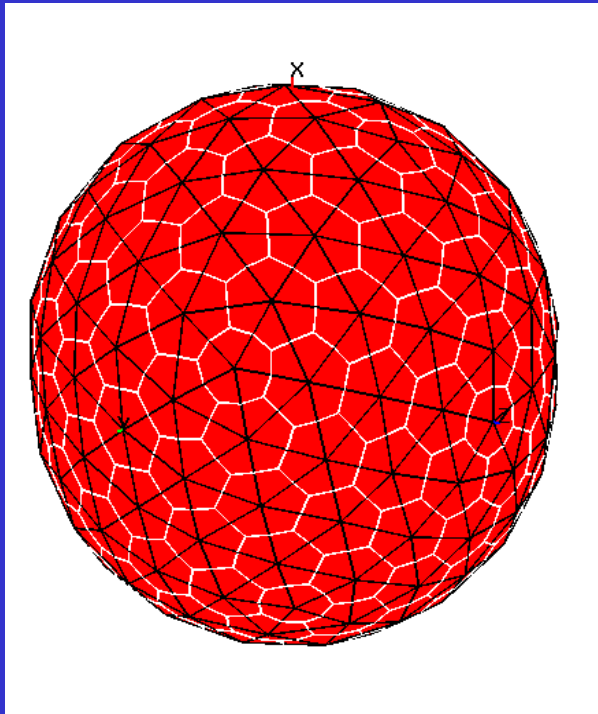
1. a new layer of triangles is constructed on top of a previous one
2. The previous deposited layers remain unchanged
3. the triangles are organized in polygons
4. The thickness  $l$  of a new layer is determined by the local amount of absorption of nutrient / light along the mean surface normal vector

# Accretive growth: initial object



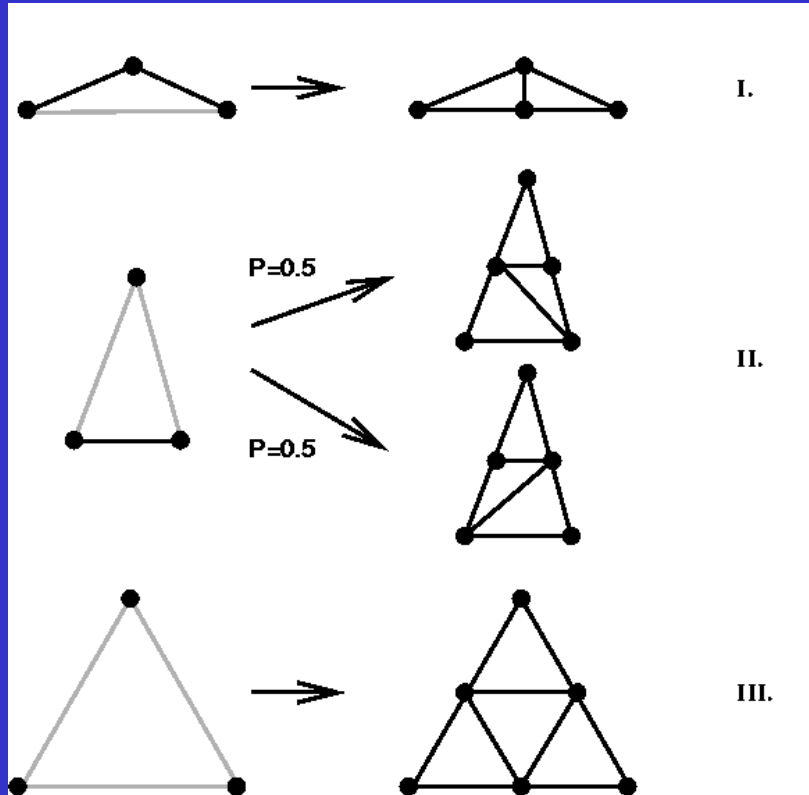
# Insertion/fusion rules

## Two subsequent meshes

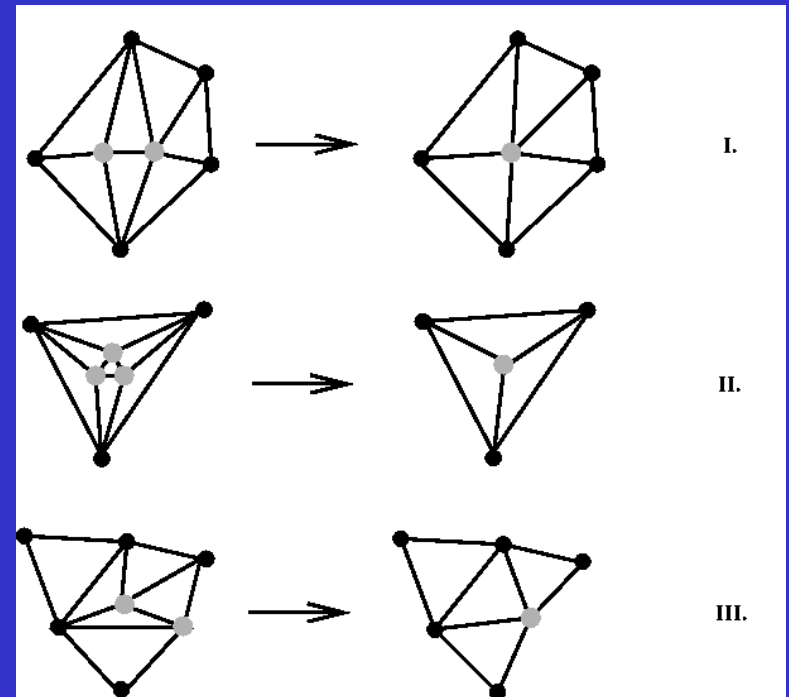


# Insertion and fusion rules

## Consequences for triangle mesh

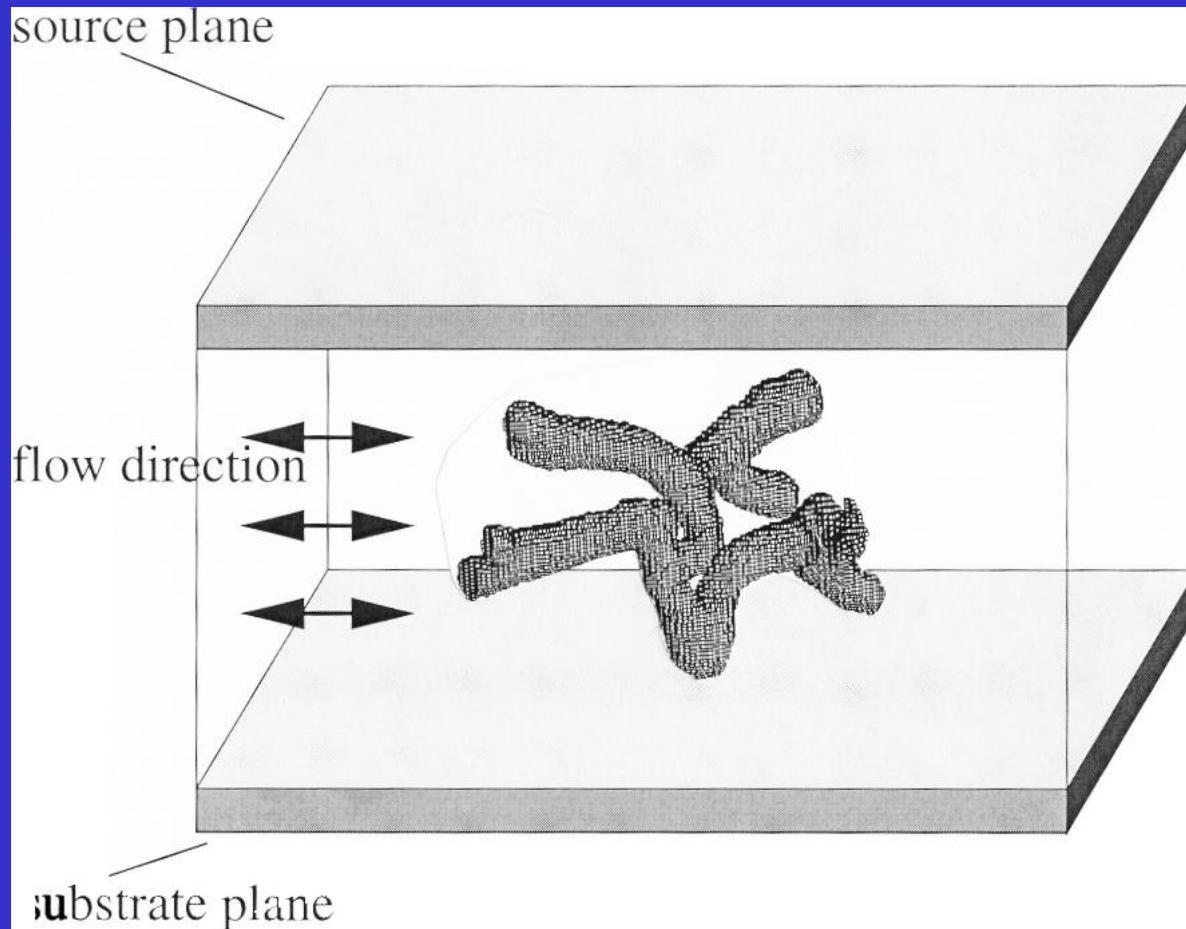


insertion



fusion

# Coupling accretive growth model and diffusion / light model



# Modelling diffusion-limited growth

$$\frac{dc}{dt} = \mathcal{D} \nabla^2 c$$

where  $c$  is the concentration,  $t$  time and  $\mathcal{D}$  the diffusion coefficient.

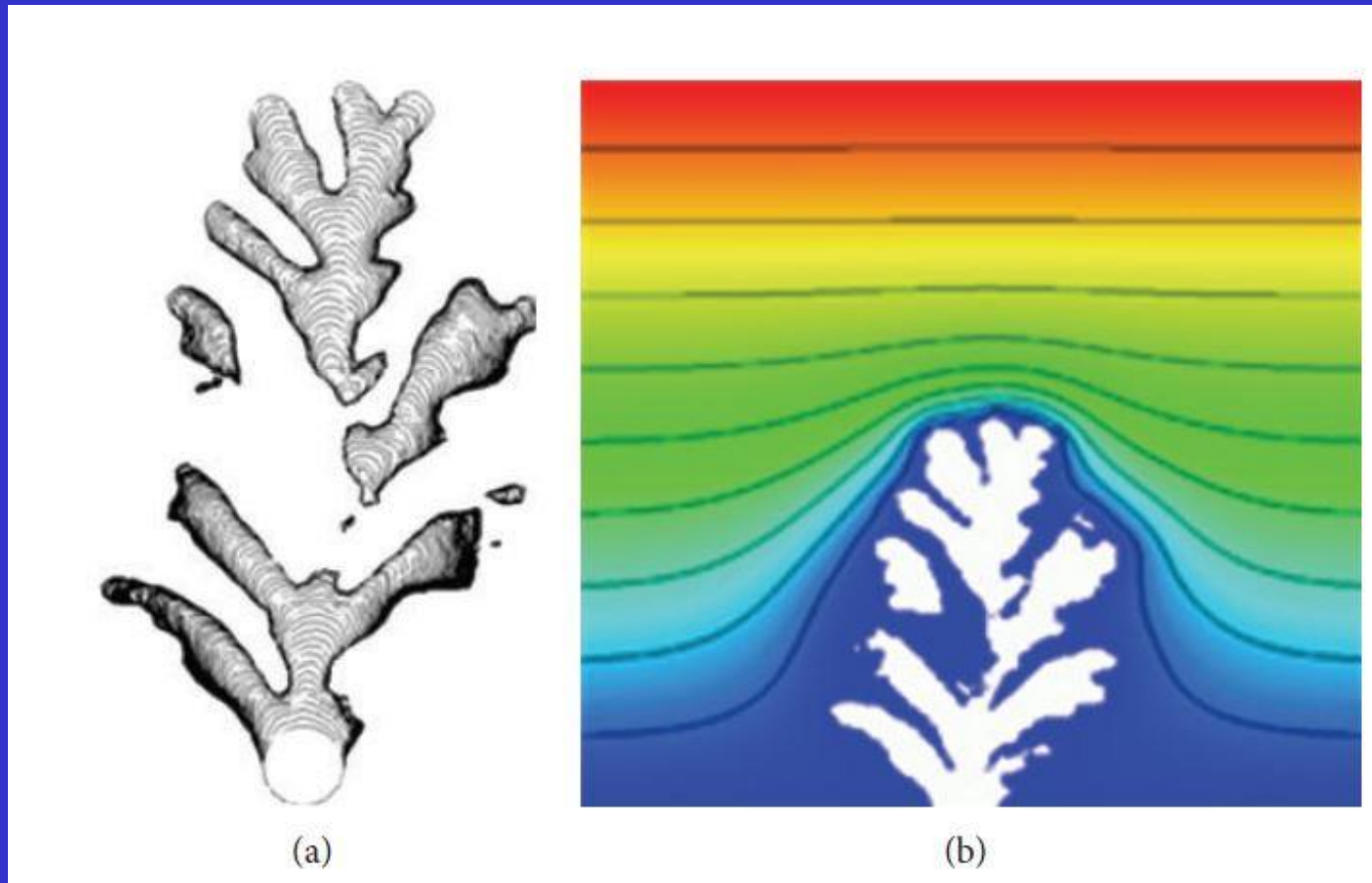
- The thickness of a new layer  $l$ , the distance between two successive vertices  $V_i$  and  $V_{i+1}$ , is computed by using the growth function:

$$l = \vec{n} c_i^{\text{total}} s,$$

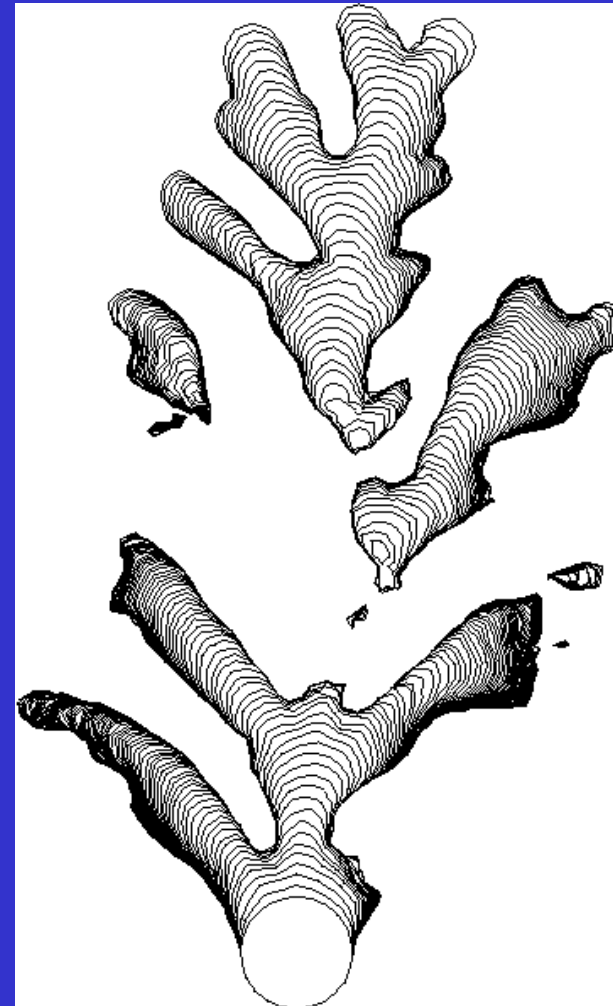
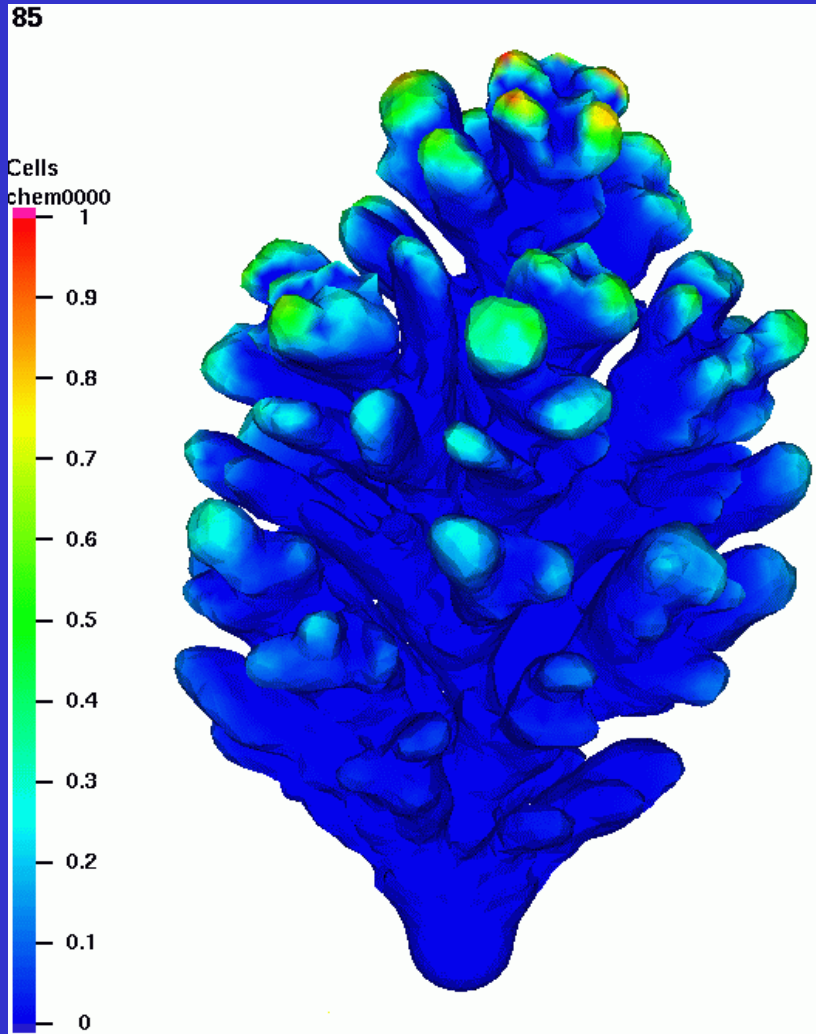
$$c_i^{\text{total}}$$

- where  $\vec{n}$  is the average normal vector in vertex  $V$  and the amount of absorbed simulated nutrients and  $s$  is the maximal thickness of the growth layer.

# Accretive growth: layered deposition of material (diffusion limited growth)



# Accretive growth: layered deposition of material (diffusion limited growth)



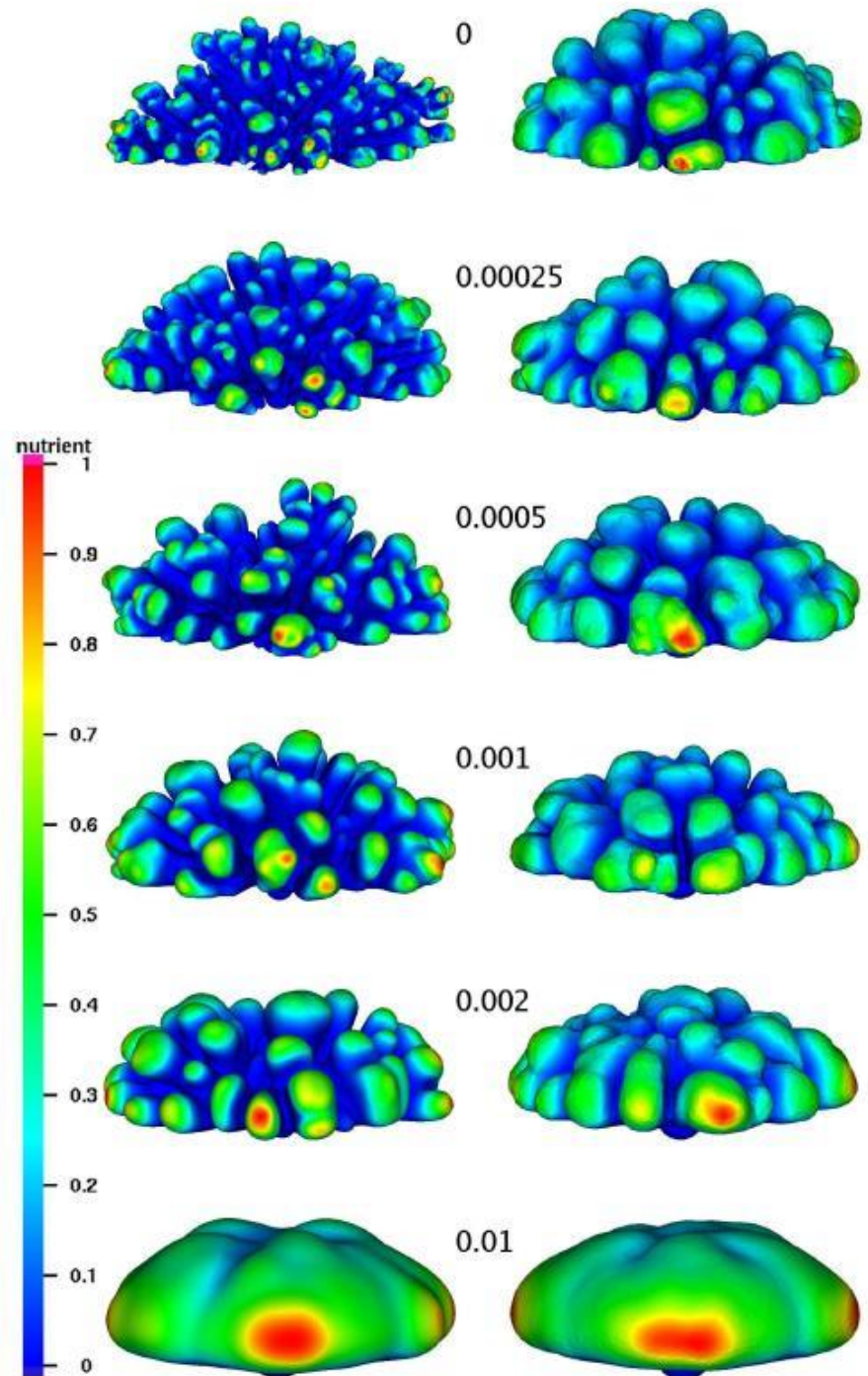


# Modelling diffusion-limited growth and translocation of absorbed nutrients by surface diffusion

- The translocation of absorbed nutrients by surface diffusion is modelled by:

$$\frac{\partial c(x, t)}{\partial t} = D_{\text{surf}} \nabla^2 c(x, t)$$

Diffusion  
limited growth  
+ surface  
diffusion: from  
top to bottom  
amount of  
surface  
diffusion  
( $D_{surf}$ ) is  
increased



# Modelling diffusion-limited growth and the influence of light intensities

- The thickness of a new layer  $l$ , the distance between two successive vertices  $V_i$  and  $V_{i+1}$ , is computed by using the growth function:

$$c_i^{\text{total}} = (1 - \alpha) c_i^{\text{nutrient}} + \alpha c_i^{\text{light}}, \quad 0 \leq \alpha \leq 1$$

- Where  $c_i^{\text{nutrient}}$  are local absorbed nutrient and  $c_i^{\text{light}}$  are the local absorbed light intensity, and alpha is a weight factor .

# Computing local light intensity

$$c_i^{\text{light}} = (1 - \text{ambient}) \cos \theta + \text{ambient},$$
$$0 \leq \text{ambient} \leq 1.$$

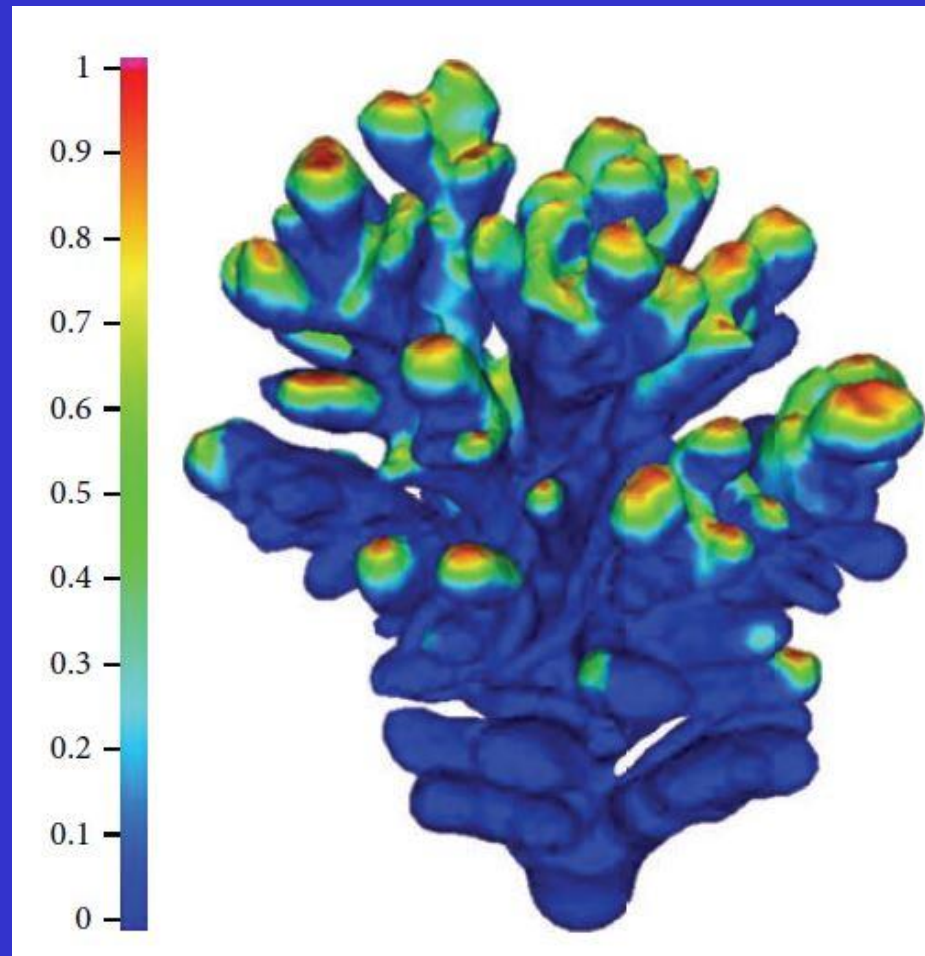
- Where  $\theta$  is the angle between the mean normal vector in vertex  $V_i$  and the direction to the light source (the vertical in the simulation box). The parameter *ambient* is included to capture ambient light by reflections from the environment.

# Computing local light intensity, correcting for shading effects

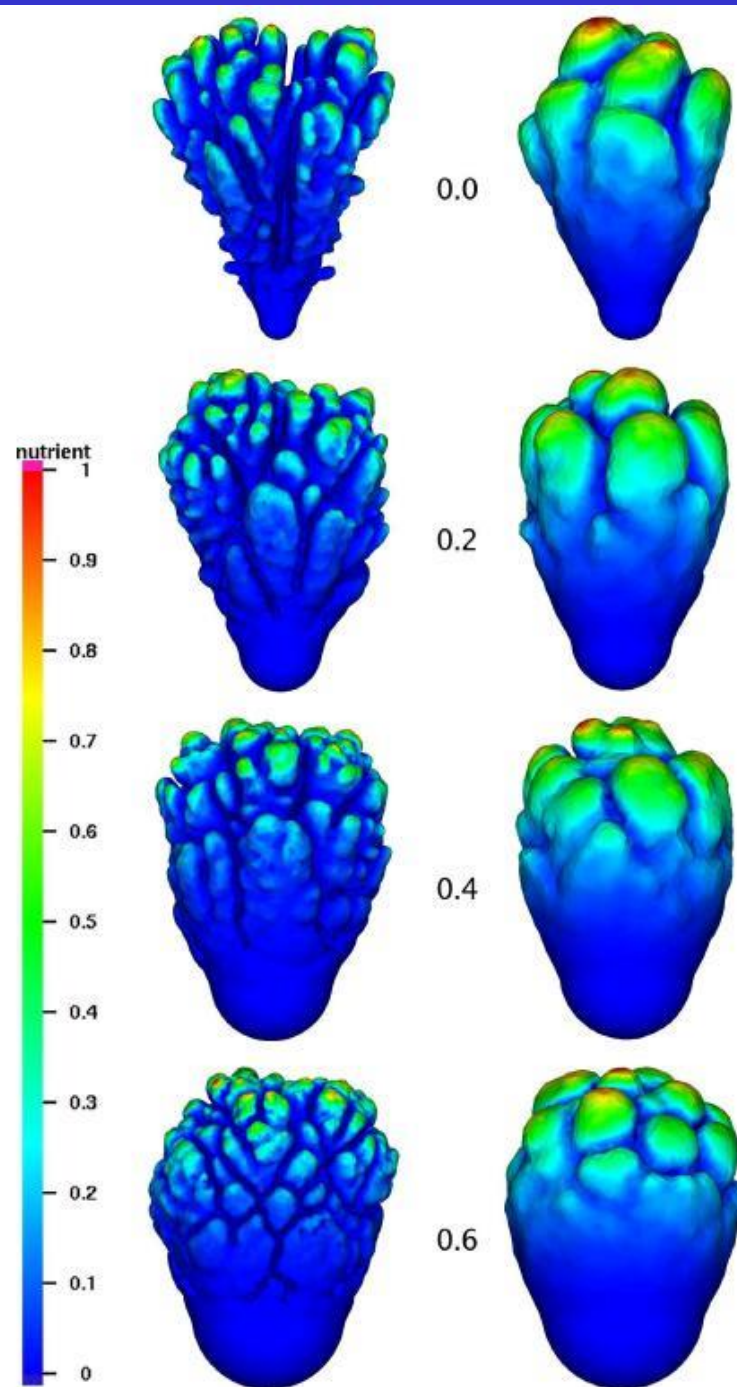
$$c_i^{\text{light}} = c_i^{\text{light}} \times \frac{\text{\#voxels-illum-in-triangles-surrounding-}i}{\text{\#voxels-total-in-triangles-surrounding-}i}$$

- In the previous equation there is no shading of triangles included; to correct for shading effects by occlusion of other parts of the simulated object we have used an algorithm based on volume rendering techniques in which the object is represented in a three dimensional lattice

# Computing light intensities in complex-shaped branching object

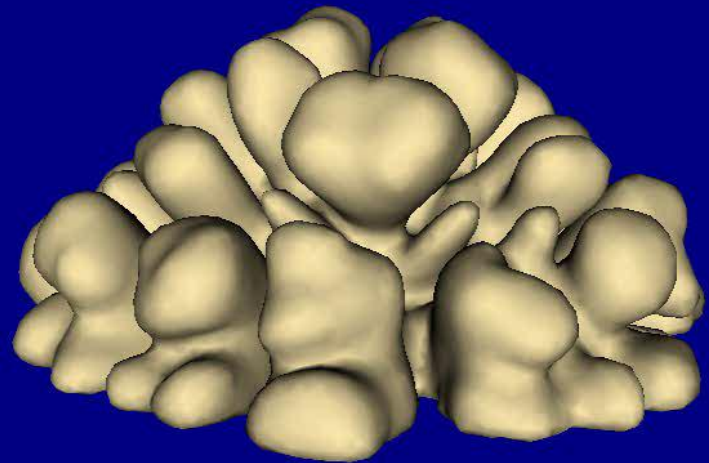
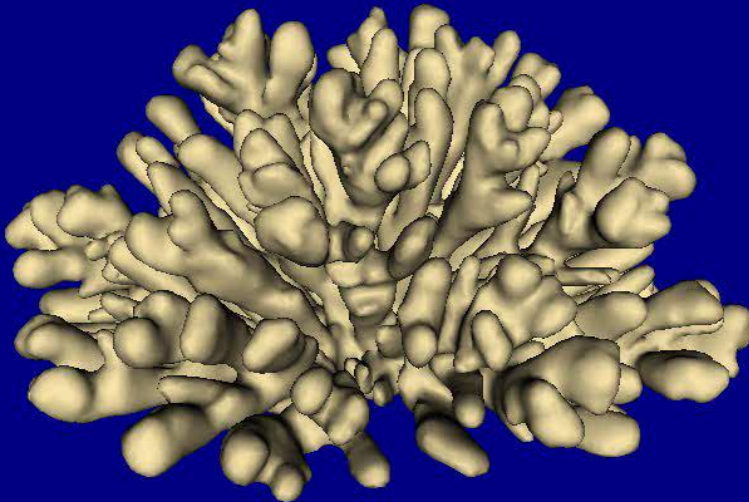
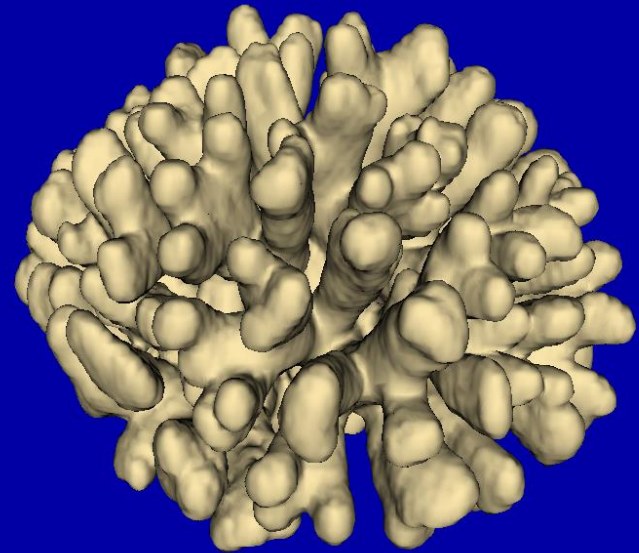


Diffusion limited  
growth + influence  
local light  
intensity: from top  
to bottom influence  
of light (alpha  
parameter) is  
increased



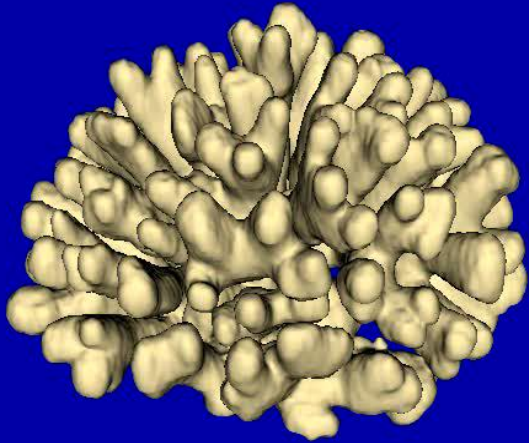
Turing test  
Accretive growth  
model (diffusion  
limited  
conditions)

(Kaandorp et al., Proc.  
Roy. Soc. Lond. B,  
2005)

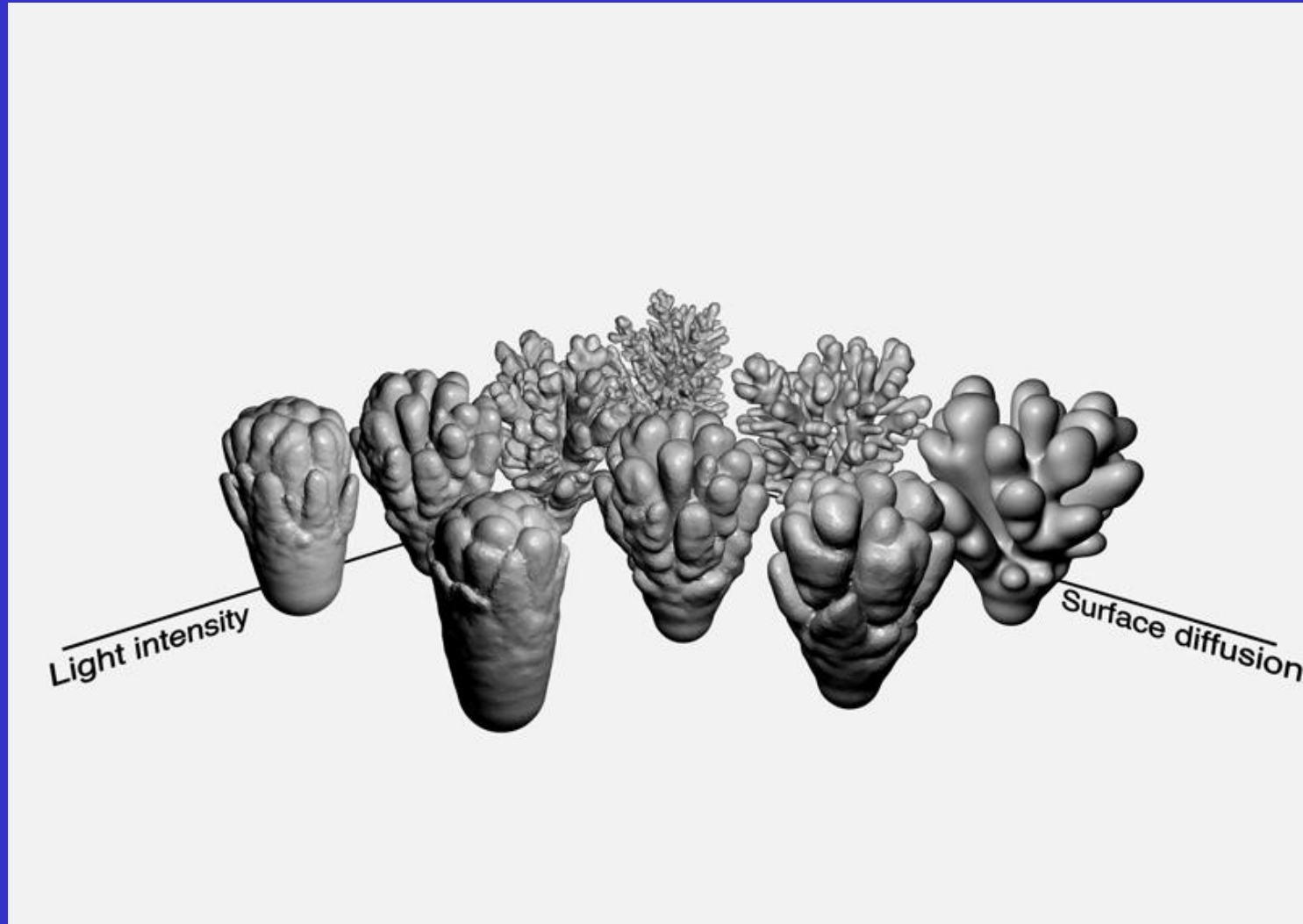




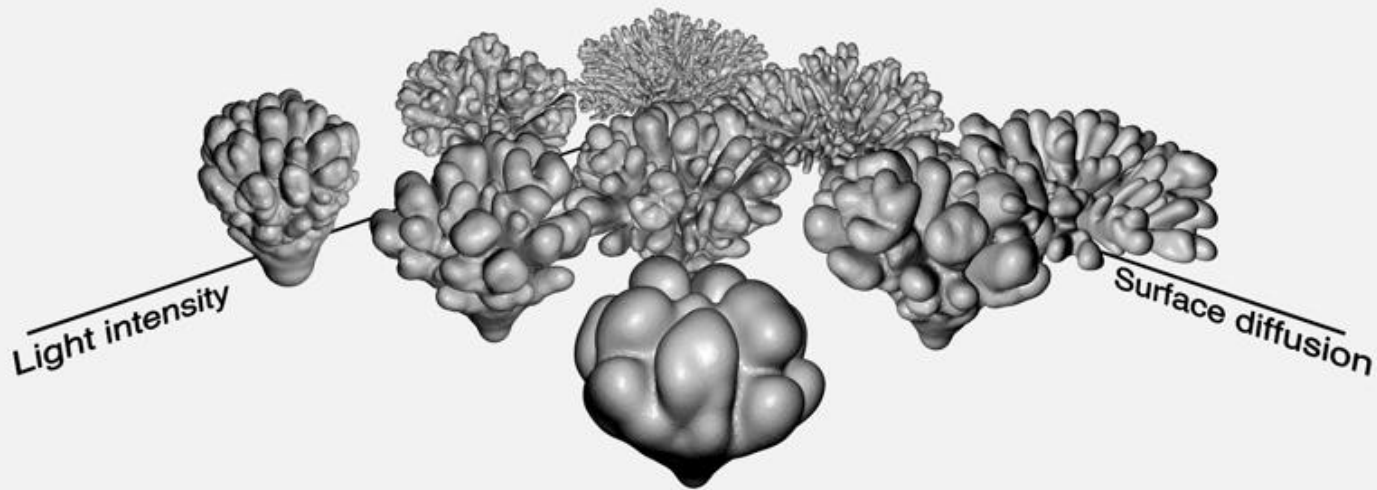
# Turing test Accretive growth model



# Simulated Morphospace (Filatov et al, Proc Roy Soc B, 2010)



# Simulated Morphospace II



# Modelling flow



## II Hydrodynamics

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \rho U = 0$$

$$\frac{\partial U}{\partial t} = -(U \cdot \nabla)U - \frac{1}{\rho} \nabla P + \nu \nabla^2 U$$

**The first equation expresses the conservation of mass and the second one the conservation of momentum, where  $\rho$  represents the mass density,  $t$  the time,  $U$  the flow velocity,  $P$  the pressure, and  $\nu$  the kinematic viscosity.**

# Modelling Advection- diffusion-limited growth

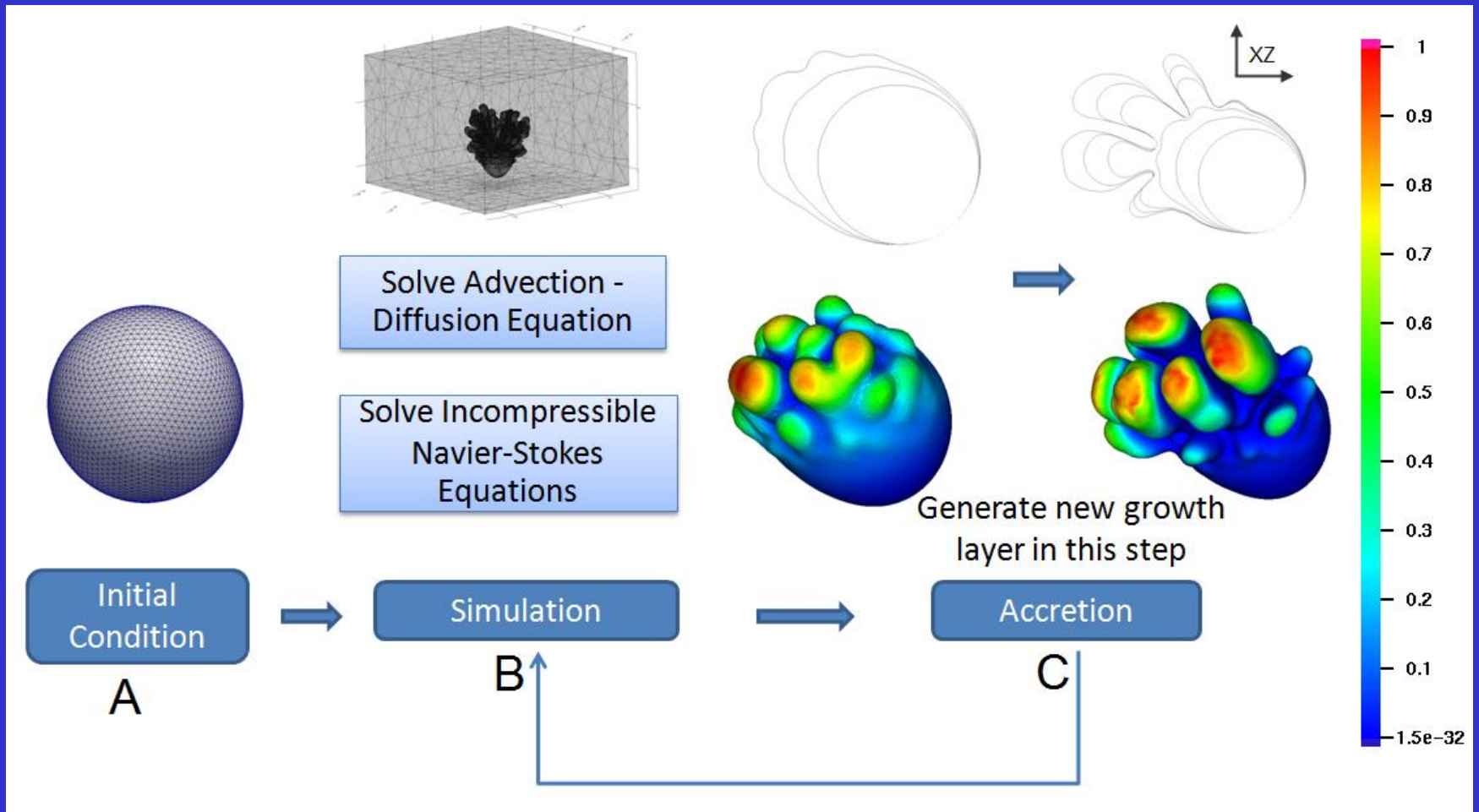
- The thickness of a new layer  $l$ , the distance between two successive vertices  $V_i$  and  $V_{i+1}$ , is computed by using the growth function:

$$l = \vec{n} c_i^{\text{total}} s,$$

$$c_i^{\text{total}}$$

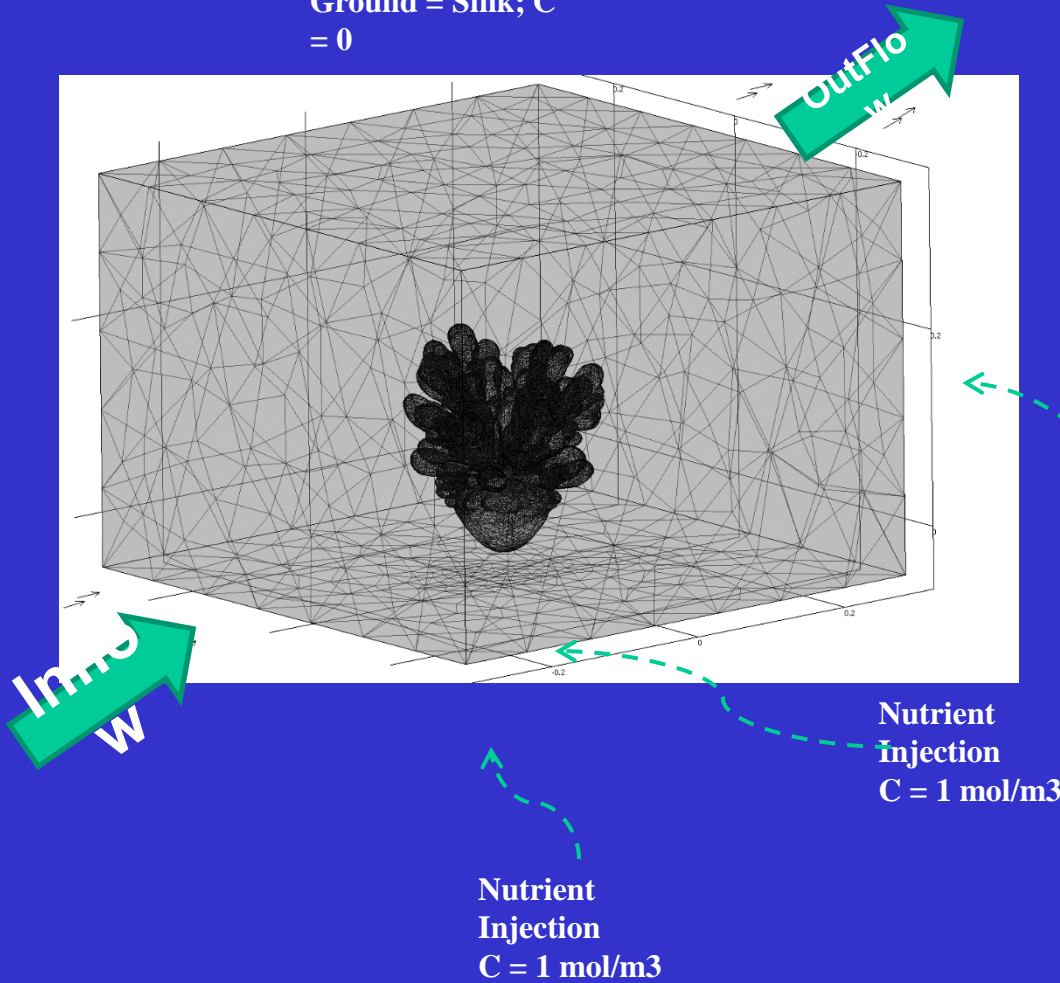
- where  $\vec{n}$  is the average normal vector in vertex  $V$  and the amount of absorbed simulated nutrients and  $s$  is the maximal thickness of the growth layer.

# Modelling Coral Growth



# Simulation Domain

Object and  
Ground = Sink;  $C$   
= 0



- A finite-element mesh was constructed by generating a simulation box with dimensions 60 cm in  $x$  and  $y$  direction and 40 cm in  $z$  direction (the height of the simulation box). The spherical object with an initial diameter of 6 cm was then imported to the simulation box.

- The flow fields around the simulated coral was obtained by solving the incompressible Navier-Stokes (NVS) equations:

$$\rho \frac{\partial \mathbf{u}}{\partial t} - \nabla \cdot [\eta(\nabla \mathbf{u} + (\nabla \mathbf{u})^T)] + \rho(\mathbf{u} \cdot \nabla)\mathbf{u} + \nabla p = \mathbf{F}$$

$$\nabla \cdot \mathbf{u} = 0$$

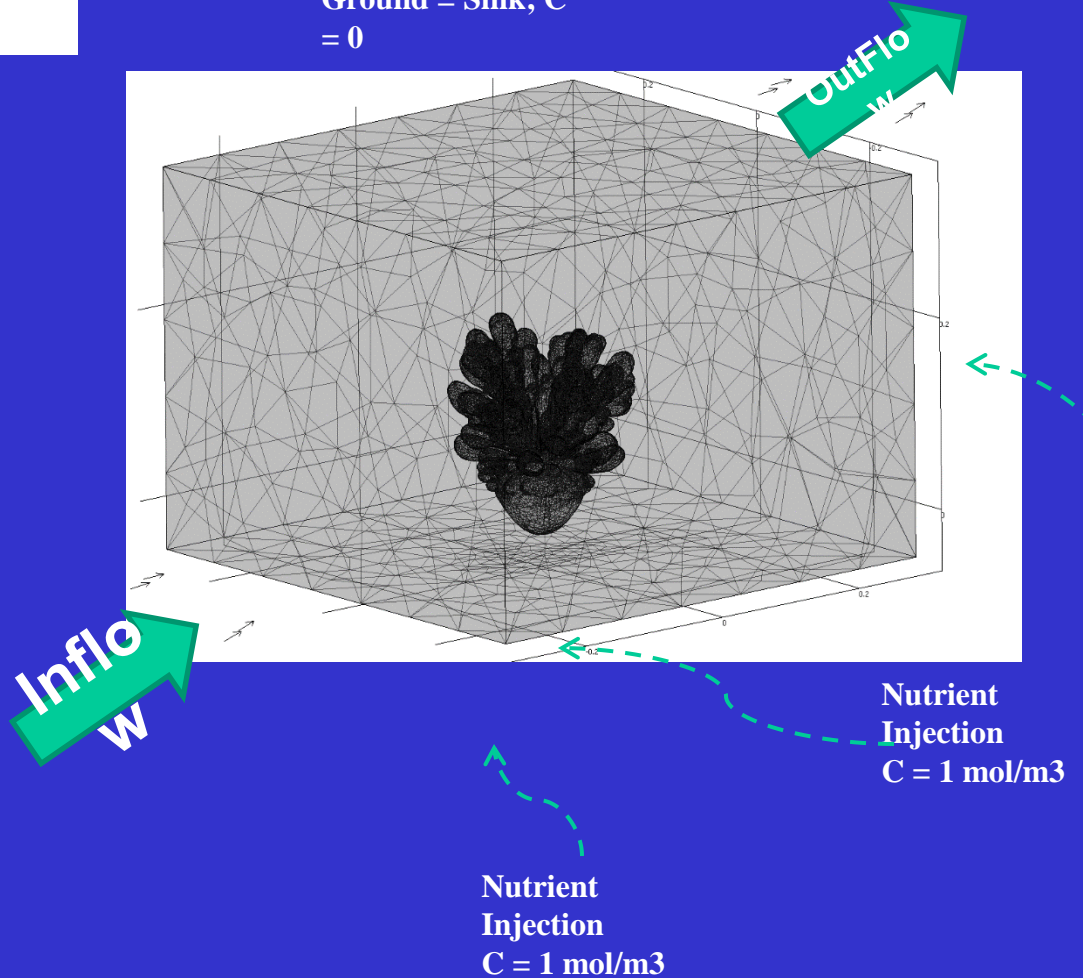
$\mathbf{u}$  is the velocity field,  
 $p$  is the pressure,  
 $\rho$  is the density,  
 $\eta$  is the dynamic viscosity  
 $\mathbf{F}$  is a volume force field such as Gravity

- The transport of nutrients was obtained by solving Advection Diffusion Equation

$$\frac{\partial C}{\partial t} + \vec{u} \cdot \nabla C = D \nabla^2 C,$$

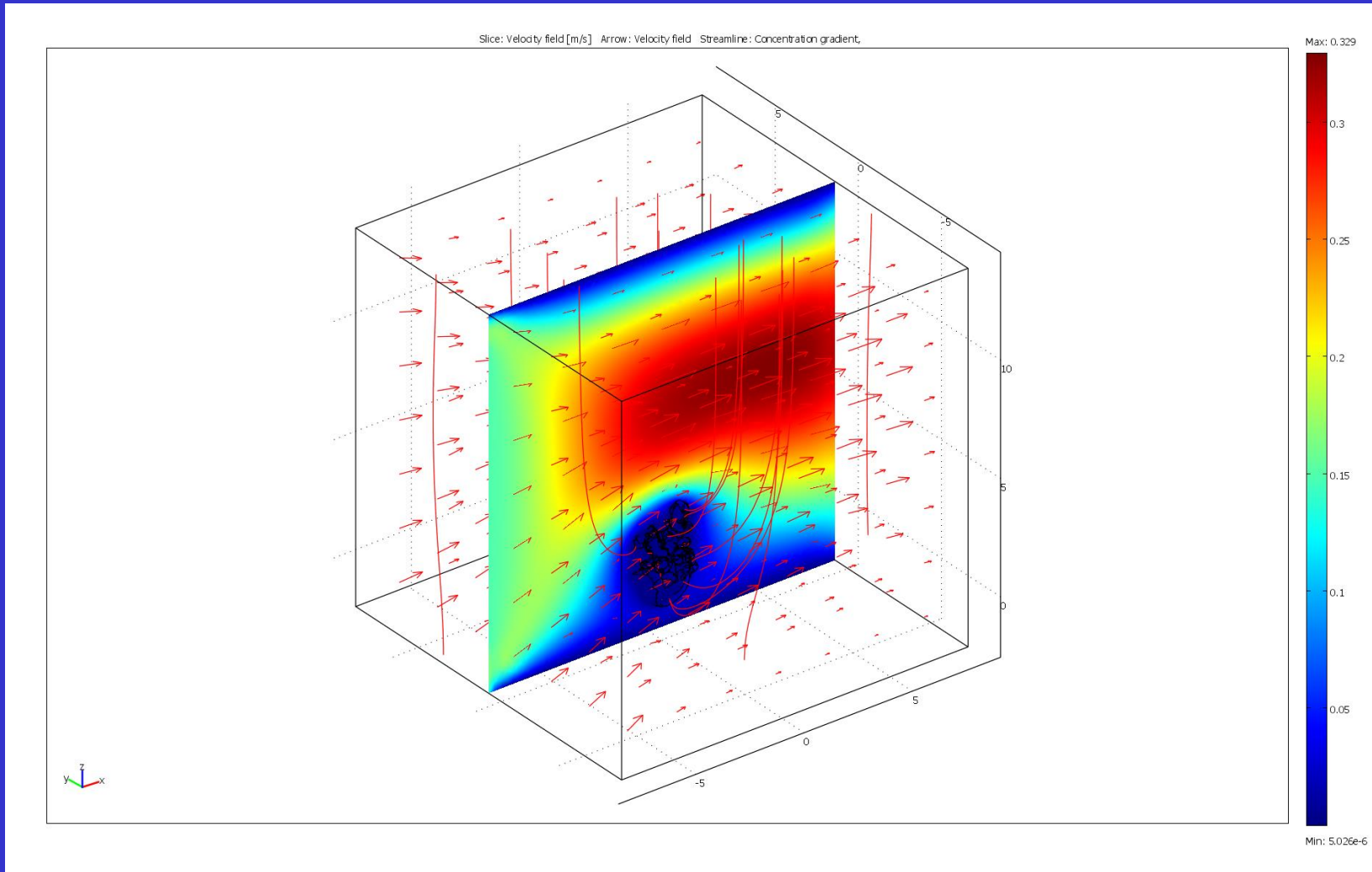
$\mathbf{u}$  is the advection velocity vector,  
 $D$  is the diffusion coefficient,  
 $C$  is a concentration

Object and Ground = Sink;  $C = 0$





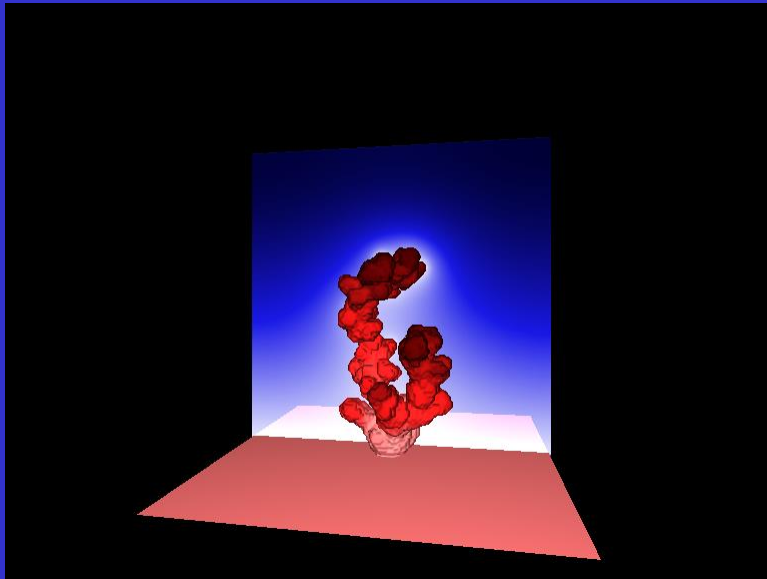
# Advection-diffusion simulations (arrow indicates local flow velocity, colour indicated local nutrient concentration)



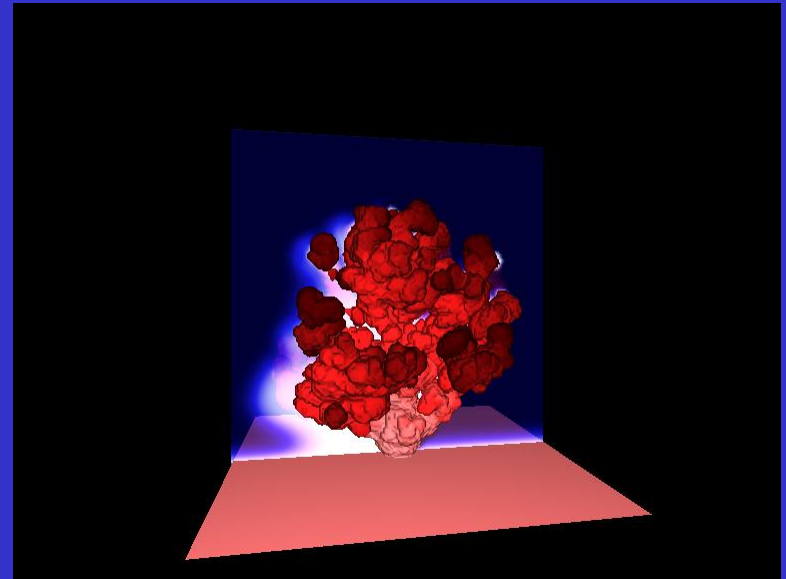
# Accretive growth model nutrient distributions



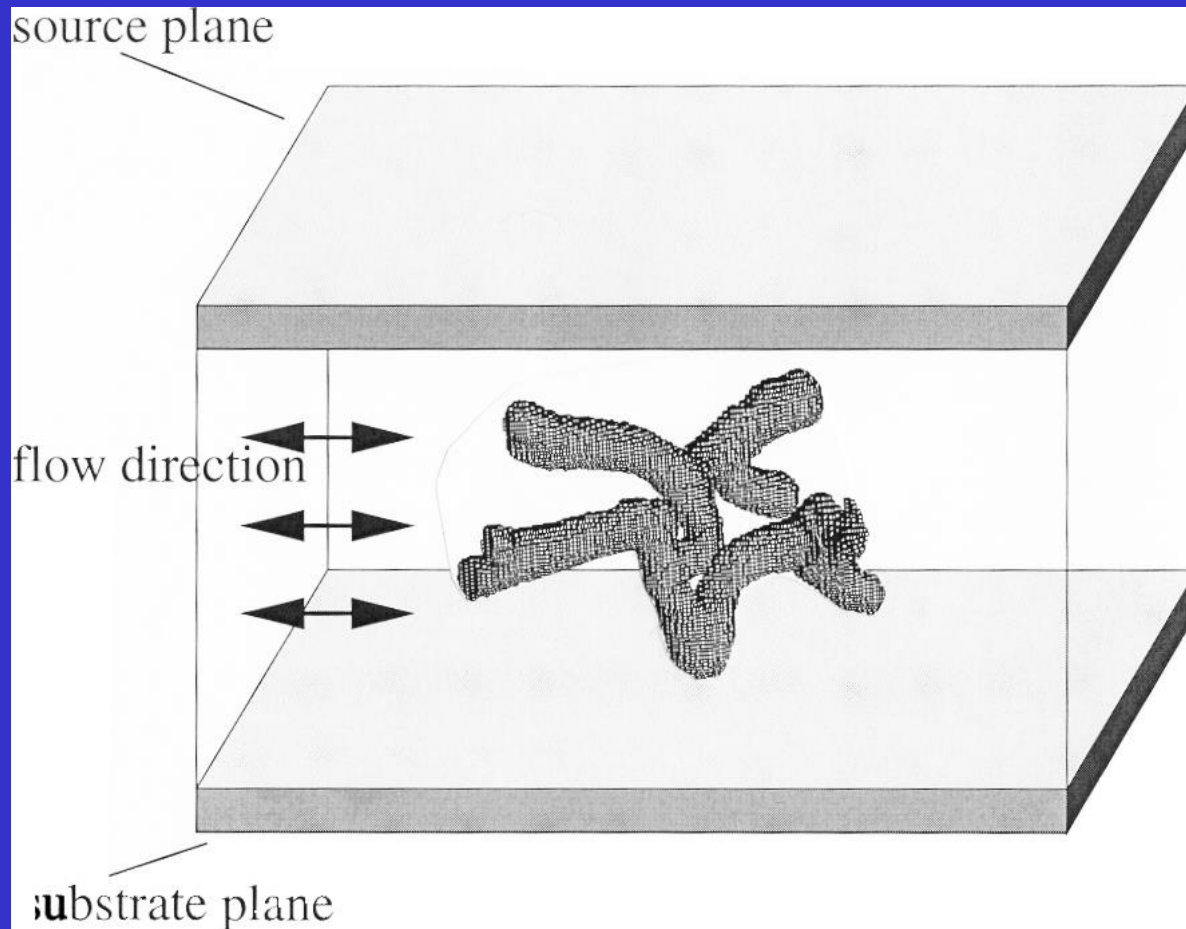
**Diffusion limited**



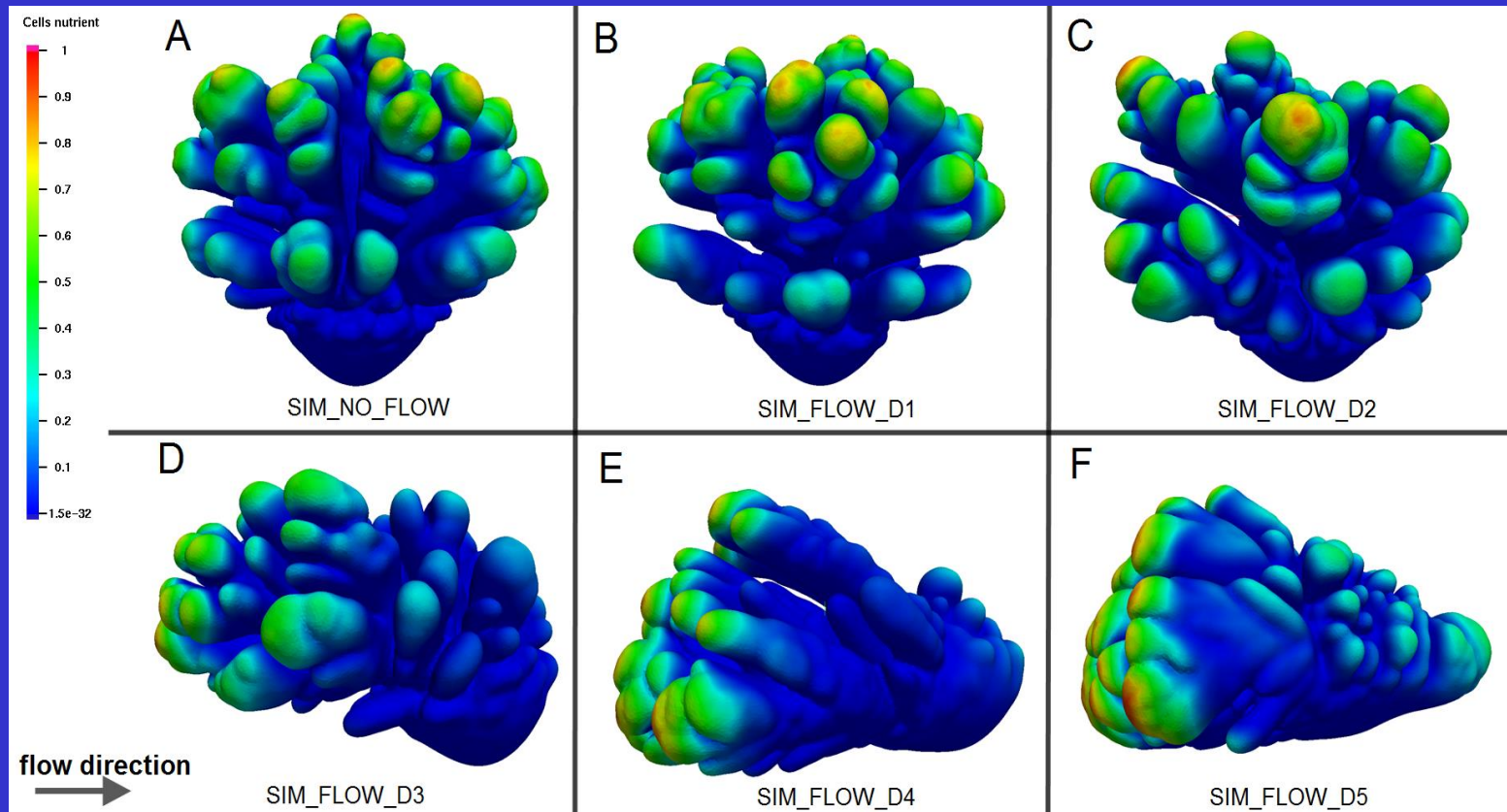
**Flow limited**



# Coupling accretive growth model and advection-diffusion



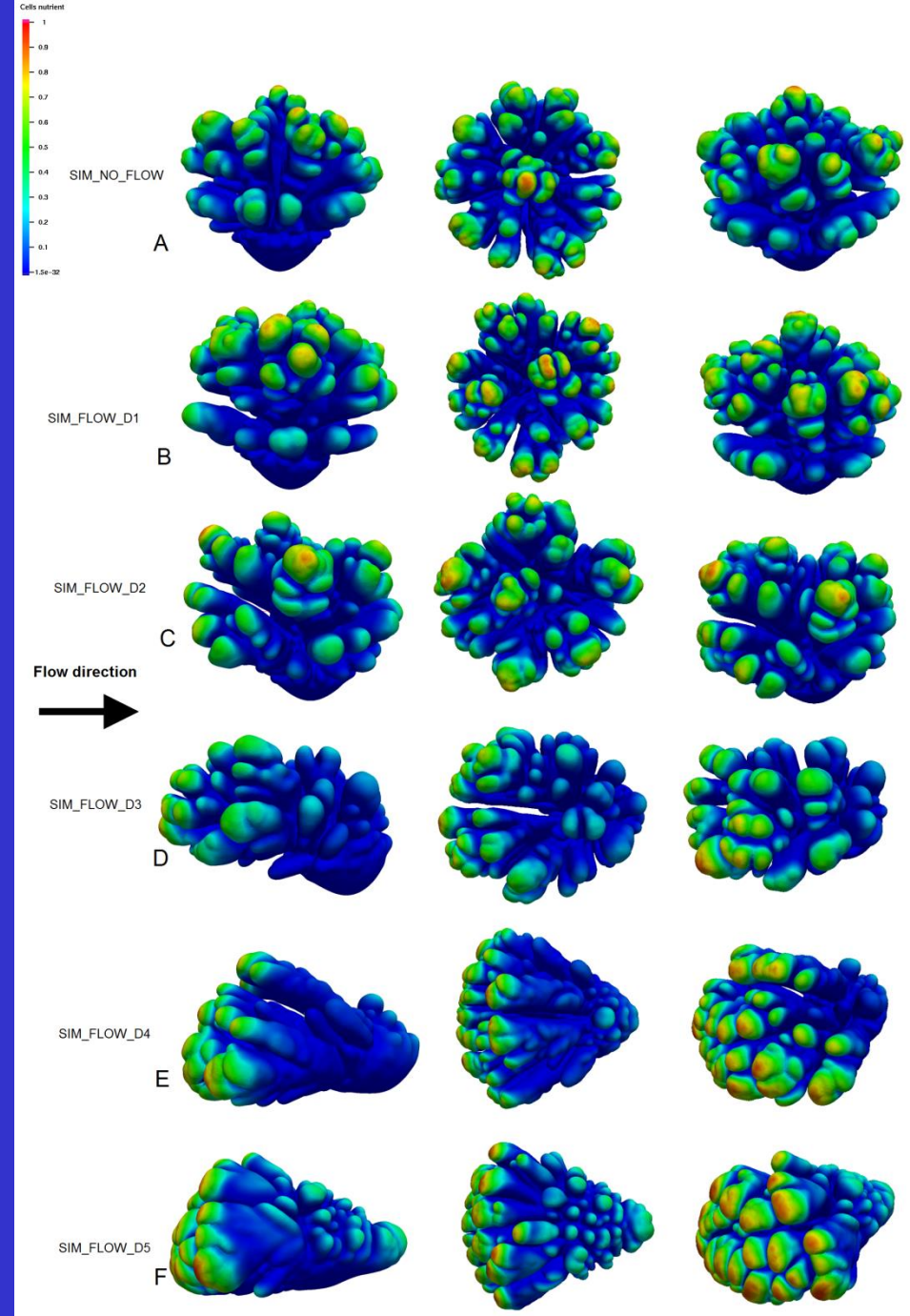
# Results (Chindapol et al., Plos Comp. Biol., 2013)

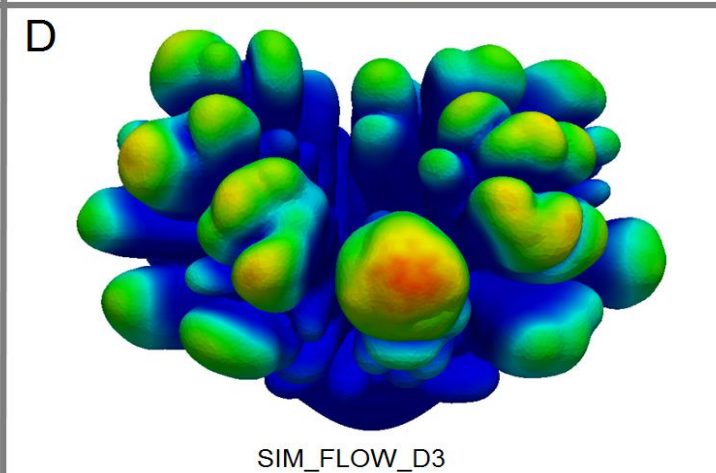
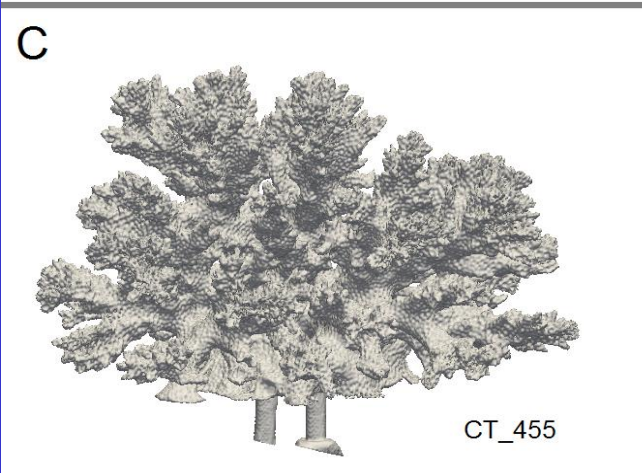
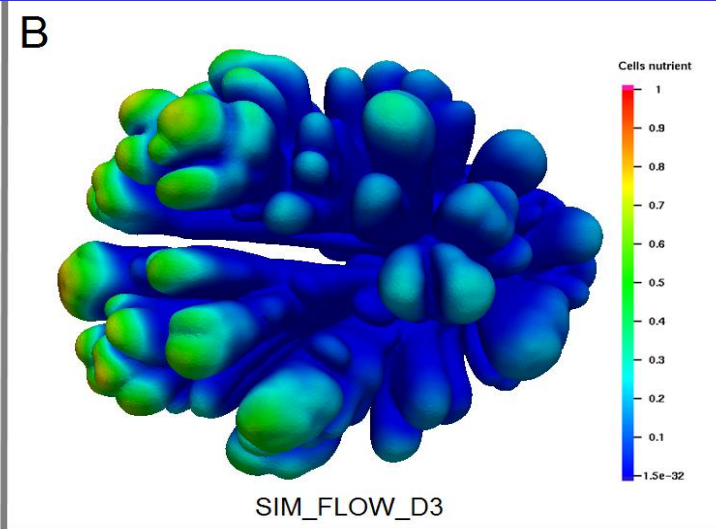
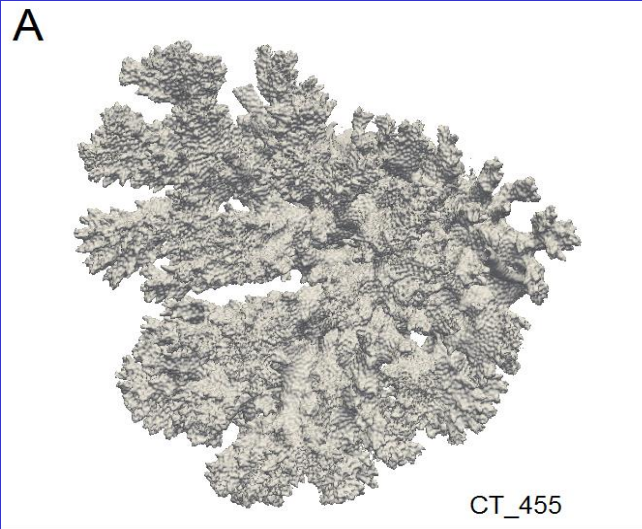


- (A) Simulated coral in a no-flow condition. (B-F) Simulated growth forms from different flow simulations (B)  $Pe = 0.34$ , (C)  $Pe = 3.45$ , (D)  $Pe = 33.5$ , (E)  $Pe = 302.89$ , (F)  $Pe \sim 3000$ , Arrow indicates flow direction. The labels of the simulated corals are located on the bottom of each figure (See Table 1 for labels).

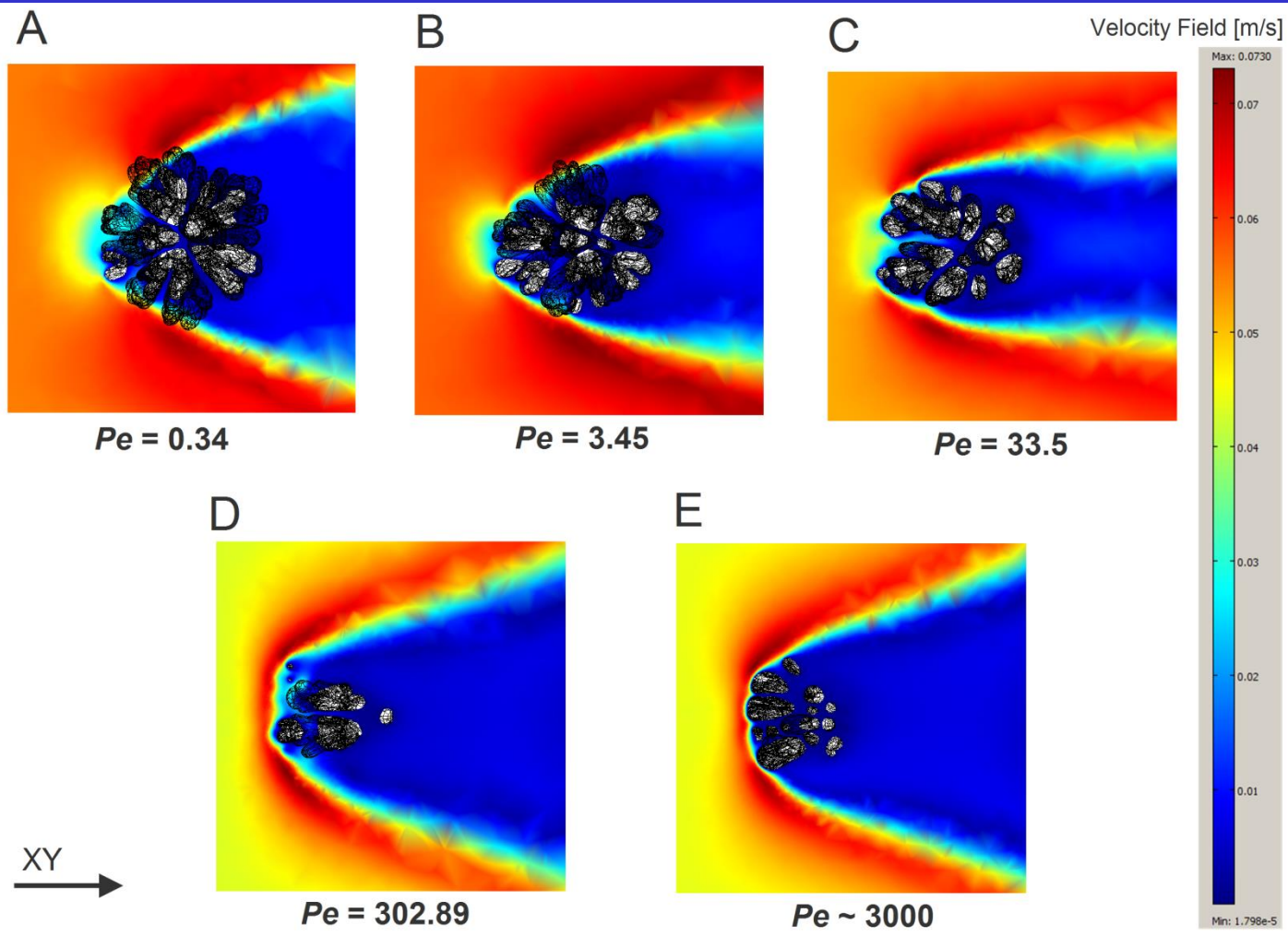
# Influence of flow on morphology

We observed that in a range of increasing  $Pe$  numbers the degree of asymmetry of the branching objects becomes larger. In this range branches tend to be formed in the stream upward direction. While branch formation on the downstream sides is gradually suppressed





- Qualitative comparison between the real (A,C) and simulated coral (B,D)  $Pe = 33.5$



At higher  $Pe$  values the simulated growth forms show an asymmetrical branching pattern with a high degree of compactification.

The gradient in flow velocities in the upstream part of the simulated object becomes steeper for higher  $Pe$  numbers, leading to a higher degree of absorption of simulated nutrient in the upstream part of the object.

$z$ -plane Slices ( $z=0.07$ ) of the flow pattern around the simulated corals, the slices were taken from the middle part of the colony.

# Conclusion

- Increasing the  $Pe$  number induces the formation of asymmetrical branching growth forms
- In the flow simulations, we have found a decreasing trend of the surface/volume ratio and increased skewedness which is the same as real corals
- Our model shows that in this case there is no gene regulation needed to explain the formation of asymmetrical branching forms
- In reality most scleractinian corals will not be growing under uni-directional flow conditions but will be exposed to a two-phase flow where the flow direction is reversing twice a day because of the tidal movements.



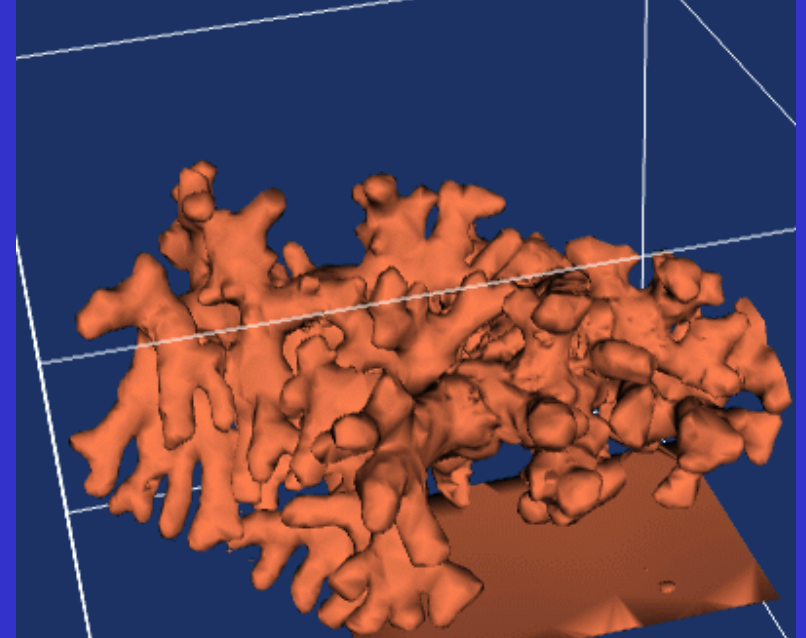
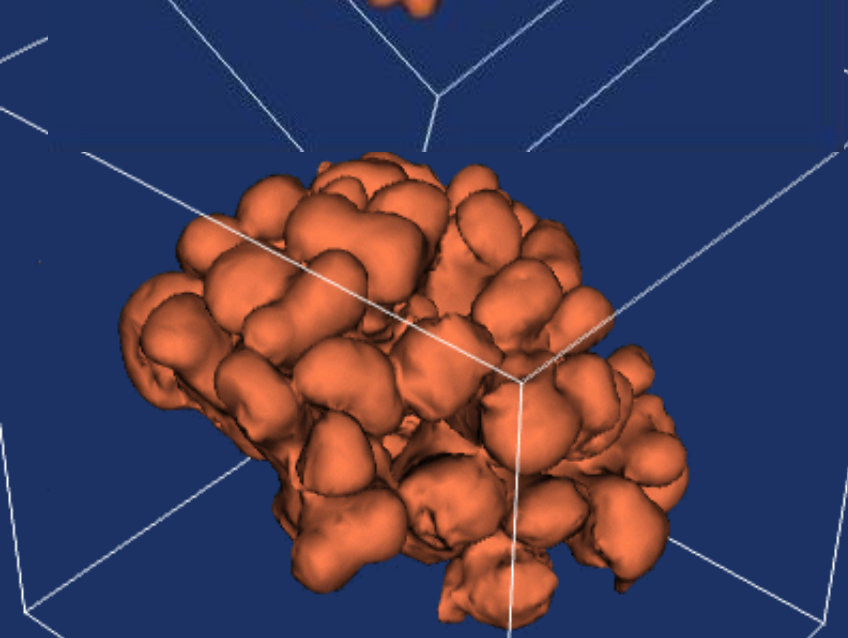
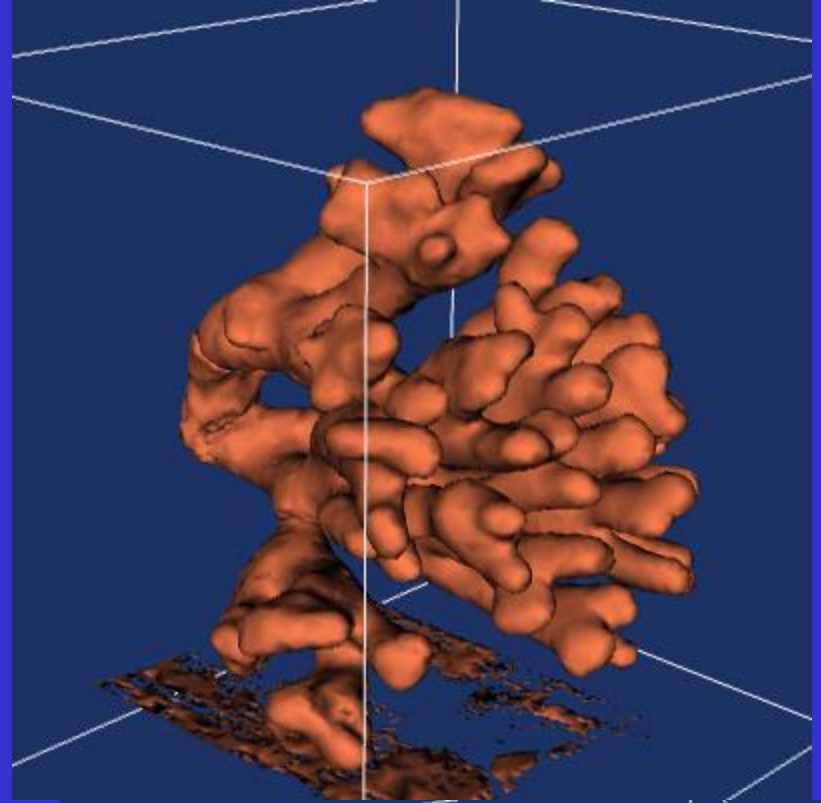
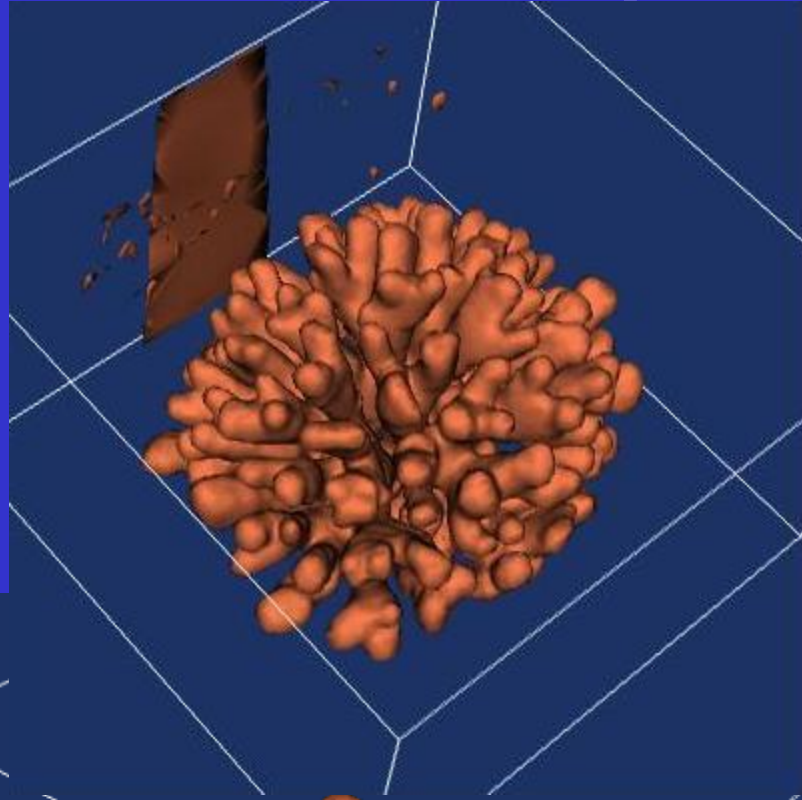
# Morphometrics of 3D indeterminate complex-shaped (branching) growth forms

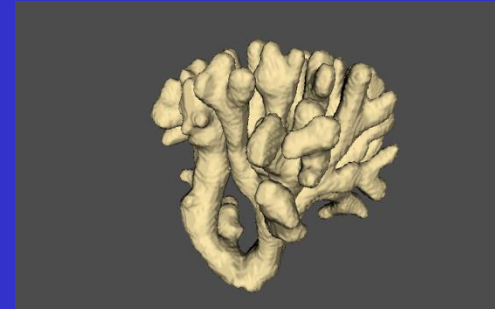
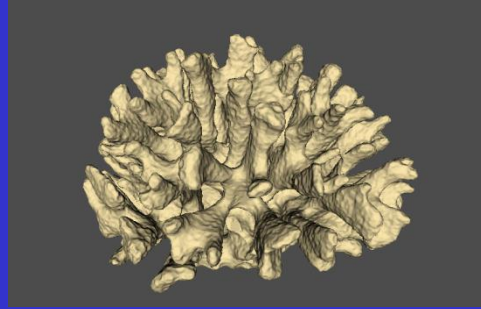
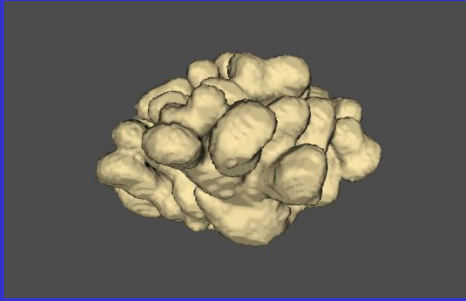
- Global measurements: fractal dimensions, branch ordering, compactness, surface, volume, surface/volume
- Local measurements: local curvature and morphological skeletons in 3D
- Quantifying absorption of nutrient and light in a growth form in 3D simulations

# Data acquisition



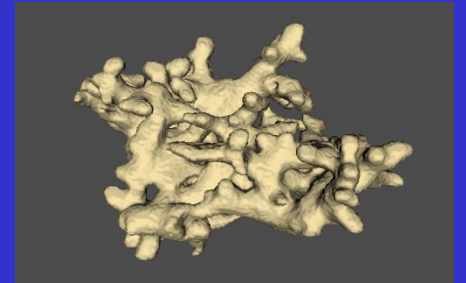
Comparison morphologies in  
different *Madracis* species





## ◆ Samples (CT-scans) of 4 coral species

- ◆ *Madracis decactis*
- ◆ *Madracis mirabilis*
- ◆ *Madracis carmabi*
- ◆ *Madracis formosa*



# Data processing

- ◆ DICOM image processing (e.g. filtering)
- ◆ Iso-surface extraction
- ◆ 3D-volume construction

# Landmark-based methods in unitary organisms (D'Arcy Thompson, 1917)

points will be found to correspond to very slight modifications of

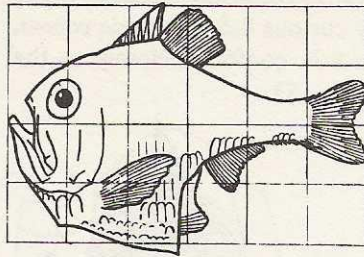


Fig. 146. *Argyropelecus olfersi*.

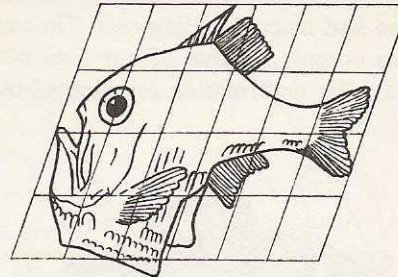


Fig. 147. *Sternoptyx diaphana*.

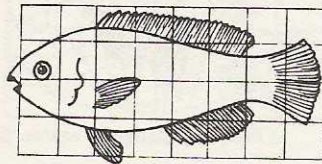


Fig. 148. *Scarus* sp.

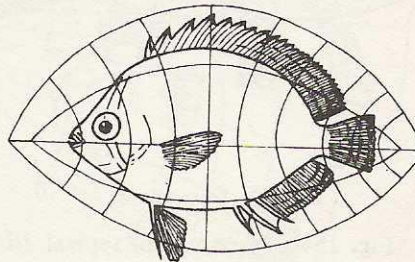
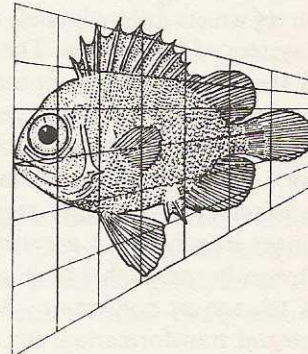
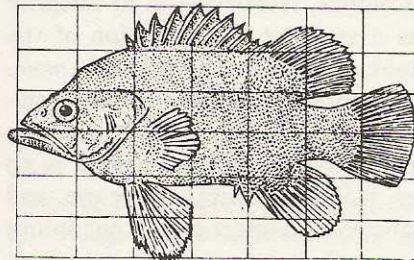


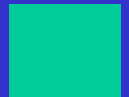
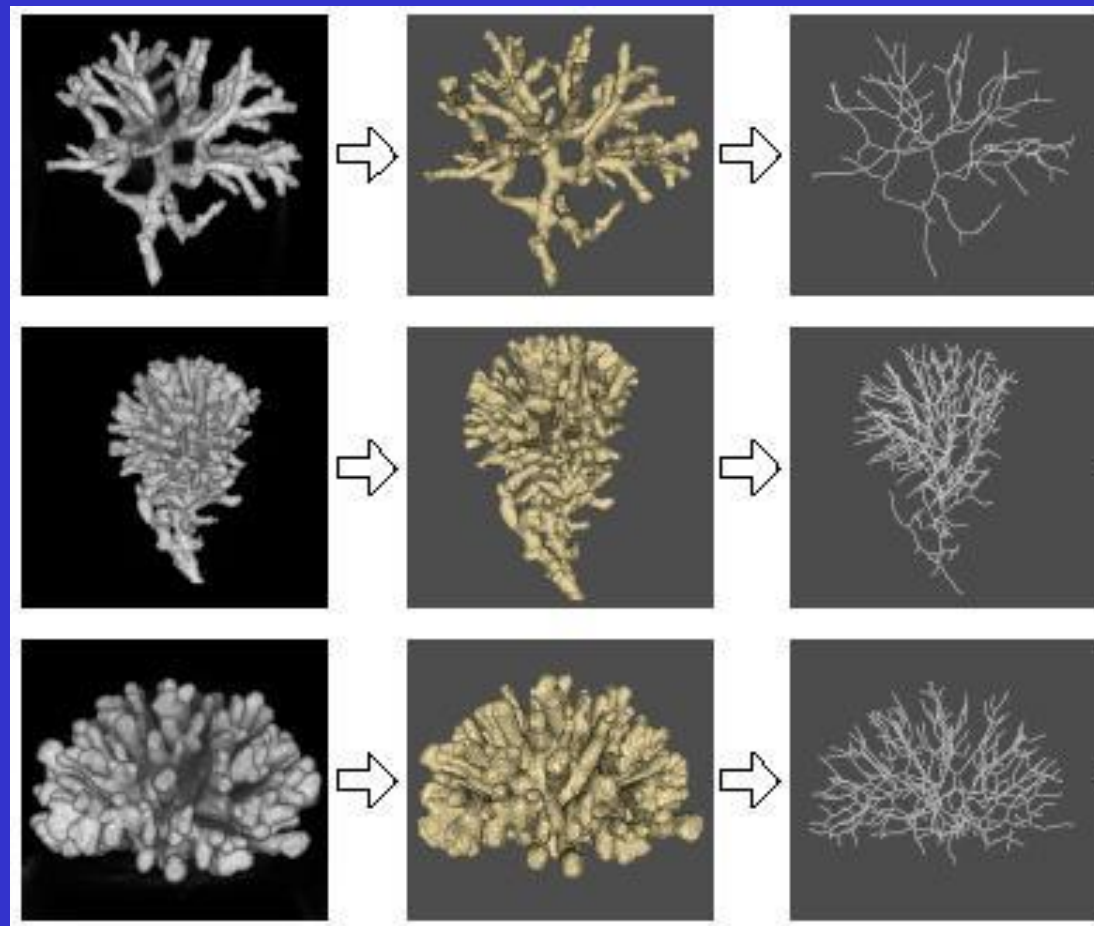
Fig. 149. *Pomacanthus*.



# Morphometrics of 3D indeterminate (branching) growth forms

- Global measurements: fractal dimensions, branch ordering, compactness, surface, volume, surface/volume
- Local measurements: local curvature and morphological skeletons in 3D

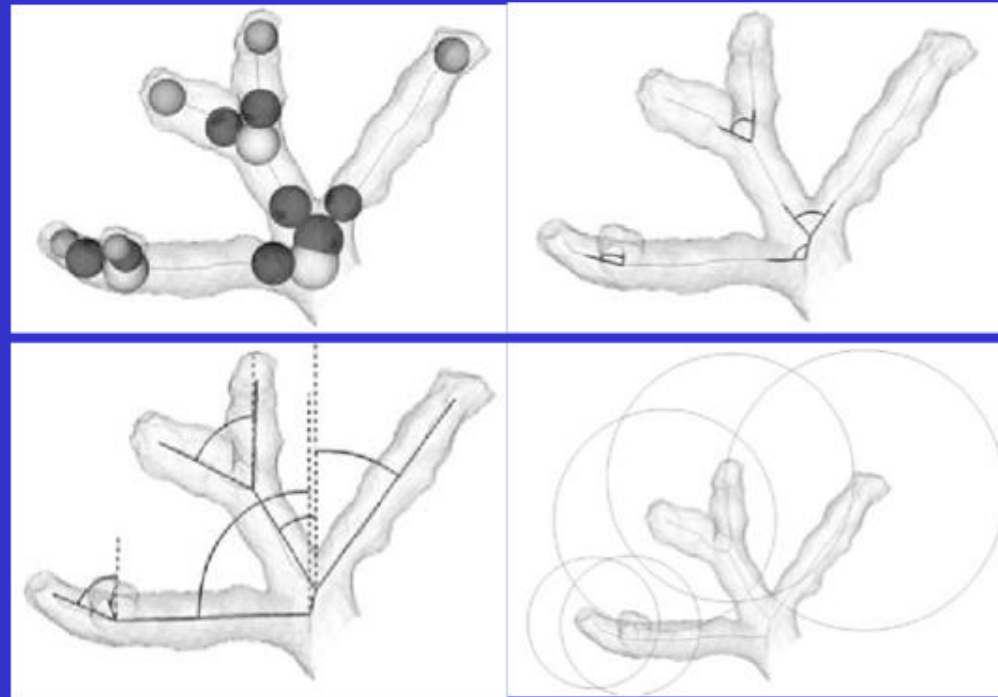
Morphological Skeleton in a 3D images of the coral *Madracis mirabilis* (K. Kruszynski, J.A. Kaandorp, R. van Liere, Coral Reefs 2007)



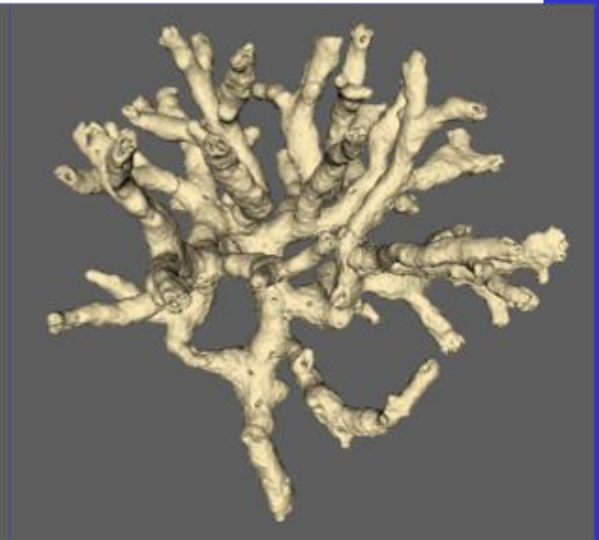
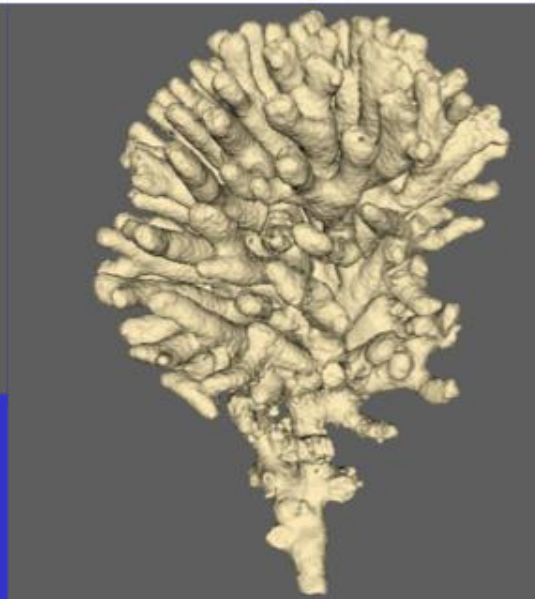
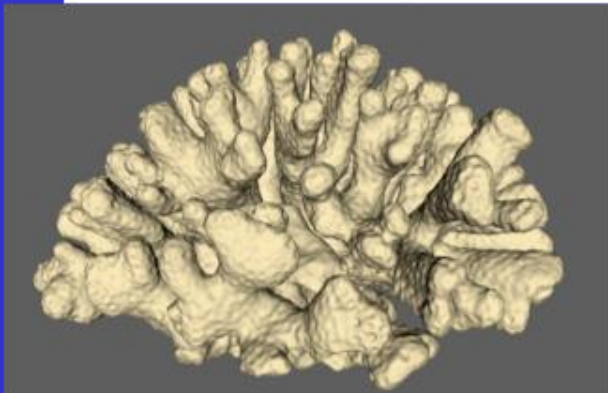
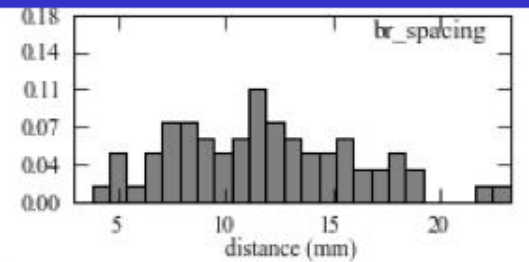
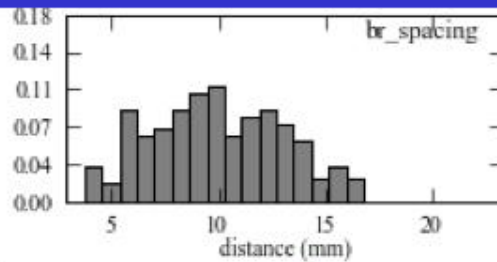
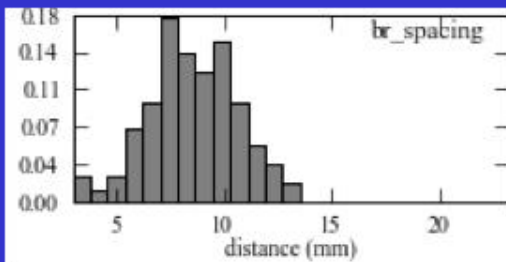


# Coral Morphometrics

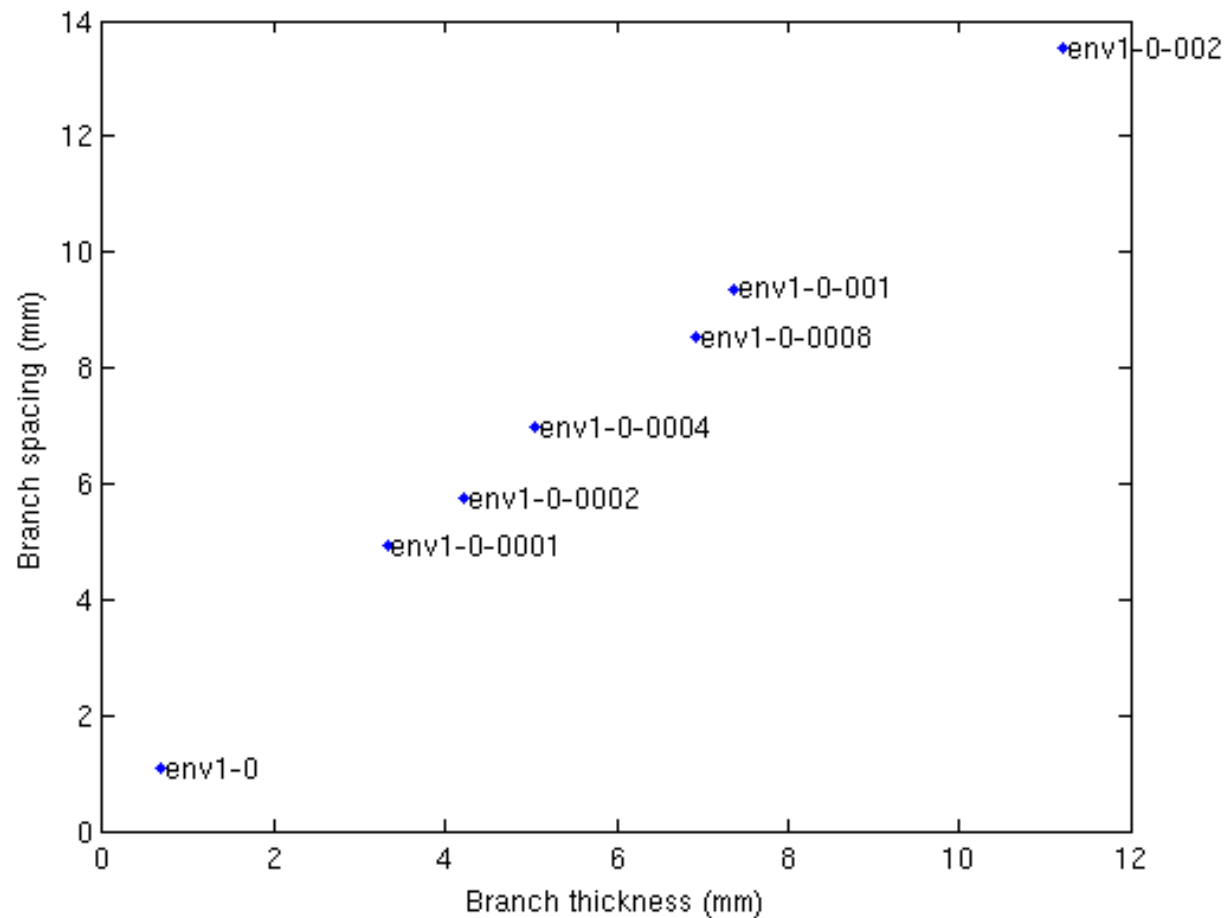
- ◆ Branch thickness
- ◆ Branching angle
- ◆ Branch spacing



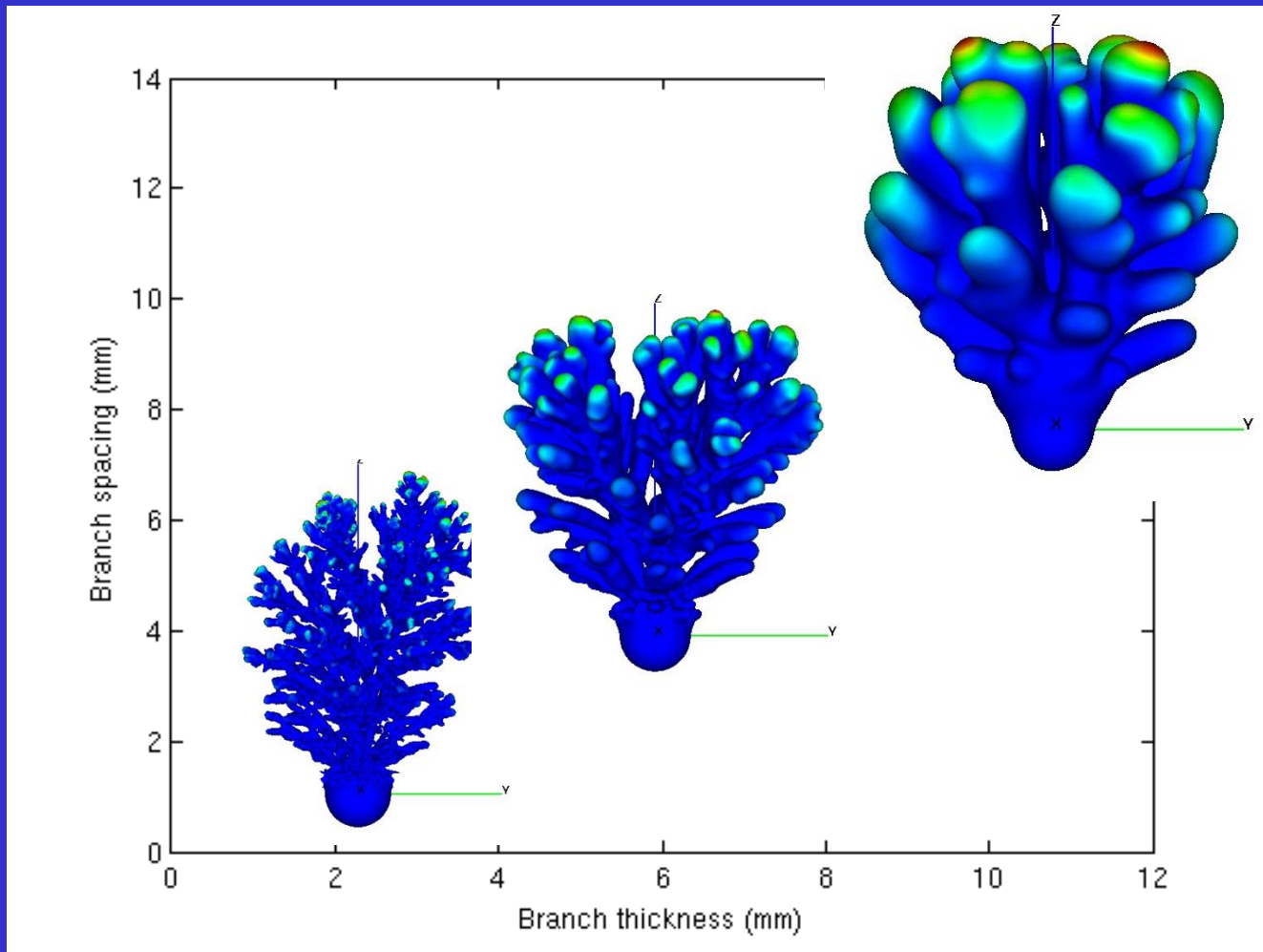
# Coral Morphometrics II



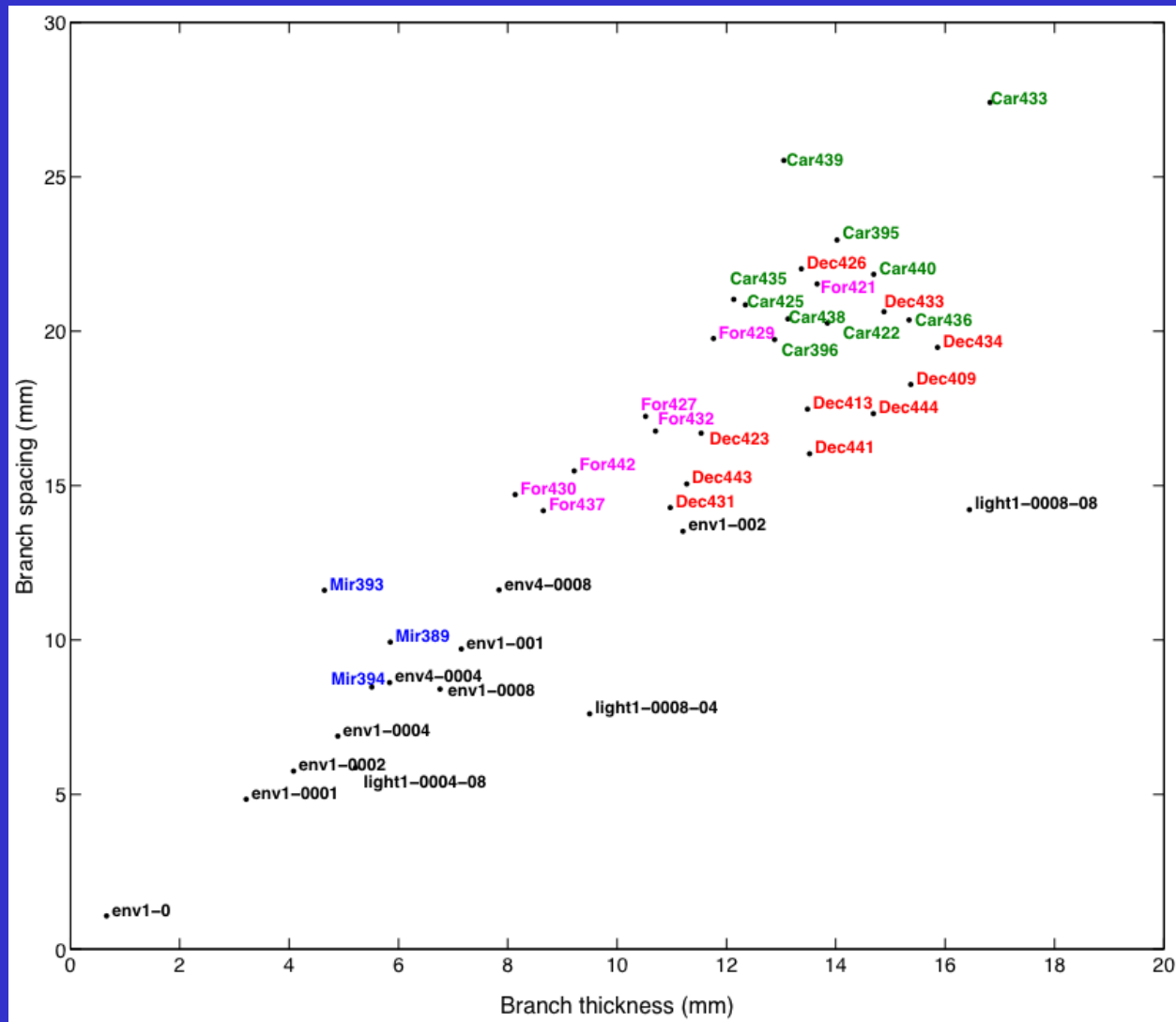
# Results I



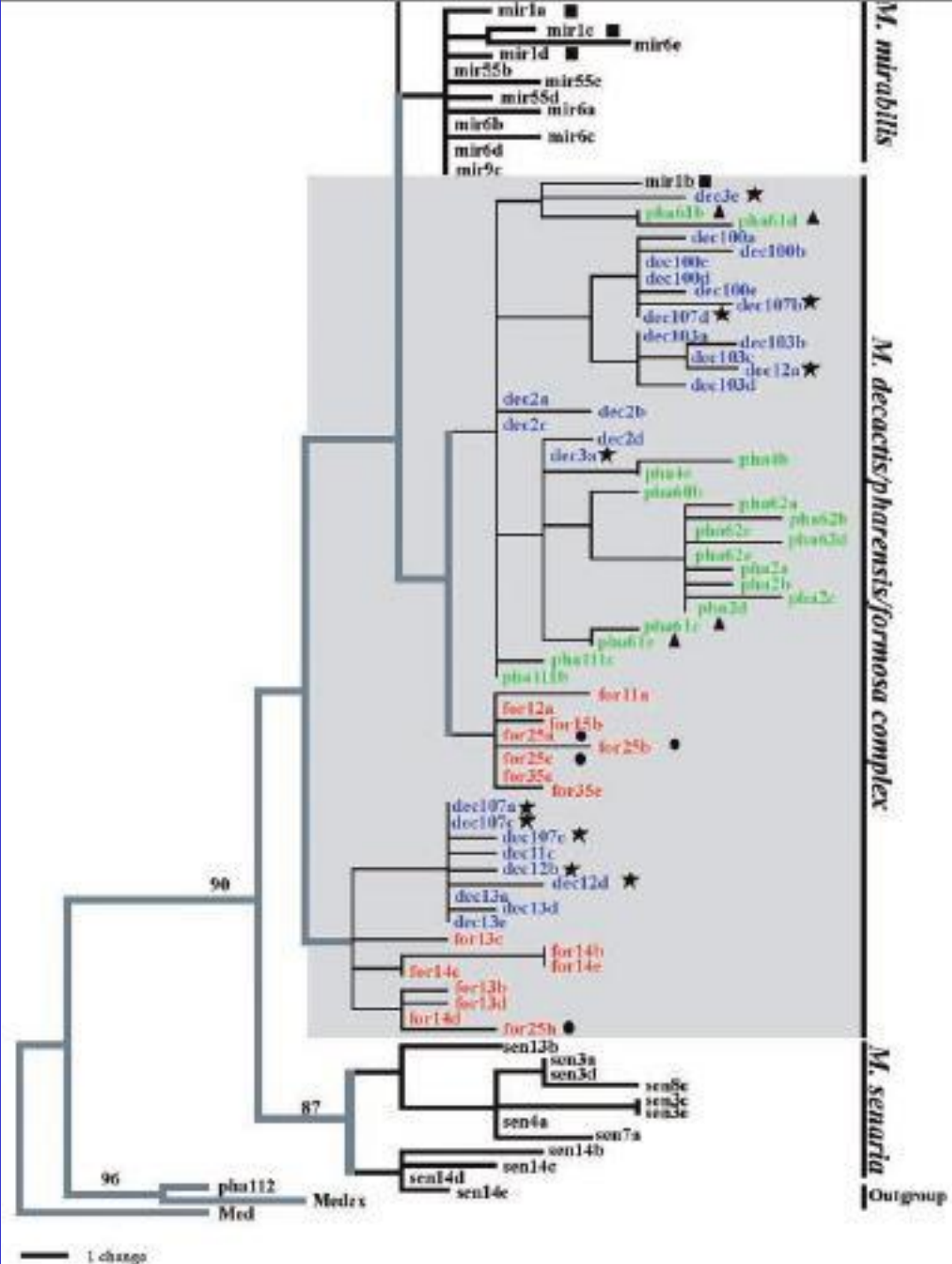
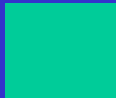
# Results I



# Quantitative comparison simulated and actual growth forms *Madracis* sp.



# Genetic comparison Madracis species (Diekmann et al., 2001; Frade et al., 2009); M. V. Filatov, P. R. Frade, , R. P.M. Bak, M. J.A. Vermeij, and J. A. Kaandorp,, Plos One, 2013



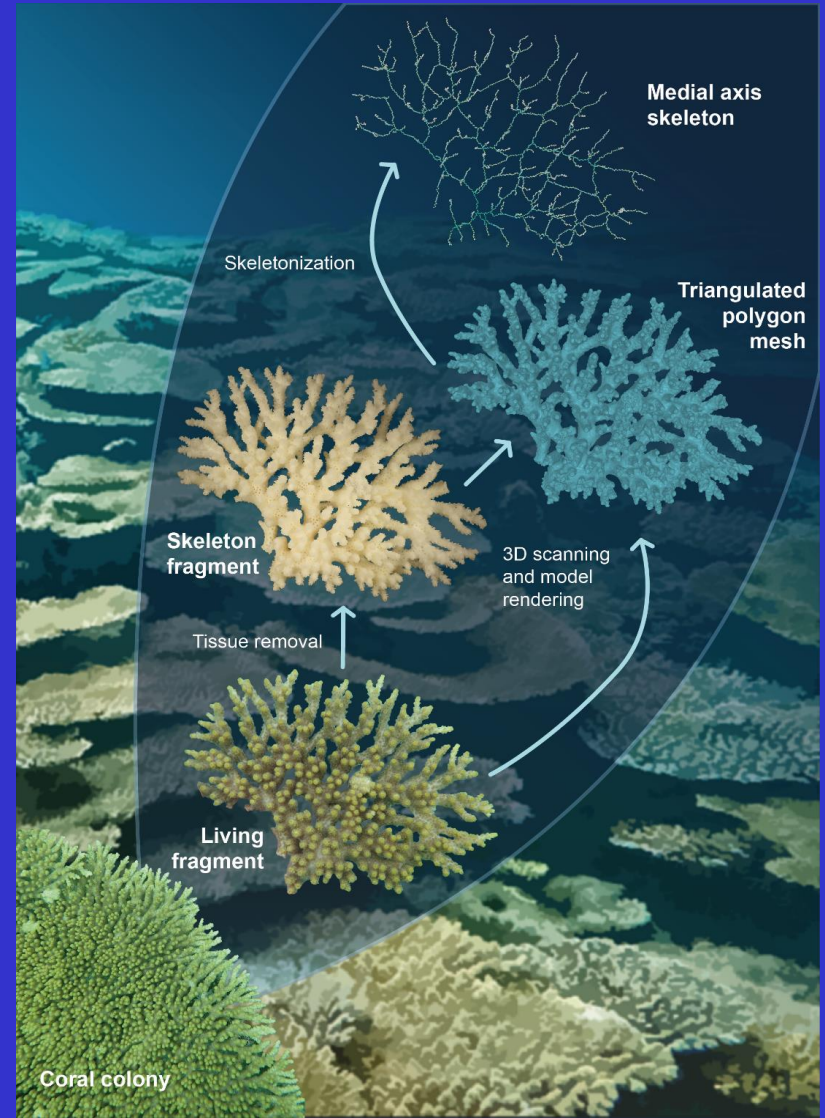
Quantitative three-dimensional morphological analysis supports species discrimination in complex-shaped and taxonomically challenging corals,

C. Ramirez-Portilla , I. M. Bieger ,R.t G. Belleman , T. Wilke, Jean-Francois Flot ,A. H. Baird , S. Harii , F. Sinniger and J. A. Kaandorp  
September 2022. Frontiers in Marine Science 9:955582,  
DOI: 10.3389/fmars.2022.955582

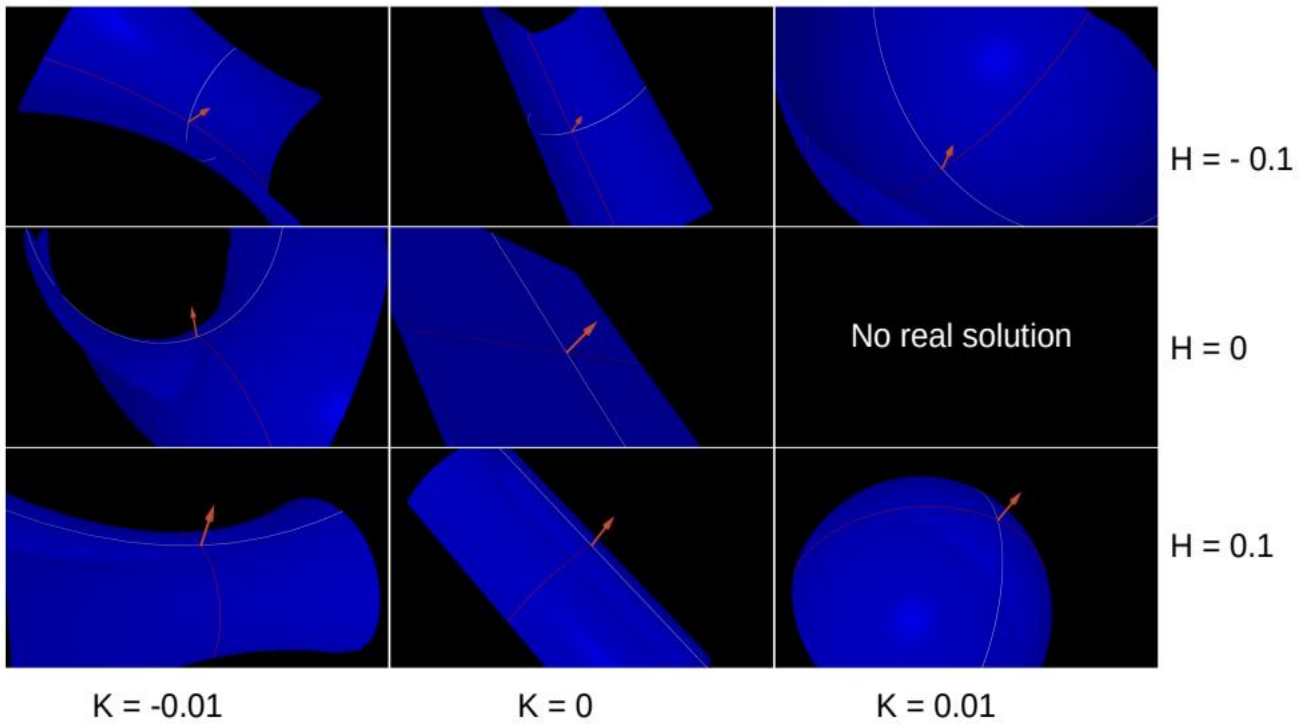
Develop quantitative measures to characterize morphology using high resolution polygon meshes from three closely related *Acropora* (*A.*) species (*C. Ramirez-Portilla, I Bieger et al., submitted*):

- *A. cf. bifurcata*
- *A. cf. cytherea*
- *A. aff. hyacinthus*

Which 3D-derived metrics can aid to delineate these species?







## Curvature of a surface

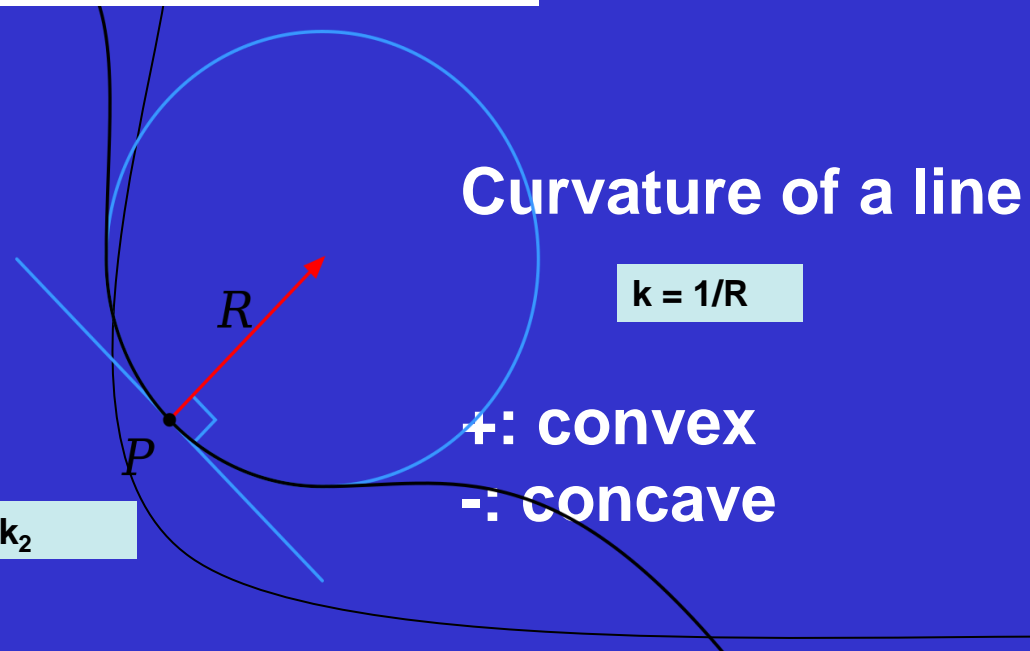
$k_1$  : maximum curvature

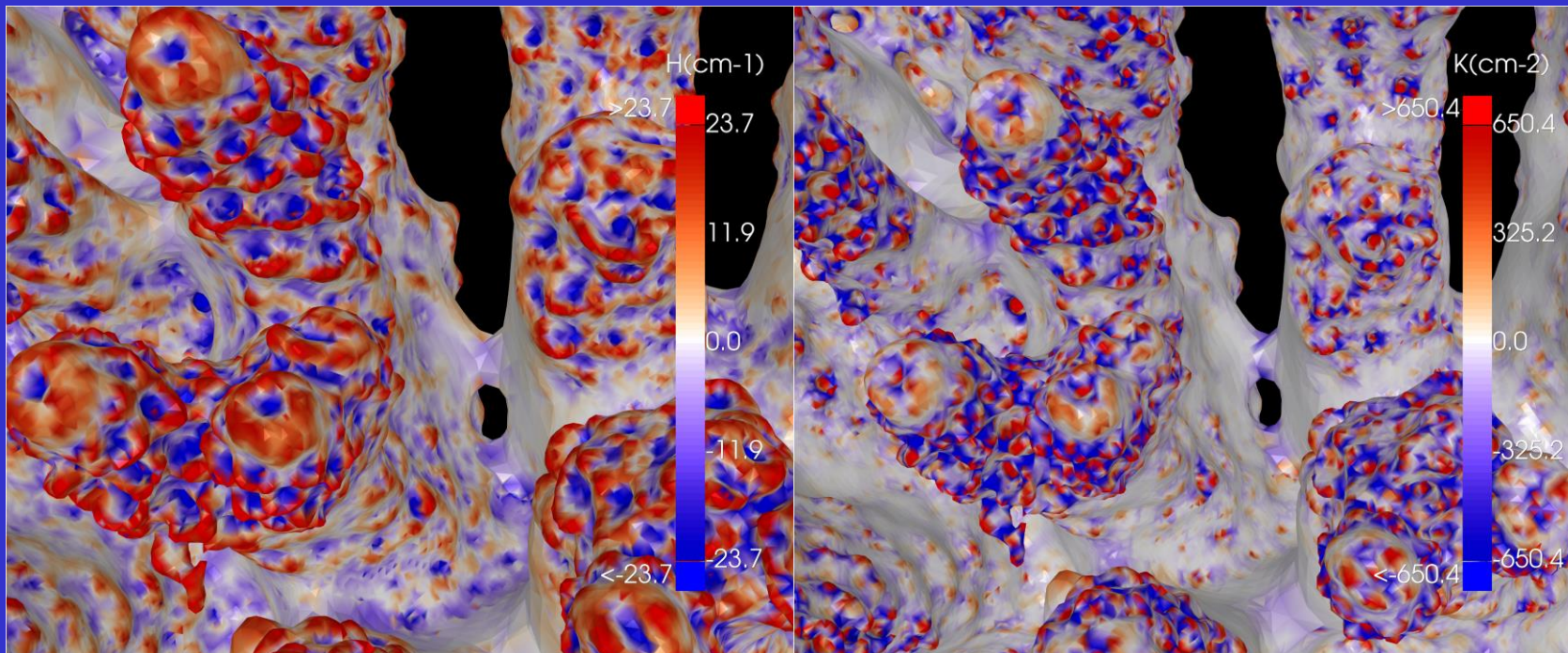
$k_2$  : minimum curvature

Mean (H) curvature:

$$H = (k_1 + k_2)/2$$

Gaussian (K) curvature  $K = k_1 * k_2$





Species A

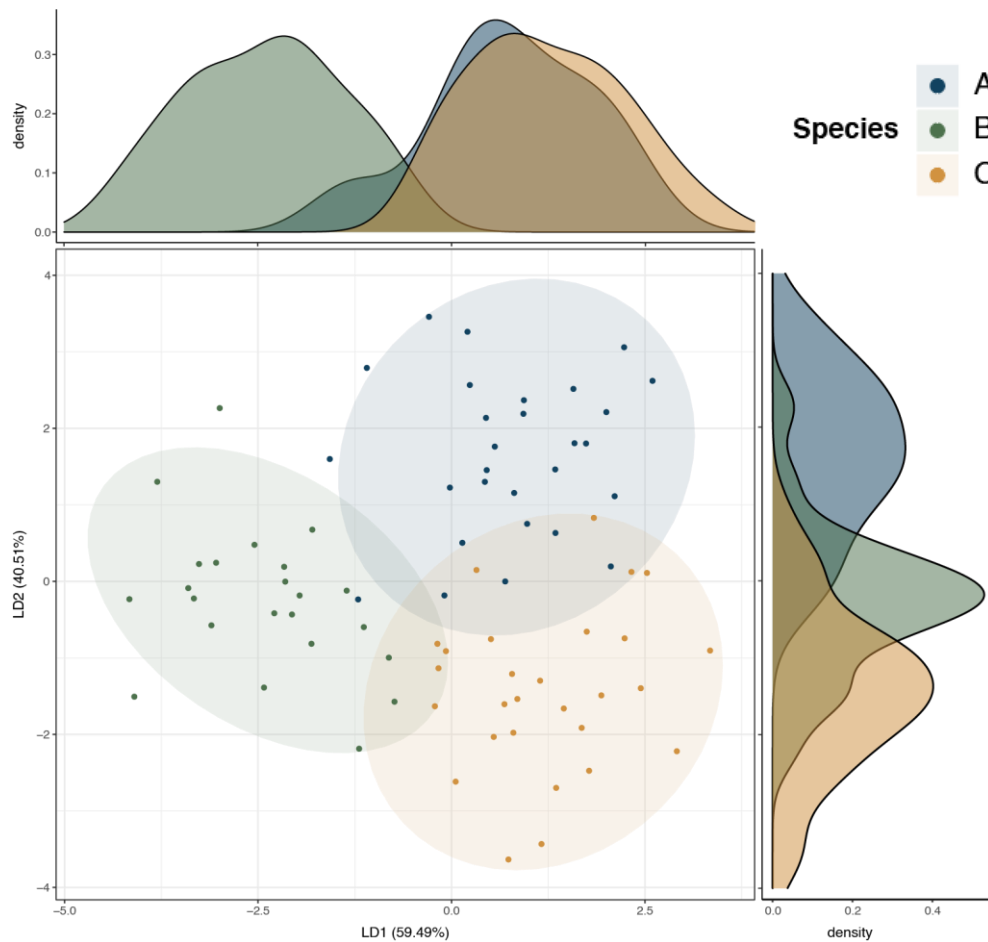


Species B



Species C





## Linear discriminant analysis (LDA)

LDA	Allocated to A	Allocated to B	Allocated to C
A	23	2	3
B	0	22	1
C	2	0	26

**89.87% of discriminative power (71/79 specimens)**

# Conclusions and Open Questions

- Many crucial parts of information are still missing, there are many gaps in the knowledge of molecular biology and the physiology of calcification
- Many (Most) details about gene regulation of calcification are missing
- The genome of a scleractinian coral and its symbiont are available, important for research on gene regulation of calcification
- How are gene expression in the host (the coral) and symbiont related is not very well known
- Models can be used to infer regulatory networks from gene expression data, understand the fluxes in complicated metabolic pathways, study the influence of the physical environment in detail, to study how the different processes at very different scales in time and space are coupled
- Models can be used to organize data and data collection and to detect the missing pieces of knowledge in a systematic way

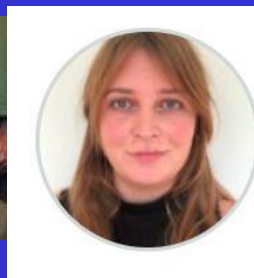
# Acknowledgements



**Amir Abdol**



**Carlos Tamulonis**



**Helena Willard**



**Roland Dries**



**Paula Ramos-Silva**



**Frederic Marin  
Dijon**



**Renske Vroomans,  
University Cambridge**



**Grisha  
Genikhovich,  
University Vienna**



**Stefano  
Goffredo  
Univ Bologna**



**Jean-Francois Flot  
Univ Brussels**



**Aizhan Shagadatova**



**Imke Lansky**



**Maarten van  
der Sande**



**Coen Honingh**



**Koen Gruell**

# References I

- A.M. Abdol, D. Cicin-Sain, J. A Kaandorp, A. Crombach, [Scatter Search Applied to the Inference of a Development Gene Network](#), *Computation* 5:22-, 2017, doi:[10.3390/computation5020022](https://doi.org/10.3390/computation5020022)
- Amir M Abdol, Eric Röttinger, Fredrik Jansson, Jaap A Kaandorp, A novel technique to combine and analyse spatial and temporal expression datasets: A case study with the sea anemone *Nematostella vectensis* to identify potential gene interactions, *Developmental biology*, 428:204-214, 2017
- F.A. Al-Horani and S.M. Al-Moghrabi and D. de Beer. The mechanism of calcification and its relation to photosynthesis and respiration in the scleractinian coral *Galaxea fascicularis*, *Mar. Biol.*, 2003, 142:419-426
- D. Allemand, E´. Tambutt´e, D. Zoccola, S. Tambutt´e, Coral calcification, cells to reefs, in: Z. Dubinsky, N. Stambler (Eds.), *Coral Reefs: An Ecosystem in Transition*, Springer Netherlands, Dordrecht, 2011, pp. 119–150.

# References II

- E.E. Ball et al., A simple plan - cnidarians and the origins of developmental mechanisms, *Nature Genetics*, 2004, 5: 567-577
- M.F. Barnsley, *Fractals everywhere*, Academic Press, Boston, 1988
- D. Botman, E. Rottinger, M. Q. Martindale, J. de Jong and J. A. Kaandorp, Computational Approach towards a Gene Regulatory Network for the Developing *Nematostella vectensis* Gut., *Plos One*, 9: e103341, 2014
- S. Brenner, Sequences and consequences *Phil. Trans. R. Soc. B* (2010) 365: 207–212



# References III

- C. Chia-Miin, The effect of ocean acidification and warming on early life history stages of corals, PhD thesis James Cook University, 2012
- N. Chindapol , J. A. Kaandorp , C. Cronemberger, T. Mass and A. Genin Modelling growth and form of the scleractinian coral *Pocillopora verrucosa* and the influence of hydrodynamics, PLOS Computational Biology, 9, e1002849, 2013
- [M. F. Colombo-Pallotta](#), [A. Rodríguez-Román](#), [Roberto Iglesias-Prieto](#), Calcification in bleached and unbleached *Montastraea faveolata*: Evaluating the role of oxygen and glycerol, [Coral Reefs](#) 29(4):899-907, 2010, [10.1007/s00338-010-0638-x](#)
- S. Douady and Y. Couder, Phyllotaxis as a physical self-organized process, Phys. Rev. Lett. 68:2098-2101, 1992

# References III

- M.V. Filatov, J.A. Kaandorp, M. Postma, R. van Liere, K.J. Kruszynski, M.J.A. Vermeij, G.J. Streekstra and R.P.M. Bak, A comparison between coral colonies from the *Madracis* genus and simulated forms, Proc. R. Soc. B 277:3555-3561, 2010
- M. V. Filatov, P. R. Frade, , R. P.M. Bak, M. J.A. Vermeij, and J. A. Kaandorp, Comparison between colony morphology and molecular phylogeny in the Caribbean scleractinian coral genus *Madracis*, Plos One Plos One 8, e71287, 2013
- E. Fox Keller, Making sense of life:explaining biological development with models, metaphors and machines, Harvard University Press, Cambridge, 2002
- Fukuda I, Ooki S, Fujita T, Murayama E, Nagasawa H, Isa Y, Watanabe T (2003) Molecular cloning of a cDNA encoding a soluble protein in the coral exoskeleton. Biochem Biophys ResCom 304:11-17
- S.F. Gilbert, Developmental Biology, 6<sup>th</sup> edition, Sinauer Associates, Inc, 2000
- Thomas F Goreau, THE PHYSIOLOGY OF SKELETON FORMATION IN CORALS. I. A METHOD FOR MEASURING THE RATE OF CALCIUM DEPOSITION BY CORALS UNDER DIFFERENT CONDITIONS, Biol Bull, 1959, 116,:59-75

# References V

- Y. Fomekong Nanfack, J.A. Kaandorp and J.G. Blom Efficient parameter estimation for spatio-temporal models of pattern formation: Case study of *Drosophila melanogaster* *Bioinformatics* 23:3356-3363, 2007
- Y. Fomekong Nanfack, M. Postma J.A. Kaandorp, Inferring *Drosophila* gap gene regulatory network: a parameter sensitivity and perturbation analysis *BMC Systems Biology*, 3:94, 2009a.
- Y. Fomekong Nanfack, M. Postma J.A. Kaandorp, Inferring *Drosophila* gap gene regulatory network: pattern analysis of gene expression profiles and stability analysis, *BMC Research Notes*, 2:256, 2009b.

# References IV

- S. He, F. del Viso, C. Chen, A. Ikmi, A. E. Kroesen, M. C. Gibson , An axial Hox code controls tissue segmentation and body patterning in *Nematostella vectensis*, *Science* 361:1377–1380, 2018
- H. Honjo and S. Ohta and M. Matsushita, Irregular fractal-like crystal growth of ammonium chloride, *J. Phys. Soc. Japan*, 55:2487-2490, 1986
- J.A. Kaandorp, P.M.A. Sloot, R.M.H. Merks, R.P.M. Bak and M.J.A. Vermeij, Morphogenesis of the branching reef coral *Madracis mirabilis*, *Proc. Roy. Soc. B.* 272:127-133, 2005.
- Hiroaki Kitano, Computational systems biology, *Nature* 420:206-210, 2002
- Y. Kraus and U. Technau, Gastrulation in the sea anemone *Nematostella vectensis* occurs by invagination and immigration: an ultrastructural study *Dev Genes Evol* (2006) 216: 119–132, DOI 10.1007/s00427-005-0038-3
- K. Kruszynski, J.A. Kaandorp and R. van Liere A computational method for quantifying morphological variation in scleractinian corals, *Coral Reefs* 26:831-840, 2007

# References V

- C. R. Magie , Marymegan Daly , Mark Q. Martindale, Gastrulation in the cnidarian *Nematostella vectensis* occurs via invagination not ingression, *Developmental Biology* 305 (2007) 483–497
- Tali Mass and Amatzia Genin, Environmental versus intrinsic determination of colony symmetry in the coral *Pocillopora verrucosa*, *Mar Ecol Prog Ser*, 369: 131–137, 2008, doi: 10.3354/meps07578
- T. McConnaughey, J. Whelan, Calcification generates protons for nutrient and bicarbonate uptake, *Earth-Science Reviews* 42 (1-2) (1997) 75–117
- E. Mjolsness and D.H. Sharp and J. Reinitz. A connectionist model of development, *J. Theor. Biol.*, 1991, 152: 429-453
- E.W.A.Mulder, Fibonacci patroon ook bij fossiele kolonie vormende algen, *Bionieuws*, 7 juli, 2023
- L. Muscatine and E. Cernichiari, ASSIMILATION OF PHOTOSYNTHETIC PRODUCTS OF ZOOXANTHELLAE BY A REEF Coral, *Biol. Bull.*, 137: 506-523, 1969, <https://doi.org/10.2307/1540172>

# References VI

- T. Nakamura, R. van Woesik, Water-flow rates and passive diffusion partially explain differential survival of corals during the 1998 bleaching event, *Mar Ecol Prog Ser.* 212: 301–304, 2001
- C. Ramirez-Portilla , I. M. Bieger ,R.t G. Belleman , T. Wilke, Jean-Francois Flot ,A. H. Baird , S. Harii , F. Sinniger and J. A. Kaandorp Quantitative three-dimensional morphological analysis supports species discrimination in complex-shaped and taxonomically challenging corals, September 2022. [Frontiers in Marine Science](#) 9:955582, DOI: [10.3389/fmars.2022.955582](#)
- P. Ramos-Silva, F. Marin, J.A. Kaandorp, and B. Marie, « Biomineralization toolkit »: the importance of sample cleaning prior to the characterization of biomineral proteomes, *PNAS* ., 3–5. doi:10.1073/pnas.1303657110, 2013
- P. Ramos-Silva J.A, Kaandorp, L. Huisman, B. Marie, I. Zanella-Cléon<sup>4</sup>, N. Guichard, D.J. Miller and F. Marin, The skeletal proteome of the coral *Acropora millepora*: the evolution of calcification by cooption and domain shuffling, *Molecular Biology and Evolution*, 30:2099-2112, 2013  
<http://mbe.oxfordjournals.org/content/early/2013/06/12/molbev.mst109.full.pdf>

# References VII

- **Reyes-Bermudez, Alejandro (2009) *Cellular mechanisms of coral calcification*. PhD thesis, James Cook University**
- B. Rinkevich and Y. Loya, Does light enhance calcification in hermatypic corals?, *Marine Biology* 80, 1-6 (1984)
- M van der Sande, Y Kraus, E Houliston, J Kaandorp [A cell-based boundary model of gastrulation by unipolar ingression in the hydrozoan cnidarian \*Clytia hemisphaerica\*](#), *Developmental Biology* 460 (2), 176-186
- [K. SIMKISS](#), PHOSPHATES AS CRYSTAL POISONS OF CALCIFICATION, *Biological Reviews*, 39: 487-504, 1964, <https://doi.org/10.1111/j.1469-185X.1964.tb01166.x>
- Slavkov, D. Carrillo-Zapata, N. Carranza, X. Diego, F. Jansson, J. Kaandorp, S. Hauert, J. Sharpe, Morphogenesis in Robotic Swarms, *Science Robotics*, DOI: 10.1126/scirobotics.aau9178, 2018

# References VII

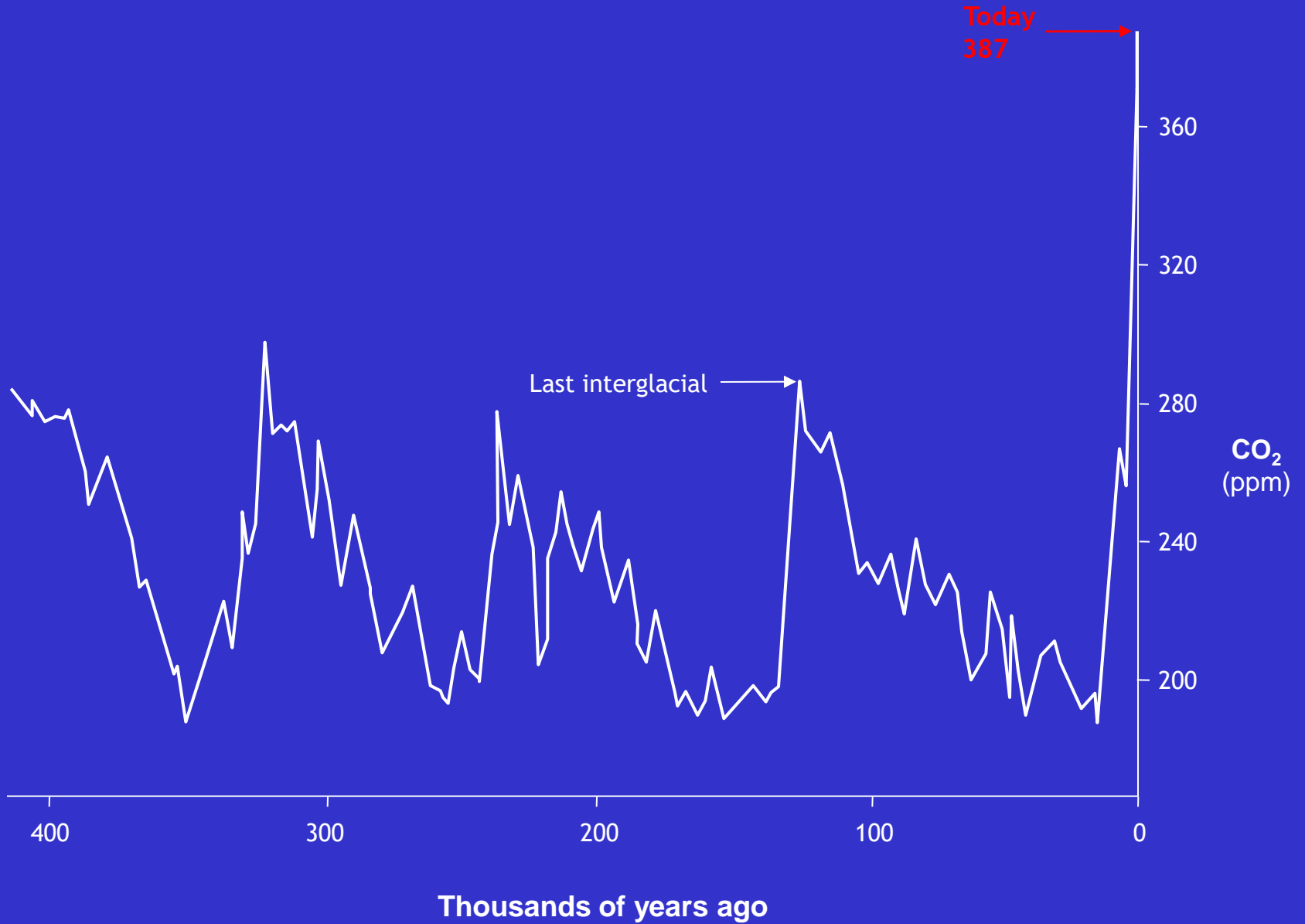
- I. Taubner, M. Y. Hu, A. Eisenhauer, M. Bleich, Electrophysiological, evidence for light-activated cation transport in calcifying corals, *Proceedings of the Royal Society B* 286 (1896) (2019) 20182444
- C. Tamulonis, M. Postma, H. Marlow, C. Magie, J. de Jong and J.A. Kaandorp, Morphometrics & Modeling of *Nematostella vectensis* Gastrulation, *Developmental Biology* 351:217-228, 2011
- D.W. Thompson, *On growth and form*, Cambridge University Press, Cambridge, 1942
- M.D'A.A. Le Tissier and B. Clayton and B.E. Brown and P. Spencer Davies, Skeletal correlates of coral density banding and an evaluation of radiography as used in sclerochronology, *Mar. Ecol. Prog. Ser.*, 110:29-44, 1994
- Alexander Venn, Eric Tambutte' Michael Holcomb, Denis Allemand, Sylvie Tambutte' Live Tissue Imaging Shows Reef Corals Elevate pH under Their Calcifying Tissue Relative to Seawater, *Plos One*, Volume 6, Issue 5, e20013, 2011
- J.E.N. Veron and M. Pichon, Scleractinia of eastern Australia part 41. *Environ Biol Fish* (2015) 98:1117–1131. doi:10.1007/s10641-014-0211-4



# References VI

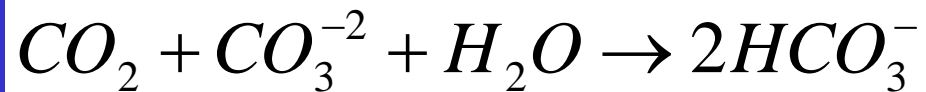
- W.H. de Weerd, A systematic revision of the north-eastern Atlantic shallow-water Haplosclerida (Porifera, Demospongiae), part II: Chalinidae, *Beaufortia*, 36:81-165, 1986
- H.F. Willard, E. S. Deutekom, D. Allemand, S. Tambutté, J. A. Kaandorp, Testing hypotheses on the calcification in scleractinian corals using a spatio-temporal model that shows a high degree of robustness, *Journal of Theoretical Biology*, Volume 561, 21 March 2023, 111382, <https://doi.org/10.1016/j.jtbi.2022.111382>
- Witten, T.A. and L.M. Sander, Diffusion-limited aggregation, a kinetic critical phenomenon, *Phys. Rev. Lett.* 47:1400-1403, 1981
- R. E. Zeebe, D. Wolf-Gladrow, CO<sub>2</sub> in seawater: equilibrium, kinetics, isotopes, no. 65, Gulf Professional Publishing, 2001

(Veron, 2009)



# In summary

- Dissolving  $\text{CO}_2$  in seawater increases the hydrogen ion ion ( $\text{H}^+$ ) concentration in the ocean and decreases ocean pH. Since the industrial revolution began, it is estimated that surface ocean pH has dropped by slightly less than 0.1 units (on the logarithmic scale of pH; approximately a 25% increase in  $\text{H}^+$ ), and it is estimated that it will drop by a further 0.3 to 0.5 units by 2100 as the oceans absorb more anthropogenic  $\text{CO}_2$  (see also wikipedia, ocean acidification) "



- Dissolving  $\text{CO}_2$  decreases carbonate ion ( $\text{CO}_3^{2-}$ ) concentration in the ocean and lowers the saturation state of carbonate minerals (see also wikipedia, ocean acidification)

# Saturation state of aragonite in corals (wikipedia)

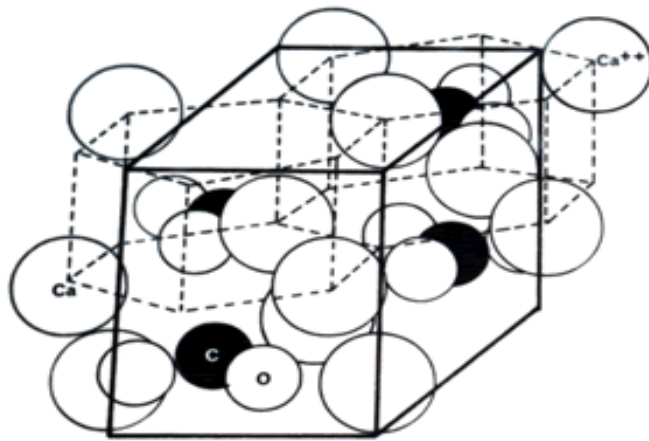
- "The saturation state of seawater for a mineral( $\Omega$ ) is a measure of the thermodynamic potential for the mineral to form or to dissolve; specifically it is the product of the concentrations (or activities) of the reacting ions that form the mineral ( $\text{Ca}^{2+}$  and  $\text{CO}_3^{2-}$ ), divided by the product of the concentrations of those ions when the mineral is at equilibrium ( $K_{sp}$ ), that is, when the mineral is neither forming nor dissolving.

$$\Omega_{sp} = \frac{[\text{Ca}^{2+}][\text{CO}_3^{2-}]}{K_{sp}}$$

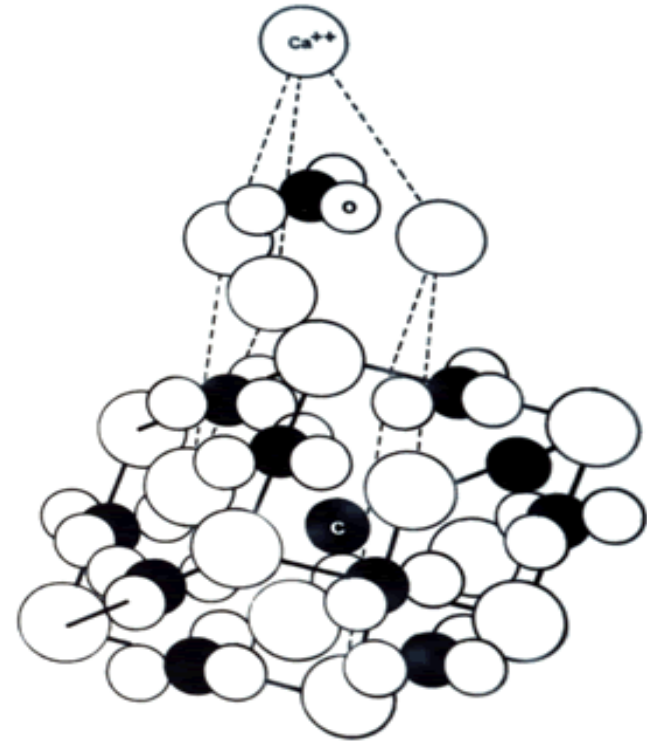
- In seawater, a natural boundary is formed as a result of temperature, pressure, and depth, and is known as the saturation horizon. It is above this saturation horizon that calcifying organisms live, as  $\text{CaCO}_3$  does not readily dissolve there
- Calcium carbonate exists in 2 commonly occurring forms: aragonite and calcite. The aragonite form is much more soluble than the calcite form which means that the aragonite saturation horizon is always nearer to the surface than the calcite saturation horizon. This means that those organisms that produce calcite may possibly be less vulnerable to changes in ocean acidity than those which produce aragonite (the scleractinian corals).

# CaCO<sub>3</sub> Crystals

CALCITE



ARAGONITE



— Unite cell  
- - - Pseudo-hexagonal prism

# carbonate minerals

Aragonite



Calcite



# Aragonite saturation state vs calcification rate (Leclercq et al., 2000)

